Project real text

October 19, 2021

```
[1]: import sys
     from operator import add
     from pyspark.sql import SparkSession
     from pyspark import SparkContext
     import pyspark
     from pyspark.ml.linalg import Vectors
     import numpy as np
     from sklearn.linear_model import LinearRegression
     from pyspark.sql.types import *
     from pyspark.sql import functions as func
     from pyspark.sql.functions import *
     from pyspark.sql import SQLContext
     import matplotlib.pyplot as plt
     import time
     from pandas import Series, DataFrame
     import pandas as pd
     import re
     from collections import Counter
     from sklearn.linear_model import LinearRegression
     from pyspark.ml.classification import LogisticRegression
     from pyspark.ml.evaluation import MulticlassClassificationEvaluator
     from pyspark.ml.classification import LinearSVC
     # building functions
     def isfloat(value):
         try:
             float(value)
             return True
         except:
             return False
     def correctRows(p):
         if isfloat(p[3]) and isfloat(p[4]) and isfloat(p[6]) and isfloat(p[7]) and
     →isfloat(p[9]):
             return p
```

```
def to_list(a):
   return [a]
def addToList(x, y):
    x.append(y)
    return x
def extend(x,y):
   x.extend(y)
    return x
if __name__ == "__main__":
    if len(sys.argv) != 3:
        print("Usage: wordcount <file> <output> ", file=sys.stderr)
        exit(-1)
    spark = SparkSession.builder.master("local[*]").getOrCreate()
    sc = SparkContext.getOrCreate()
    sqlContext = SQLContext(sc)
    # load data set
    lines2 = sc.textFile("Google-Playstore.csv")
    # generate test case file
    df = pd.read_csv("Google-Playstore.csv")
    test_case = df.sample(n = 10000)
    test_case.to_csv('Google-Playstore_test.csv', index=False)
    11 11 11
    Simple Linear Regression
    11 11 11
    print("#### Finding Simple Linear Regression Equation ####")
    # data pre-processing
    correctLine = lines2.map(lambda x: x.split(','))
    cleaned = correctLine.filter(correctRows)
    max_install = cleaned.map(lambda p: (float(p[7])))
    rating = cleaned.map(lambda p: (float(p[3])))
    # apply linear regression
```

```
x = np.array(max_install.collect())
   y = np.array(rating.collect())
   X = np.stack([x], axis = 1)
   reg = LinearRegression(fit_intercept=True).fit(X, y)
   print("The m (coefficient) =",reg.coef_)
   print("The b (y-intercept) =",reg.intercept_)
   print("The equation is: y = "+str(reg.coef_[0])+"X + "+str(reg.intercept_))
   11 11 11
   Gradient Descent for parameters
   11 11 11
   print("#### Finding the parameters using gradient descent ####")
   start1 = time.time()
   df = np.stack([y, x], axis=1)
   dff = map(lambda x: (float(x[0]), Vectors.dense(x[1:])), df)
   mydf = spark.createDataFrame(dff, schema=["Money", "Distance"])
   myRDD=mydf.rdd.map(tuple).map(lambda x: (float(x[0]), np.array(x[1])))
   learningRate = 0.00001
   num iteration = 100
   size = float(len(y))
   beta = np.array([0.1])
   costs = []
   for i in range(num_iteration):
       gradientCost=myRDD.map(lambda x: (x[1], (x[0] - x[1] * beta)))
                               .map(lambda x: (x[0]*x[1], x[1]**2)).
\rightarrowreduce(lambda x, y: (x[0] +y[0], x[1]+y[1] ))
       cost= gradientCost[1]
       gradient=(-1/float(size))* gradientCost[0]
       print(i, "Beta", beta, " Cost", cost)
