

Laboratory Assignment 5

Objectives

- Work with higher order functions
- Work with the `plot` package

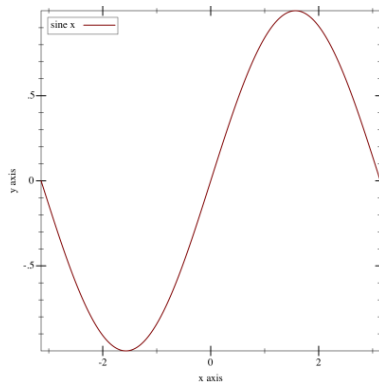
Activities

1. Let f and g be two functions, mapping integers to integers. Define a function `dominate` so that `(dominate f g)` outputs the smallest positive integer k for which $f(k) > g(k)$. Thus, if $f(1) > g(1)$, `(dominate f g)` should output 1. If $f(1) \leq g(1)$ but $f(2) > g(2)$, then `(dominate f g)` should output 2, etc.
2. [SICP Exercise 1.41]
Define a procedure `double` that takes a procedure of one argument as an argument and returns a procedure that applies the original procedure twice. For example, if `inc` is a procedure that adds 1 to its argument, then `(double inc)` should be a procedure that adds 2. What value is returned by `((double (double double)) inc) 5`?
3. So far this semester, we have written several functions which find the n^{th} number in a sequence which satisfies some property (e.g. the n^{th} even number). It would be helpful if we wrote a higher order function which could take a function which generated the sequence and a function which tested for the property in which we are interested as well as the integer n and returned the n^{th} value in that sequence which satisfied the property (i.e. the test function returns true when passed that value).
 - (a) Write a function, named `find`, which takes three parameters (`sequence`, `test`, and `n`) and returns the n^{th} value in `sequence` for which the `test` function returns true (`#t`) when passed a value in `sequence`.
 - (b) Test your program with by finding the 5^{th} of even number and the 5^{th} of odd number. Verify your results with the solutions to the problem sets and in the lecture slides.
 - (c) A Fibonacci prime is a Fibonacci number which is prime. Use your higher-order function to find the 5^{th} Fibonacci prime.
4. Racket also provides a graphing package, named `plot`, with which you can graph the functions you write in SCHEME. With Racket 5.2.1, change your language to “Use the language declared in the source” and add `#lang racket` as the first line in your Definitions window. To plot a function, start with the following two instructions which will import the plotting functions and create graphs in a new window.

```
(%require plot)
(plot-new-window? #t)
```

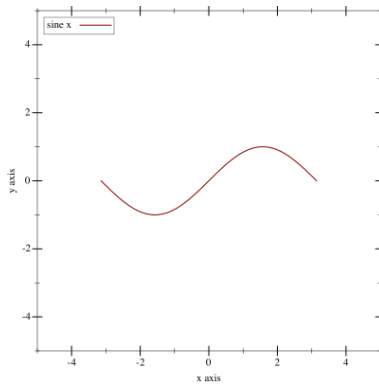
Next you can graph a function by using `plot`:

```
(plot (function sin (- pi) pi #:label "sine_x"))
```



where $(-\pi)$ and π determine the x-axis bounds. Additional plot keywords can be used to specify additional features of the plotted functions such as a legend and x and y bounds of the graph (separate from the bounds of the function to be graphed):

```
(plot (function sin (- pi) pi #:label "sine_x")
      #:x-min -5 #:x-max 5 #:y-min -5 #:y-max 5)
```



Plot the following function in the interval $[-5, 5]$, using Racket's plot capabilities:

```
(define (f x) (+ (* (sin x) (- 3 x)) 1))
```