

# STA 504 Mathematical Statistics I with Calculus Review

Fall 2022

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**Office Hours:** Monday: 3:00 PM-5:00 AM  
Tuesday/Thursday: 1:00 PM – 5:00 PM

**Course Web Page:** D2L.

**Class Meeting:** Monday 5:45 PM - 9:30 PM in UNA

**Required Text:** *Mathematical Statistics with Applications*, 7th edition Wackerly, Mendenhall, and Scheaffer.

## COURSE DESCRIPTION

A rigorous treatment of probability spaces and an introduction to the estimation of parameters. This course will also review relevant calculus topics.

## STUDENT LEARNING OUTCOMES FOR MS IN APPLIED STATISTICS

1. Demonstrate an understanding of probability and statistical inference, including the fundamental laws of classical probability, discrete and continuous random variables, expectation theory, maximum likelihood methods, hypothesis testing, power, and bivariate and multivariate distribution theory.
2. Demonstrated the ability to apply the elementary methods of statistical analysis, namely those based on classical linear models, categorical methods, and non-parametric ideas to perform data analysis for statistical inference.
3. Demonstrate proficiency in the effective use of computers for research data management and analysis of data with standard statistical software packages, particularly SAS.
4. Learn to develop and critically assess the design of experimental studies and the collection of data.
5. Apply one or more methods of statistical inference to a particular area of interest, particularly the program in the elective concentration.

6. Gain practical experience in statistical consulting and communicating with non- statisticians, culminating with interaction with research workers at a local company as part of the internship practicum.

### **COURSE OBJECTIVES**

1. To review basic concepts from calculus. These include, but are not limited to, limits, differentiation, and integration techniques. [SLO 1]
2. To introduce the basic ideas and methods of probability theory. [SLO 1]
3. To illustrate the rich diversity of applications of probability theory in the sciences. [SLO 1]
4. To develop the probabilistic foundations for the study of mathematical statistics. [SLO 1]

### **POLICIES ON HOMEWORK**

There will be regular homework assignments for this class. The assigned problems reflect the contents covered in the class. Following policies apply to the homework of this class

1. No later homework will be accepted.
2. You are assumed to complete all problems assigned each time. I may randomly pick a few of them to grade. Your HW grade will be based on the randomly selected ones. I will post the detailed solutions to each of the assigned problems on the course web page.
3. **Collaboration:** you are encouraged to work together on homework problems. However, the write-up **MUST** be your own (be aware of the University's policies on academic integrity).
4. Please submit organized, neat, and stapled paper copies of homework. You are strongly encouraged to prepare your homework using RMarkdown.

### **EVALUATION & GRADING**

The course grade will be based on

- (1). Homework (30%)
- (2). Two Midterm Exams (20% each)
- (3). Final Comprehensive Exam (30%).

A letter grade will be assigned based on performance in the course, according to the following scale:

Grade	Quality Points	Percentage Equivalents	Interpretation
A	4.00	[93%, 100%]	Superior graduate attainment
A-	3.67	[90%, 93%)	
B+	3.33	[86%, 90%)	Satisfactory graduate attainment
B	3.00	[83%, 86%)	
B-	2.67	[80%, 83%)	
C+	2.33	[76%, 80%)	Attainment below graduate expectations
C	2.00	[73%, 76%)	
C-	1.67	[70%, 73%)	
F	0	< 70%	Failure

D grades are not used. Refer to the Graduate Catalog for a description of NG (No Grade), W, & other grades.

### TENTATIVE TOPICS

Following is the list of tentative topics to be covered in the semester. I may modify and list as we move forward during the semester.

#### Topic 1: Basic Probability Theory [CO 1] (Sections 2.1 - 2.11)

- Calculus Review: functions, sequence, and limit.
- Counting Rules and Definitions of Probability
- Laws of Probability
- Conditional Probability
- Bayes Theorem

#### Topic 2: Discrete Random Variables [CO 1,2] (Sections 3.1 - 3.8)

- Calculus Review: Derivatives of single variable functions
- Definition of Discrete Random Variable (Distribution)
- Partial Characterization of the Distribution of Random Variable:
- Special Discrete Random Variables / Distributions
  - Binomial distribution
  - Poisson distribution

#### Topic 3. Continuous Random Variables [CO 1,2] (Sections 4.1 - 4.8)

- Calculus Review: Integrals of single-variable real functions
- Definitions and Characterization of Continuous Variables
- Special continuous distributions

- Uniform distribution
- Normal distribution
- Exponential and Weibull distribution
- Gamma distribution

**Topic 4.** Concepts of Mixture Distributions (Expanded Section 4.11)

- Calculus Review: Piece-wise functions
- Definition of a Mixture Distribution
- Overview of Applications of Mixture Distributions
- Characterizations of Mixture distributions
- Special Mixture Distributions: k-component normal mixture models

**Midterm Exam #1: 10/3**

**Topic 5.** Moment Generating Functions [CO 3] (Sections 3.9, 4.9)

- Calculus Review: Taylor Expansions
- Definition of Moment Generating Function (MGF)
- Applications of MGF
- Limiting Distributions

**Topic 6.** Joint Probability Distributions [CO 1,2] (Sections 5.1 - 5.2)

- Calculus Review: Functions with multiple variables
- Bivariate Random Variables
- Characterizations
  - Discrete distribution function
  - Continuous distribution functions