       beta = beta - learningRate * gradient
       costs.append(cost[0])
   end1 = time.time()
   print(f"Computation time of BGD is {(end1 - start1)/60} Minutes")
   # making plot
```

```
xValues = [i for i in range(len(costs))]
  plt.plot(xValues, costs, 'o', markersize=2)
  plt.xlabel("Number of Iteration")
  plt.ylabel("Cost")
  plt.title("Cost with the number of iteration")
  plt.show()
   nnn
  Multi-Linear Regression
   11 11 11
  print("#### Finding the parameters of multi-linear regression using ⊔

→gradient descent ####")
  start2 = time.time()
  rating = cleaned.map(lambda p: (p[0], p[3]))
  rating count = cleaned.map(lambda p: (p[0], p[4]))
  min_install = cleaned.map(lambda p: (p[0], p[6]))
  max_install = cleaned.map(lambda p: (p[0], p[7]))
  price = cleaned.map(lambda p: (p[0], p[9]))
  rating = rating.combineByKey(to_list, addToList, extend)
  rating = rating.collect()
  rating count = rating count.combineByKey(to list, addToList, extend)
  rating_count = rating_count.collect()
  min_install = min_install.combineByKey(to_list, addToList, extend)
  min_install = min_install.collect()
  max_install = max_install.combineByKey(to_list, addToList, extend)
  max_install = max_install.collect()
  price = price.combineByKey(to_list, addToList, extend)
  price = price.collect()
  ratingKey = []
  ratingValue = []
  for i in range(len(rating)):
      ratingKey.append(rating[i][0])
      rate = 0
       total = 0
       for j in [float(i) for i in rating[i][1]]:
           rate += j
           total += 1
```

```
ratingValue.append(rate/total)
ratingCountKey = []
ratingCountValue = []
for i in range(len(rating_count)):
    ratingCountKey.append(rating_count[i][0])
    rate = 0
    for j in [float(i) for i in rating_count[i][1]]:
        rate += j
    ratingCountValue.append(rate)
min_installKey = []
min_installValue = []
for i in range(len(min_install)):
    min_installKey.append(min_install[i][0])
    count = 0
    for j in [float(i) for i in min_install[i][1]]:
        if j != 0:
            count += 1
    min_installValue.append(count)
max_installKey = []
max_installValue = []
for i in range(len(max_install)):
    min_installKey.append(max_install[i][0])
    count = 0
    for j in [float(i) for i in max_install[i][1]]:
        if j != 0:
            count += 1
    max_installValue.append(count)
priceKey = []
priceValue = []
for i in range(len(price)):
    priceKey.append(price[i][0])
```

```
amount = 0
       for j in [float(i) for i in price[i][1]]:
           amount += j
       priceValue.append(amount)
   app = ratingKey
   rating = ratingValue
   countOfRating = ratingCountValue
   mi_install = min_installValue
   Price = priceValue
   ma_install = max_installValue
   x = []
   y = []
   for i in range(len(app)):
       x.append([float(rating[i]), float(countOfRating[i]),__
→float(mi_install[i]), float(Price[i])])
       y.append(float(ma_install[i]))
   learningRate = 0.000001
   num_iteration = 100
   size = len(y)
   costs = []
   beta = np.array([0.1, 0.1, 0.1, 0.1])
   data = \{'y':y, 'x':x\}
   df = DataFrame(data)
   spark_df_from_pandas = spark.createDataFrame(df, schema=['x', 'y'])
   myRDD=spark_df_from_pandas.rdd.map(lambda x: (float(x[0]), np.array(x[1])))
   for i in range(num_iteration):
       gradientCost=myRDD.map(lambda x: (x[1], (x[0] - x[1] * beta)))
                               .map(lambda x: (x[0]*x[1], x[1]**2)).
\rightarrowreduce(lambda x, y: (x[0] +y[0], x[1]+y[1] ))
