## STA 504 Homework #4

Due: Monday, October 02

Show you're your work to earn full credit. You are encouraged to work with your peers on assignments. The write-up must be your own.

4.60 A normally distributed random variable has density function

$$f(y) = \frac{1}{\sigma\sqrt{2\pi}} e^{-(y-\mu)^2/(2\sigma^2)}, \qquad -\infty < y < \infty.$$

Using the fundamental properties associated with any density function, argue that the parameter  $\sigma$  must be such that  $\sigma > 0$ .

- **4.61** What is the median of a normally distributed random variable with mean  $\mu$  and standard deviation  $\sigma$ ?
- **4.62** If Z is a standard normal random variable, what is

a 
$$P(Z^2 < 1)$$
?

Subtitle

**b** 
$$P(Z^2 < 3.84146)$$
?

## Problem 4.

The lifetime (in hours) Y of an electronic component is a random variable with density function given by

$$f(y) = \begin{cases} \frac{1}{100} e^{-y/100}, & y > 0, \\ 0, & \text{elsewhere.} \end{cases}$$

Based on the above distribution answer the following questions.

- 1. Show that f(y) is a valid density function.
- 2. Derive the cumulative distribution function (CDF) of the lifetime variable.
- 3. Derive the expectation and variance of Y.
- 4. Find P(Y > 150) using the CDF derived in part 2.
- 5. Find P(Y > 150 | Y > 100) using CDF.

