

## STA 504 Homework #13

Due: Monday, December 11

Using transformation methods to find the following distributions.

### Problem 1.

Let continuous random vector  $(X_1, X_2)$  have joint probability density function

$$f_{X_1, X_2}(x_1, x_2) = \begin{cases} \frac{1}{4} e^{-(x_1 + x_2)/2}, & 0 < x_1 < \infty, 0 < x_2 < \infty; \\ 0, & \text{elsewhere.} \end{cases}$$

Define  $Y_1 = \frac{(X_1 - X_2)}{2}$  and  $Y_2 = \frac{(X_1 + X_2)}{2}$ . Find the joint probability distribution of  $Y_1$  and  $Y_2$ .

### Problem 2.

Let continuous random vector  $(X_1, X_2)$  have the joint probability density function

$$f_{X_1, X_2}(x_1, x_2) = \begin{cases} 10x_1x_2^2, & 0 < x_1 < x_2 < 1; \\ 0, & \text{elsewhere.} \end{cases}$$

Let  $Y_1 = X_1/X_2$  and  $Y_2 = X_2$ . Find the joint probability distribution of  $Y_1$  and  $Y_2$ .