       cost = 0
       for j in gradientCost[1]:
           cost += j
       gradient=(-1/float(size))* gradientCost[0]
       print(i, "Beta", beta, " Cost", cost)
       beta = beta - learningRate * gradient
```

```
costs.append(cost)
   end2 = time.time()
   print(f"Computation time of multi-linear regression by BGD is \{(end2 - \Box )\}
⇔start2)/60} minutes")
   xValues = [i for i in range(len(costs))]
   plt.plot(xValues, costs, 'o', markersize=2)
   plt.xlabel("Number of Iteration")
   plt.ylabel("Cost")
   plt.title("Cost with the number of iteration")
   plt.show()
   11 11 11
   Logistic Regression
   nnn
   print("#### gradient descent algorithm to learn a logistic regression⊔
→model #####")
   start3 = time.time()
   total_install = cleaned.map(lambda p: (p[0], p[7]))
   tuples = total_install.collect()
   appWords = []
   for i in app:
       words = i.split(" ")
       for j in words:
           j = re.sub('[^A-Za-z0-9]+', '', j)
           appWords.append(j)
   appWords = ' '.join(appWords).split()
   allWords = sc.parallelize(appWords)
   allCount = allWords.map(lambda x: (x, 1)).reduceByKey(add)
   topWords = allCount.top(20000, lambda x: x[1])
   topWordsK = sc.parallelize(range(20000))
   dictionary = topWordsK.map(lambda x: (topWords[x][0], x))
```

```
def TF(words_list, top_words):
      words_dict = dict(Counter(words_list))
      tf_vector = []
      for word in top_words:
           if word in words_dict.keys():
               tf = words_dict[word]
               tf_vector.append(tf)
           else:
               tf_vector.append(0)
      return tf_vector
  key_id = [i for i in range(len(tuples))]
  key_values = {tuples[i][0]: i for i in key_id}
  topWordsBC = sc.broadcast(dictionary.keys().collect())
  feat = cleaned.map(lambda x: (key_values[x[0]], TF(x[1], topWordsBC.value)))
  labels = cleaned.map(lambda x: (key_values[x[0]], int(x[0][0] == 'A' and_\( \)
\rightarrow x[0][1] == 'U')))
  trainRDD = feat.join(labels)
  learningRate = 0.0003
  num iteration = 5
  lambda cof = 0.01
  size = len(tuples)
  loss_list = list()
  parameter_vector = np.random.normal(0, 0.1, (dictionary.count(), 1))
  def sigmoid(x):
      return 1.0 / (1 + np.exp(-x))
  def loss_func(feat_line, y, parameter_vector):
      feat_line = np.array(feat_line)
      pred = sigmoid(np.dot(feat_line, parameter_vector))
      return -y * np.log(pred + 1e-12) - (1 - y) * np.log((1 - pred) + 1e-12)
  def accuracy_score(feat_line, y, parameter_vector):
      feat_line = np.array(feat_line)
      pred = sigmoid(np.dot(feat_line, parameter_vector))
      pred = 1 if pred >= 0.5 else 0
      acc = int(pred == y)
      return acc
  def grad_func(feat_line, y, parameter_vector):
      feat_line = np.array(feat_line)
      pred = sigmoid(np.dot(feat_line, parameter_vector))
      grad = (pred - y) @ feat_line[None, :]
```

```
return grad
   acc his = []
   loss_his = []
   grad_his = []
   prev_param_norm = 0
   for i in tqdm.trange(num_iteration):
       parameter_vector_BC = sc.broadcast(parameter_vector)
       loss = trainRDD.map(lambda x: loss_func(x[1][0], x[1][1],
→parameter_vector_BC.value)).reduce(add) / size
       acc = trainRDD.map(lambda x: accuracy_score(x[1][0], x[1][1],__
→parameter_vector_BC.value)).reduce(add) / size
       grad = trainRDD.map(lambda x: grad_func(x[1][0], x[1][1],
→parameter_vector_BC.value)).reduce(add) / size
       parameter_vector = parameter_vector - learningRate * grad[:, None]
