

Name: Solutions

The following implementation of Newton's method contains two errors. Find the errors and explain what you could do to fix them.

```
1 function [x,xerr,ferr,k] = newton(f,fp,x0,xtol,ftol,kmax)
2 % [x,xerr,ferr,k] = NEWTON(f,fp,x0,xtol,ftol,kmax) approximates
   the root
3 % of a function using Newton-Raphson iteration
4 %
5 % inputs
6 % -----
7 % f: function handle for objective function
8 % fp: function handle for the derivative of f
9 % x0: initial approximation for the root of f
10 % xtol: tolerance for location of the root
11 % ftol: tolerance for function values of the root
12 % kmax: maximum number of iterations
13 %
14 % outputs
15 % -----
16 % x: approximate root of objective function
17 % xerr: error estimate for the root
18 % ferr: value of f at the approximate root
19 % k: number of iterations required
20 %
21 % examples
22 % -----
23 % x = newton(@(x) x.^3-1, @(x) 3*x.^2, 2, 1e-6, 0, 10)
24
25 x = x0;
26 fx = f(x);
27
28 for k = 1:kmax
29     x = x+fx/fp(x);
30     xerr = x-x0;
31     fx = f(x);
32     ferr = abs(fx);
33     x0 = x;
34     if (xerr < xtol) || (ferr < ftol)
35         break
36     end
37 end
38
39 end
```

Newton's iteration is $x = x - fx/fp(x)$.

Error is $abs(x-x0)$.