Example

This document provide some examples of using the functions in mixedSCORE.R for clustering analysis. See J. Jin, Ke, and Luo (2017) for the details of the method.

First source the code

```
source('mixedSCORE.R')
```

The main function is mixedSCORE

Input parameters:

- A: n-by-n adjacency matrix of the network
- K: number of clusters
- verbose: (optional) boolean, whether to generate messages, by default is False.

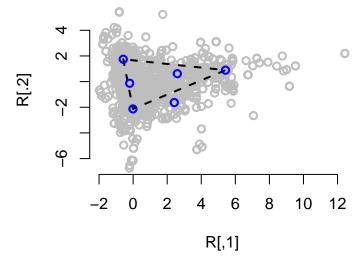
Outputs: a list containing

- R: n-by-(k-1) ratio matrix
- L: selected L by the vertex hunting algorithm
- \bullet centers: L cluster centers
- vertices: K vertices selected from L centers
- memberships: n-by-K matrix, the memberships of the n nodes
- degrees: a vector of length n, estimated degrees of each node
- puritys: a vector of length n, estimated purity (the maximum of memberships on K clusters) of each node
- major.labels: the hard clustering labels

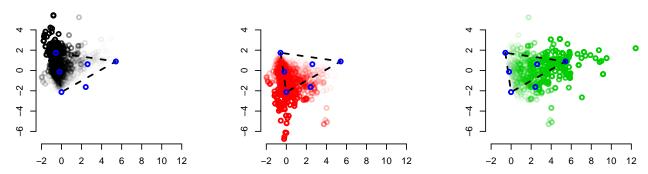
lty = 2, lwd = 2, col = 'black')
points(ms.out\$centers, lwd = 2, col = 'blue')

Here we use the citee network data from Ji and Jin (2016) as an example, which is included as citee.RData in the repository. The citee network has 1790 nodes, where each node represents an author, and two nodes are connected if the two authors were once cited together.

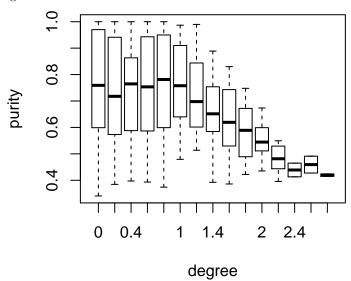
```
load('citee.RData')
dim(citee)
## [1] 1790 1790
ms.out = mixedSCORE(citee, K = 3)
names(ms.out)
## [1] "R"
                                       "vertices"
                                                       "centers"
## [5] "memberships" "degrees"
                                       "puritys"
                                                       "major.labels"
ms.out$L
## [1] 6
Plot the L vertices and the selected K cluster centers on top of the first two ratios
plot(ms.out$R, col='grey', lwd = 2, xlab = 'R[,1]', ylab = 'R[.2]',bty="n")
lines(ms.out$vertices[c(1,2,3,1),1], ms.out$vertices[c(1,2,3,1),2],
```



The membership for each of three clusters



Plot the purity versus degree of nodes



Reference

Ji, P. S., and J. S. Jin. 2016. "Coauthorship and Citation Networks for Statisticians." Journal Article. *Annals of Applied Statistics* 10 (4): 1779–1812. doi:10.1214/15-Aoas896.

Jin, Jiashun, Zheng Tracy Ke, and Shengming Luo. 2017. "Estimating Network Memberships by Simplex Vertex Hunting." $arXiv\ Preprint\ arXiv:1708.07852$.