       if np.abs(np.linalg.norm(parameter_vector) - prev_param_norm) < 1e-7:</pre>
           print('Break')
           break
       prev_param_norm = np.linalg.norm(parameter_vector)
       # L2
       parameter_vector = parameter_vector - 2 * lambda_cof * parameter_vector
       acc_his.append(acc)
       loss_his.append(loss)
       grad_his.append(np.linalg.norm(grad))
   end3 = time.time()
   print(f"Computation time of multi-linear regression by BGD is \{(end3 - \Box )\}
⇔start3)/60} minutes")
   fig, ax = plt.subplots(3, figsize=(13, 13))
   ax[0].set_title('Accurary')
   ax[0].plot(acc_his)
   ax[1].set_title('Loss')
   ax[1].plot(loss_his)
   ax[2].set_title('GradNorm')
   ax[2].plot(grad_his)
   plt.savefig("TrainingProcess.png")
   plt.show()
   print('The five words with the largest coefficients',
```

```
np.array(topWordsBC.value)[np.argsort(parameter_vector[:, 0])[-5:]])
   HHHH
  Logistic Regression Model Evaluation
   11 11 11
  print("#### model evaluation ####")
  start4 = time.time()
  t_tuples = total_install.collect()
  key_id = [i for i in range(len(tuples))]
  key_values = {tuples[i][0]: i for i in key_id}
  topWordsBC = sc.broadcast(dictionary.keys().collect())
  feat = cleaned.map(lambda x: (key_values[x[0]], TF(x[1], topWordsBC.value)))
  labels = cleaned.map(lambda x: (key_values[x[0]], int(x[0][0] == 'A' and_\( \)
\rightarrow x[0][1] == 'U')))
  testRDD = feat.join(labels)
   # val
  def TP_func(feat_line, y, parameter_vector):
       feat_line = np.array(feat_line)
       pred = sigmoid(np.dot(feat_line, parameter_vector))
       pred = 1 if pred >= 0.5 else 0
       TP = int(pred == 1 \text{ and } y == 1)
       return TP
  def FP_func(feat_line, y, parameter_vector):
       feat_line = np.array(feat_line)
       pred = sigmoid(np.dot(feat_line, parameter_vector))
       pred = 1 if pred >= 0.5 else 0
       FP = int(pred == 1 and y != 1)
       return FP
  def FN_func(feat_line, y, parameter_vector):
       feat_line = np.array(feat_line)
       pred = sigmoid(np.dot(feat_line, parameter_vector))
       pred = 1 if pred >= 0.5 else 0
       FN = int(pred != 1 and y == 1)
       return FN
```

```
def TN_func(feat_line, y, parameter_vector):
       feat_line = np.array(feat_line)
       pred = sigmoid(np.dot(feat_line, parameter_vector))
       pred = 1 if pred >= 0.5 else 0
       TN = int(pred != 1 and y != 1)
       return TN
   parameter_vector_BC = sc.broadcast(parameter_vector)
   acc = testRDD.map(lambda x: accuracy score(x[1][0], x[1][1],
→parameter_vector_BC.value)).reduce(add) / size
   TP = testRDD.map(lambda x: TP_func(x[1][0], x[1][1], parameter_vector_BC.
→value)).reduce(add)
   FP = testRDD.map(lambda x: FP_func(x[1][0], x[1][1], parameter_vector_BC.
→value)).reduce(add)
   FN = testRDD.map(lambda x: FN_func(x[1][0], x[1][1], parameter_vector_BC.
→value)).reduce(add)
   TN = testRDD.map(lambda x: TN_func(x[1][0], x[1][1], parameter_vector_BC.
→value)).reduce(add)
   F1 = 2 * TP / (2 * TP + FN + FP)
   print('The Acc of Test: ', acc)
   print('The F1 score of Test: ', F1)
   print(f"Computation time of multi-linear regression by BGD is {(end4 - ∪
11 11 11
   SVM Model
   11 11 11
   print("##### SVM model #####")
   start5 = time.time()
   d_corpus = sc.textFile("Google-Playstore.csv")
   d_keyAndText = d_corpus.map(lambda x: (x[x.index('id="') + 4: x.index('"u
\rightarrowurl=')], x[x.index('">') + 2:][:-6]))
