Practice Exercise Key Week #2 (part 1)

The even-numbered problems are selected from the required textbook. The answers to these problems are given in a separate file. The link to the answers to next to the link to this file.

Section 1.5.

Find the dy/dx of the following functions

14.
$$y = 3x^{10}$$
 14. $30x^9$

18.
$$y = 3x^{-5}$$
 18. $-15x^{-6}$

26.
$$y = -4.8x^{1/3}$$
 26. $-1.6x^{-2/3}$

Find the derivative of the following functions (Hint: simplifying before taking derivative if n)

30.
$$\frac{d}{dx} \left(\sqrt[3]{x} + \frac{4}{\sqrt{x}} \right)$$
 30. $\frac{1}{3\sqrt[3]{x^2}} - \frac{2}{x\sqrt{x}}$

38.
$$f(x) = \frac{5}{x} - x^{2/3}$$
 38. $-\frac{5}{x^2} - \frac{2}{3}x^{-1/3}$

48.
$$y = \frac{2}{x} - \frac{x}{2}$$
 48. $-\frac{2}{x^2} - \frac{1}{2}$

56. If
$$y = \frac{1}{3x^4}$$
, find $\frac{dy}{dx}$ at $x = -1$. **56.** $\frac{4}{3}$

For each function, find the points on the graph at which the tangent line is horizontal. If none exist, state that fact.

64.
$$y = -x^3 + 1$$

66.
$$y = 3x^2 - 5x + 4$$
 66. $\left(\frac{5}{6}, \frac{23}{12}\right)$

66.
$$\left(\frac{5}{6}, \frac{23}{12}\right)$$

78.
$$f(x) = \frac{1}{3}x^3 + \frac{1}{2}x^2 - 2$$

78.
$$f(x) = \frac{1}{3}x^3 + \frac{1}{2}x^2 - 2$$
 78. $(0, -2), (-1, -\frac{11}{6})$

For each function, find the points on the graph at which the tangent line has slope 1

80.
$$y = 20x - x^2$$

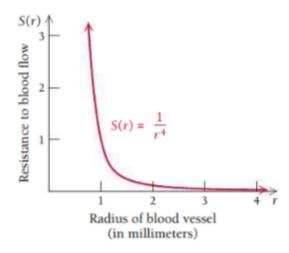
86.
$$y = \sqrt{x} + \frac{1}{2}x$$

86.
$$(1,\frac{3}{2})$$

90. Blood flow resistance. The equation

$$S(r) = \frac{1}{r^4}$$

can be used to determine the resistance to blood flow, S, of a blood vessel that has radius r, in millimeters (mm). (Source: Mathematics Teacher, Vol. 99, No. 4, November 2005.)



- a) Find the rate of change of resistance with respect to r, the radius of the blood vessel.
- **b)** Find the resistance at r = 1.2 mm.
- c) Find the rate of change of S with respect to r when r = 0.8 mm.

90. (a)
$$S'(r) = -\frac{4}{r^5}$$
;

- (b) 0.4823 unit of resistance;
- (c) -12.2 units of resistance per millimeter