**Topic 7.** Marginal and Conditional Probability Distributions [CO 1,2] (Sections 5.3)

- Calculus Review: partial derivatives and double integrals
- Marginal Distributions: Integrations and Implications
- Conditional Distributions: Integrations and Implications

**Topic 8.** Independent Variables and Functional Random Variable [CO 1,2] (Sections 5.4 - 5.6)

- Calculus Review: More on double summations and double integrals
- Independent distributions
- Expectations and Variance of a Function of Random Variables

## Midterm Exam #2: 11/14

### Topic 9. Covariance of Several Random Variables [CO 1, 2][Sections 5.7- 5.8, 5.11]

- Calculus Review: The double integral over non-rectangular regions
- Covariance and Covariance Matrix
- Expectations and Variance of Linear Functions of Random Variables
- Special Results about Expectations

### Topic 10. Functions of Random Variables – Part I [CO 3] (Sections 6.1 - 6.3)

- [Calculus Review](#): Inverse Functions
- Distribution of a Function of Variables
- Methods of Distribution Functions
- Random Number Generation

### Topic 11. Functions of Random Variables – Part II [CO 3] (Sections 6.4 - 6.6)

- Calculus Review
  - Review of Matrix and Determinant
  - The derivative of implicit functions
- The Method of Transformation
- The Method of Moment Generating Function
- The Method of Multivariable Transformation

### Topic 12. Order Statistics [CO 3] (Sections 6.7) ([optional](#))

## ACADEMIC & PERSONAL INTEGRITY

It is the responsibility of each student to adhere to the university's standards for academic integrity. Violations of academic integrity include any act that violates the rights of another student in academic work, that involves misrepresentation of your work, or that disrupts the instruction of the course. Other violations include (but are not limited to): cheating on assignments or examinations; plagiarizing, which means copying any part of another's work and/or using ideas of another and presenting them as one's own without giving proper credit to the source; selling, purchasing, or exchanging of term papers; falsifying of information; and

using your own work from one class to fulfill the assignment for another class without significant modification. Proof of academic misconduct can result in the automatic failure and removal from this course. For questions regarding Academic Integrity, the No-Grade Policy, Sexual Harassment, or the Student Code of Conduct, students are encouraged to refer to the Department Graduate Handbook, the Graduate Catalog, the *Ram's Eye View*, and the University website at [www.wcupa.edu](http://www.wcupa.edu).

### **STUDENTS WITH DISABILITIES**

If you have a disability that requires accommodations under the Americans with Disabilities Act (ADA), please present your letter of accommodations and meet with me as soon as possible so that I can support your success in an informed manner. Accommodations cannot be granted retroactively. If you would like to know more about West Chester University's Services for Students with Disabilities (OSSD), please visit them at 223 Lawrence Center. The OSSD hours of Operation are Monday – Friday, 8:30 a.m. – 4:30 p.m. Their phone number is 610-436-2564, their fax number is 610-436-2600, their email address is [ossd@wcupa.edu](mailto:ossd@wcupa.edu), and their website is at [www.wcupa.edu/ussss/ossd](http://www.wcupa.edu/ussss/ossd).

### **REPORTING INCIDENTS OF SEXUAL VIOLENCE**

West Chester University and its faculty are committed to assuring a safe and productive educational environment for all students. In order to meet this commitment and to comply with Title IX of the Education Amendments of 1972 and guidance from the Office for Civil Rights, the University requires faculty members to report incidents of sexual violence shared by students to the University's Title IX Coordinator, Ms. Lynn Klingensmith. The only exceptions to the faculty member's reporting obligation are when incidents of sexual violence are communicated by a student during a classroom discussion, in a writing assignment for a class, or as part of a University-approved research project. Faculty members are obligated to report sexual violence or any other abuse of a student who was, or is, a child (a person under 18 years of age) when the abuse allegedly occurred to the person designated in the University protection of minor's policy. Information regarding the reporting of sexual violence and the resources that are available to victims of sexual violence is set forth at the webpage for the Office of Social Equity at <http://www.wcupa.edu/admin/social.equity/>.

### **EXCUSED ABSENCES POLICY**

Students are advised to carefully read and comply with the excused absences policy, including absences for university-sanctioned events, contained in the WCU Graduate Catalog. In particular, please note that the “responsibility for meeting academic requirements rests with the student,” that this policy does not excuse students from completing required academic work, and that professors can require a “fair alternative” to attendance on those days that students must be absent from class in order to participate in a University-Sanctioned Event.

### **EMERGENCY PREPAREDNESS**

All students are encouraged to sign up for the University’s free WCU ALERT service, which delivers official WCU emergency text messages directly to your cell phone. For more information, visit [www.wcupa.edu/wcualert](http://www.wcupa.edu/wcualert). To report an emergency, call the Department of Public Safety at 610-436-3311.

### **ELECTRONIC MAIL POLICY**

It is expected that faculty, staff, and students activate and maintain regular access to University-provided e-mail accounts. Official university communications, including those from your instructor, will be sent through your university e-mail account. You are responsible for accessing that mail to be sure to obtain official University communications. Failure to access will not exempt individuals from the responsibilities associated with this course.