   regex = re.compile('[^a-zA-Z]')
   d_keyAndListOfWords = d_keyAndText.map(lambda x: (str(x[0]), regex.sub(' ',_
\rightarrow x[1]).lower().split())).sortByKey(False)
```

```
tuples = d_keyAndListOfWords.collect()
  allWordsList = []
  for i in range(len(tuples)):
       for j in tuples[i][1]:
           allWordsList.append(j)
  allWords = sc.parallelize(allWordsList)
  allCount = allWords.map(lambda x: (x, 1)).reduceByKey(add)
  topWords = allCount.top(20000, lambda x: x[1])
  topWordsK = sc.parallelize(range(20000))
  dictionary = topWordsK.map(lambda x: (topWords[x][0], x))
  def TF(words_list, top_words):
       words_dict = dict(Counter(words_list))
       tf_vector = []
       for word in top_words:
           if word in words_dict.keys():
               tf = words dict[word]
               tf_vector.append(tf)
           else:
               tf_vector.append(0)
       return Vectors.dense(tf vector)
  key_id = [i for i in range(len(tuples))]
  key_values = {tuples[i][0]: i for i in key_id}
  topWordsBC = sc.broadcast(dictionary.keys().collect())
  feat = d keyAndListOfWords.map(lambda x: (key_values[x[0]], TF(x[1],
→topWordsBC.value)))
  labels = d_keyAndListOfWords.map(lambda x: (key_values[x[0]], int(x[0][0]_u
\Rightarrow == 'A' \text{ and } x[0][1] == 'U')))
  train_feat_df = sqlContext.createDataFrame(feat, ['ind', 'features'])
  train_labels_df = sqlContext.createDataFrame(labels, ['ind', 'labels'])
  train_df = train_feat_df.join(train_labels_df, on=['ind']).sort(['ind'])
  train_df.cache()
  svc = LinearSVC(labelCol='labels')
   svg_model = svc.fit(train_df)
  st_test_read = time.time()
  t_corpus = sc.textFile('Google-Playstore_test.csv')
  t_keyAndText = t_corpus.map(lambda x: (x[x.index('id="') + 4: x.index('"u
\rightarrowurl=')], x[x.index('">') + 2:][:-6]))
  regex = re.compile('[^a-zA-Z]')
```

```
t_keyAndListOfWords = t_keyAndText.map(lambda x: (str(x[0]), regex.sub(' ',__
 \rightarrowx[1]).lower().split())).sortByKey(False)
    t_tuples = t_keyAndListOfWords.collect()
    t key id = [i for i in range(len(t tuples))]
    t_key_values = {t_tuples[i][0]: i for i in t_key_id}
    t feat = t keyAndListOfWords.map(lambda x: (t key values[x[0]], TF(x[1],
 →topWordsBC.value)))
    t_labels = t_keyAndListOfWords.map(
        lambda x: (t_{key\_values}[x[0]], int(x[0][0] == 'A' and x[0][1] == 'U')))
    test_feat_df = sqlContext.createDataFrame(t_feat, ['ind', 'features'])
    test_labels_df = sqlContext.createDataFrame(t_labels, ['ind', 'labels'])
    test df = test feat df.join(test labels df, on=['ind']).sort(['ind'])
    test df.cache()
    st_test = time.time()
    test_pred = svg_model.evaluate(test_df).predictions
    evaluator = MulticlassClassificationEvaluator(labelCol='labels')
    print('Acc of Test: ', evaluator.evaluate(test_pred, {evaluator.metricName:
 →"accuracy"}))
    print('F1 of Test:', evaluator.evaluate(test_pred, {evaluator.metricName:__
 →"f1"}))
    end5 = time.time()
    print(f"Computation time of SVM regression by BGD is \{(end5 - start5)/60\}_{\sqcup}
 ⇔minutes")
##### Finding Simple Linear Regression Equation #####
The m (coefficient) = [0.00285053]
The b (y-intercept) = 0.3456192319738405
The equation is: y = 0.0028505272834074033X + 0.3456192319738405
##### Finding the parameters using gradient descent #####
0 Beta [0.1] Cost [1.22465805e+09]
1 Beta [-0.0045326] Cost [12179629.77029447]
2 Beta [0.00420567] Cost [3706927.27275984]
```

