

0.1 Examples of fossil record simulations

0.1.1 From Silvestro et al. [2014]

Simulated data sets were generated based on six patterns of species diversification chosen to yield scenarios of varying species richness commonly observed in empirical data (Fig. 2 and Table 1; Sepkoski 1981):

- I. expanding diversity with constant speciation and extinction rates ($\lambda > \mu$);
- II. expanding diversity followed by a decline with all taxa going extinct before the present ($\lambda_1 > \mu_1, \lambda_2 < \mu_2$);
- III. expanding and then declining diversity followed by turnover at equilibrium ($\lambda_1 > \mu_1, \lambda_2 < \mu_2, \lambda_3 = \mu_3$);
- IV. expanding diversity followed by turnover at equilibrium due to a decrease in speciation rate ($\lambda_1 > \mu_1, \lambda_2 = \mu_2$);
- V. expanding diversity followed by turnover at equilibrium due to a decrease in speciation rate and increase in extinction rate ($\lambda_1 > \mu_1, \lambda_2 = \mu_2$); and
- VI. constant speciation rate and a mass extinction event ($\lambda_1 > \mu_1, \lambda_2 \ll \mu_2, \lambda_1 > \mu_1$).

Based on the complete birth–death realizations, fossil occurrences were simulated for each species. Along each lineage i a number of occurrences K_i was derived from a Poisson distribution with rate parameter $qPOI = q(s_i - e_i)$ where q is the preservation rate (cf. Equation 1), and s_i, e_i are the true times of speciation and extinction. The preservation rate was assumed $q = 3$ unless stated otherwise. A number of fossils K_i were then randomly drawn from the PERT distribution for all species, resulting in a synthetic data set that mimics the fossil record. The shape parameter of the PERT distribution was assumed to be $l = 4$ (as in Equation 3) unless stated otherwise. The number of occurrences K depended only on the preservation rate q and on the species lifespan, i.e., it was not conditioned on being greater than 0. The lineages without a fossil record ($K = 0$) were disregarded in the analyses because of the condition stated in Equation (4). All extant species were then truncated at time 0 (i.e., the present). The number of extant species based on the complete birth–death realization (NOBS) was kept to construct the hyperprior of Equations (12–15).

0.1.2 From Foote [2000]

Preservation can be modeled in a number of realistic ways that include variation in time and space (Shaw 1964; Koch and Morgan 1988; Marshall 1994; Holland 1995; Holland and Patzkowsky 1999; Weiss and Marshall 1999). As a heuristic tool for understanding the behavior of diversity and rate measures, it is convenient to focus on the temporal aspect and to start by assuming time-homogeneous fossil preservation at a constant per-capita rate r per Lmy (Paul 1982, 1988; Pease 1985; Strauss and Sadler 1989; Marshall 1990; Foote and Raup 1996; Solow and Smith 1997; Foote 1997). This simple assumption will be relaxed below. In the time-homogeneous case, the proportion of lineages preserved is equal to $r/(q + r)$ if $p \gg q$ and if the fossil record is of effectively infinite length (Pease 1985; Solow and Smith 1997) (see Edge Effects, below). It is therefore natural for many problems to express preservation rate as a multiple of q . Throughout this discussion I will assume taxonomic homogeneity of taxonomic and preservational rates. For modeling, this assumption can

easily be relaxed by performing calculations for an arbitrary number of rate classes and combining the results (see Buzas et al. 1982, Koch and Morgan 1988, Holland 1995, Holland and Patzkowsky 1999, and Weiss and Marshall 1999 for explicit treatments of taxonomic heterogeneity of preservation)

0.2 Other studies comparing methods in the FR

See:

- Alroy [2000]
- Alroy [2010]
- Alroy [2014]

Bibliography

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