3 Beta [0.00347521] Cost [3647720.70333904]
4 Beta [0.00353627] Cost [3647306.97255329]
5 Beta [0.00353116] Cost [3647304.08143576]
6 Beta [0.00353159] Cost [3647304.06123297]
7 Beta [0.00353156] Cost [3647304.06109216]
8 Beta [0.00353156] Cost [3647304.06109071]
9 Beta [0.00353156] Cost [3647304.06109042]
10 Beta [0.00353156] Cost [3647304.06109096]

```
11 Beta [0.00353156]
                       Cost [3647304.06109107]
12 Beta [0.00353156]
                       Cost [3647304.06109113]
13 Beta [0.00353156]
                       Cost [3647304.06109092]
14 Beta [0.00353156]
                       Cost [3647304.06109097]
15 Beta [0.00353156]
                       Cost [3647304.06109096]
16 Beta [0.00353156]
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58 Beta [0.00353156]
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Cost [3647304.06109097]
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                      Cost [3647304.06109097]
62 Beta [0.00353156]
                      Cost [3647304.06109097]
63 Beta [0.00353156]
                      Cost [3647304.06109097]
64 Beta [0.00353156]
                      Cost [3647304.06109097]
65 Beta [0.00353156]
                      Cost [3647304.06109097]
66 Beta [0.00353156]
                      Cost [3647304.06109097]
67 Beta [0.00353156]
                      Cost [3647304.06109097]
68 Beta [0.00353156]
                      Cost [3647304.06109097]
69 Beta [0.00353156]
                      Cost [3647304.06109097]
70 Beta [0.00353156]
                      Cost [3647304.06109097]
71 Beta [0.00353156]
                      Cost [3647304.06109097]
72 Beta [0.00353156]
                       Cost [3647304.06109097]
73 Beta [0.00353156]
                       Cost [3647304.06109097]
74 Beta [0.00353156]
                      Cost [3647304.06109097]
75 Beta [0.00353156]
                      Cost [3647304.06109097]
76 Beta [0.00353156]
                      Cost [3647304.06109097]
77 Beta [0.00353156]
                      Cost [3647304.06109097]
78 Beta [0.00353156]
                      Cost [3647304.06109097]
79 Beta [0.00353156]
                      Cost [3647304.06109097]
80 Beta [0.00353156]
                      Cost [3647304.06109097]
81 Beta [0.00353156]
                      Cost [3647304.06109097]
82 Beta [0.00353156]
                      Cost [3647304.06109097]
83 Beta [0.00353156]
                      Cost [3647304.06109097]
84 Beta [0.00353156]
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85 Beta [0.00353156]
                      Cost [3647304.06109097]
86 Beta [0.00353156]
                      Cost [3647304.06109097]
87 Beta [0.00353156]
                       Cost [3647304.06109097]
88 Beta [0.00353156]
                      Cost [3647304.06109097]
89 Beta [0.00353156]
                      Cost [3647304.06109097]
90 Beta [0.00353156]
                      Cost [3647304.06109097]
91 Beta [0.00353156]
                      Cost [3647304.06109097]
92 Beta [0.00353156]
                      Cost [3647304.06109097]
93 Beta [0.00353156]
                      Cost [3647304.06109097]
94 Beta [0.00353156]
                      Cost [3647304.06109097]
95 Beta [0.00353156]
                      Cost [3647304.06109097]
96 Beta [0.00353156]
                      Cost [3647304.06109097]
97 Beta [0.00353156]
                      Cost [3647304.06109097]
98 Beta [0.00353156]
                      Cost [3647304.06109097]
99 Beta [0.00353156]
                      Cost [3647304.06109097]
Computation time of BGD is 38.446050798892976 Minutes
```

<Figure size 640x480 with 1 Axes>

Finding the parameters of multi-linear regression using gradient descent

0 Beta [0.1 0.1 0.1 0.1] Cost 5.0307575633564e+18

- 1 Beta [1.00000561e-01 -6.52332938e+03 1.00001340e-01 -4.33113272e+07] Cost
- 9.435631463641919e+35
- 2 Beta [1.00001122e-01 4.25538269e+08 1.00002679e-01 1.87587107e+16] Cost
- 1.7700028199286235e+53
- 3 Beta [1.00001683e-01 -2.77592634e+13 1.00004019e-01 -8.12464663e+24] Cost
- 3.3202971042668924e+70
- 4 Beta [1.00002245e-01 1.81082821e+18 1.00005359e-01 3.51889230e+33] Cost
- 6.228449320237621e+87
- 1.1683767963088338e+105
- 6 Beta [1.00003367e-01 7.70576714e+27 1.00008038e-01 6.60098831e+50] Cost
- 2.1917242446163375e+122
- 4.111392129332666e+139
- 8 Beta [1.00004489e-01 3.27909886e+37 1.00010717e-01 1.23826031e+68] Cost
- 7.712441600561638e+156
- 9 Beta [1.00005050e-01 -2.13906423e+42 1.00012057e-01 -5.36306976e+76] Cost
- 1.4467546167076145e+174
- 10 Beta [1.00005611e-01 1.39538207e+47 1.00013396e-01 2.32281670e+85] Cost
- 2.7139251476631882e+191
- 11 Beta [1.00006172e-01 -9.10253702e+51 1.00014736e-01 -1.00604275e+94] Cost
- 5.090973702147291e+208
- 12 Beta [1.00006734e-001 5.93788481e+056 1.00016076e-001 4.35730468e+102] Cost 9.550010345079675e+225
- 13 Beta [1.00007295e-001 -3.87347791e+061 1.00017415e-001 -1.88720650e+111] Cost 1.791458823538236e+243
- 14 Beta [1.00007856e-001 2.52679726e+066 1.00018755e-001 8.17374184e+119] Cost 3.360545800965015e+260
- 15 Beta [1.00008417e-001 -1.64831311e+071 1.00020095e-001 -3.54015609e+128] Cost 6.303950686446002e+277
- 16 Beta [1.00008978e-001 1.07524895e+076 1.00021434e-001 1.53328859e+137] Cost 1.1825398792580455e+295
- 17 Beta [1.00009539e-001 -7.01420317e+080 1.00022774e-001 -6.64087643e+145] Cost inf
- 18 Beta [1.00010100e-001 4.57559584e+085 1.00024113e-001 2.87625173e+154] Cost inf
- 19 Beta [1.00010661e-001 -2.98481192e+090 1.00025453e-001 -1.24574281e+163] Cost inf
- 20 Beta [1.00011222e-001 1.94709116e+095 1.00026793e-001 5.39547745e+171] Cost inf
- 21 Beta [1.00011783e-001 -1.27015172e+100 1.00028132e-001 -2.33685290e+180] Cost inf
- 22 Beta [1.00012345e-001 8.28561815e+104 1.00029472e-001 1.01212201e+189] Cost inf
- 23 Beta [1.00012906e-001 -5.40498172e+109 1.00030812e-001 -4.38363479e+197] Cost inf
- 24 Beta [1.00013467e-001 3.52584766e+114 1.00032151e-001 1.89861041e+206] Cost inf

```
25 Beta [ 1.00014028e-001 -2.30002660e+119 1.00033491e-001 -8.22313373e+214]
Cost inf
26 Beta [1.00014589e-001 1.50038313e+124 1.00034830e-001 3.56154837e+223] Cost
27 Beta [ 1.00015150e-001 -9.78749352e+128 1.00036170e-001 -1.54255388e+232]
Cost inf
28 Beta [1.00015711e-001 6.38470450e+133 1.00037510e-001 6.68100560e+240] Cost
29 Beta [ 1.00016272e-001 -4.16495311e+138 1.00038849e-001 -2.89363221e+249]
Cost inf
30 Beta [1.00016833e-001 2.71693614e+143 1.00040189e-001 1.25327052e+258] Cost
31 Beta [ 1.00017394e-001 -1.77234697e+148 1.00041528e-001 -5.42808098e+266]
Cost inf
32 Beta [1.00017955e-001 1.15616032e+153 1.00042868e-001 2.35097392e+275] Cost
33 Beta [ 1.00018516e-001 -7.54201471e+157 1.00044208e-001 -1.01823801e+284]
Cost inf
34 Beta [1.00019077e-001 4.91990469e+162 1.00045547e-001 4.41012400e+292] Cost
35 Beta [ 1.00019638e-001 -3.20941593e+167 1.00046887e-001
                                                                       -infl
Cost nan
36 Beta [1.00020199e-001 2.09360776e+172 1.00048226e-001
                                                                    nanl Cost
37 Beta [ 1.00020761e-001 -1.36572932e+177 1.00049566e-001
                                                                        nanl
Cost nan
38 Beta [1.00021322e-001 8.90910235e+181 1.00050906e-001
                                                                    nan] Cost
39 Beta [ 1.00021883e-001 -5.81170100e+186 1.00052245e-001
                                                                        nan]
Cost nan
40 Beta [1.00022444e-001 3.79116405e+191 1.00053585e-001
                                                                    nan] Cost
41 Beta [ 1.00023005e-001 -2.47310122e+196 1.00054924e-001
                                                                        nan]
Cost nan
42 Beta [1.00023566e-001 1.61328541e+201 1.00056264e-001
                                                                    nan] Cost
43 Beta [ 1.00024127e-001 -1.05239923e+206 1.00057603e-001
                                                                        nan]
44 Beta [1.00024688e-001 6.86514692e+210 1.00058943e-001
                                                                    nan] Cost
45 Beta [ 1.00025249e-001 -4.47836153e+215 1.00060283e-001
                                                                        nan]
Cost nan
                                                                    nan] Cost
46 Beta [1.00025810e-001 2.92138278e+220 1.00061622e-001
47 Beta [ 1.00026371e-001 -1.90571424e+225 1.00062962e-001
                                                                        nan]
48 Beta [1.00026932e-001 1.24316019e+230 1.00064301e-001
                                                                    nan] Cost
```

nan

```
49 Beta [ 1.00027493e-001 -8.10954352e+234 1.00065641e-001
                                                                         nan]
Cost nan
50 Beta [1.00028054e-001 5.29012243e+239 1.00066980e-001
                                                                     nan] Cost
51 Beta [ 1.00028615e-001 -3.45092116e+244 1.00068320e-001
                                                                         nan]
Cost nan
52 Beta [1.00029176e-001 2.25114958e+249 1.00069659e-001
                                                                     nan] Cost
53 Beta [ 1.00029737e-001 -1.46849904e+254 1.00070999e-001
                                                                         nan]
Cost nan
54 Beta [1.00030298e-001 9.57950309e+258 1.00072339e-001
                                                                     nan] Cost
55 Beta [ 1.00030859e-001 -6.24902549e+263 1.00073678e-001
                                                                         nan]
Cost nan
56 Beta [1.00031420e-001 4.07644522e+268 1.00075018e-001
                                                                     nan] Cost
57 Beta [ 1.00031981e-001 -2.65919953e+273 1.00076357e-001
                                                                         nan]
Cost nan
58 Beta [1.00032542e-001 1.73468347e+278 1.00077697e-001
                                                                     nan] Cost
59 Beta [ 1.00033103e-001 -1.13159118e+283 1.00079036e-001
                                                                         nan]
Cost nan
60 Beta [1.00033664e-001 7.38174212e+287 1.00080376e-001
                                                                     nanl Cost
61 Beta [ 1.00034225e-001 -4.81535360e+292 1.00081715e-001
                                                                         nan]
Cost nan
62 Beta [0.10003479
                           inf 0.10008305
                                                 nan] Cost nan
63 Beta [0.10003535
                           nan 0.10008439
                                                 nan] Cost nan
64 Beta [0.10003591
                           nan 0.10008573
                                                 nan] Cost nan
65 Beta [0.10003647
                           nan 0.10008707
                                                 nan] Cost nan
66 Beta [0.10003703
                           nan 0.10008841
                                                 nan] Cost nan
67 Beta [0.10003759
                           nan 0.10008975
                                                 nan] Cost nan
68 Beta [0.10003815
                           nan 0.10009109
                                                 nan] Cost nan
69 Beta [0.10003871
                           nan 0.10009243
                                                 nan] Cost nan
70 Beta [0.10003927
                           nan 0.10009377
                                                 nan] Cost nan
71 Beta [0.10003983
                           nan 0.10009511
                                                 nan] Cost nan
72 Beta [0.1000404
                           nan 0.10009645
                                                 nan] Cost nan
73 Beta [0.10004096
                           nan 0.10009779
                                                 nanl Cost nan
74 Beta [0.10004152
                           nan 0.10009913
                                                 nan] Cost nan
                           nan 0.10010047
75 Beta [0.10004208
                                                 nan] Cost nan
76 Beta [0.10004264
                                                 nan] Cost nan
                           nan 0.10010181
77 Beta [0.1000432
                           nan 0.10010315
                                                 nan] Cost nan
78 Beta [0.10004376
                           nan 0.10010449
                                                 nan]
                                                       Cost nan
79 Beta [0.10004432
                           nan 0.10010583
                                                 nan] Cost nan
80 Beta [0.10004488
                           nan 0.10010717
                                                 nan] Cost nan
81 Beta [0.10004544
                           nan 0.10010851
                                                 nan] Cost nan
82 Beta [0.10004601
                           nan 0.10010985
                                                 nan] Cost nan
83 Beta [0.10004657
                           nan 0.10011118
                                                 nan] Cost nan
```

```
84 Beta [0.10004713
                           nan 0.10011252
                                                 nan] Cost nan
85 Beta [0.10004769
                           nan 0.10011386
                                                 nan] Cost nan
86 Beta [0.10004825
                           nan 0.1001152
                                                 nan] Cost nan
87 Beta [0.10004881
                           nan 0.10011654
                                                 nan] Cost nan
88 Beta [0.10004937
                           nan 0.10011788
                                                 nanl Cost nan
89 Beta [0.10004993
                           nan 0.10011922
                                                 nan] Cost nan
90 Beta [0.10005049
                           nan 0.10012056
                                                 nan] Cost nan
91 Beta [0.10005105
                           nan 0.1001219
                                                 nanl Cost nan
92 Beta [0.10005161
                           nan 0.10012324
                                                 nan] Cost nan
93 Beta [0.10005218
                           nan 0.10012458
                                                 nan] Cost nan
94 Beta [0.10005274
                           nan 0.10012592
                                                 nan] Cost nan
95 Beta [0.1000533
                           nan 0.10012726
                                                 nan] Cost nan
96 Beta [0.10005386
                           nan 0.1001286
                                                 nan] Cost nan
97 Beta [0.10005442
                           nan 0.10012994
                                                 nan] Cost nan
98 Beta [0.10005498
                           nan 0.10013128
                                                 nan]
                                                       Cost nan
99 Beta [0.10005554
                           nan 0.10013262
                                                 nan] Cost nan
```

Computation time of multi-linear regression by BGD is 24.002660648028055 minutes

<Figure size 640x480 with 1 Axes>

Logistic regression model

Acc of Test: 0.9975432599871822 F1 of Test: 0.9974863907576629

Computation time of logistic regression is 28.70752596855166 minutes

SVM model

Acc of Test: 0.982736100123734 F1 of Test: 0.980016837261283

Computation time of logistic regression is 29.631058894040428 minutes

[]: