

# Standard Code Library

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# 1 Algorithms and Datastructures

## 1.1 High Precision (Integer)

*//need iostream, string, algorithm*

```
class HP
{
public:
    static const int MAXL = 10000;
    int len, s[MAXL];
    HP() { (*this) = 0; };
    HP(int inte) { (*this) = inte; };
    HP(const char* str) { (*this) = str; };
    HP(string str) { (*this) = str; };
    friend ostream& operator << (ostream &cout, const HP &x);
    HP operator = (int inte);
    HP operator = (const char* str); HP operator = (string str);
    HP operator + (const HP &b); HP operator += (const HP &b);
    HP operator - (const HP &b); HP operator -= (const HP &b);
    HP operator * (const HP &b); HP operator *= (const HP &b);
    HP operator / (const HP &b); HP operator /= (const HP &b);
    HP operator % (const HP &b); HP operator %= (const HP &b);
    int comp(const HP &b);
    bool operator > (const HP &b); bool operator < (const HP &b);
    bool operator >= (const HP &b); bool operator <= (const HP &b);
    bool operator == (const HP &b); bool operator != (const HP &b);
};

ostream& operator << (ostream &cout, const HP &x)
{
    for (int i = x.len - 1; i >= 0; --i) cout << x.s[i];
    return cout;
}

HP HP::operator = (int inte)
{
    if (inte == 0)
    {
        len = 1;
        s[0] = 0;
    }
    else
    {
        len = 0;
        while (inte)
        {
            s[len++] = inte % 10;
            inte /= 10;
        }
    }
    return (*this);
}

HP HP::operator = (const char* str)
```

```
{
    len = strlen(str);
    for (int i = 0; i != len; ++i) s[i] = int(str[len - 1 - i] - '0');
    return (*this);
}

HP HP::operator = (string str)
{
    len = str.size();
    for (int i = 0; i != len; ++i) s[i] = int(str[len - 1 - i] - '0');
    return (*this);
}

HP HP::operator + (const HP &b)
{
    HP c;
    c.s[0] = 0;
    for (int i = 0; i < len || i < b.len; ++i)
    {
        if (i < len) c.s[i] += s[i];
        if (i < b.len) c.s[i] += b.s[i];
        c.s[i + 1] = c.s[i] / 10;
        c.s[i] %= 10;
    }
    c.len = max(len, b.len) + 1;
    while (c.len > 1 && !c.s[c.len - 1]) --c.len;
    return c;
}

HP HP::operator - (const HP &b)
{
    HP c = (*this);
    for (int i = 0; i != b.len; ++i)
    {
        c.s[i] -= b.s[i];
        if (c.s[i] < 0)
        {
            c.s[i] += 10;
            --c.s[i + 1];
        }
    }
    while (c.len > 1 && !c.s[c.len - 1]) --c.len;
    return c;
}

HP HP::operator * (const HP &b)
{
    HP c;
    for (int i = 0; i != len + b.len; ++i) c.s[i] = 0;
    for (int i = 0; i != len; ++i)
        for (int j = 0; j != b.len; ++j)
        {
            c.s[i + j] += s[i] * b.s[j];
            c.s[i + j + 1] += c.s[i + j] / 10;
            c.s[i + j] %= 10;
        }
    c.len = len + b.len;
}
```

```

    while (c.len > 1 && !c.s[c.len - 1]) --c.len;
    return c;
}

```

```

HP HP::operator / (const HP &b)
{
    HP c, d;
    if (b.len == 1 && b.s[0] == 0) return c;
    for (int i = len - 1; i >= 0; --i)
    {
        if (d.len != 1 || d.s[0] != 0)
        {
            for (int j = d.len; j > 0; --j)
                d.s[j] = d.s[j - 1];
            ++d.len;
        }
        d.s[0] = s[i];
        c.s[i] = 0;
        while (d >= b)
        {
            d -= b;
            ++c.s[i];
        }
    }
    c.len = len;
    while (c.len > 1 && !c.s[c.len - 1]) --c.len;
    return c;
}

```

```

HP HP::operator % (const HP &b)
{
    HP d;
    if (b.len == 1 && b.s[0] == 0) return d;
    for (int i = len - 1; i >= 0; --i)
    {
        if (d.len != 1 || d.s[0] != 0)
        {
            for (int j = d.len; j > 0; --j)
                d.s[j] = d.s[j - 1];
            ++d.len;
        }
        d.s[0] = s[i];
        while (d >= b) d -= b;
    }
    return d;
}

```

```

int HP::comp(const HP &b)
{
    if (len > b.len) return 1;
    if (len < b.len) return -1;
    int i = len - 1;
    while ((i > 0) && (s[i] == b.s[i])) --i;
    return s[i] - b.s[i];
}

```

```

HP HP::operator += (const HP &b)

```

```
{
    (*this) = (*this) + b;
    return (*this);
}

HP HP::operator -= (const HP &b)
{
    (*this) = (*this) - b;
    return (*this);
}

HP HP::operator *= (const HP &b)
{
    (*this) = (*this) * b;
    return (*this);
}

HP HP::operator /= (const HP &b)
{
    (*this) = (*this) / b;
    return (*this);
}

HP HP::operator %= (const HP &b)
{
    (*this) = (*this) % b;
    return (*this);
}

bool HP::operator > (const HP &b) { return this->comp(b) > 0; }
bool HP::operator < (const HP &b) { return this->comp(b) < 0; }
bool HP::operator >= (const HP &b) { return this->comp(b) >= 0; }
bool HP::operator <= (const HP &b) { return this->comp(b) <= 0; }
bool HP::operator == (const HP &b) { return this->comp(b) == 0; }
bool HP::operator != (const HP &b) { return this->comp(b) != 0; }
```

## 1.2 High Precision (Floating-point Number)

### 1.3 Fraction

### 1.4 Binary Heap

```
//need algorithm
//small on top

const int MAXN = 1048576;
int heapsize, heap[MAXN + 1];

void move_up(int x)
```

```
{
    while (x != 1)
    {
        if (heap[x / 2] > heap[x])
        {
            swap(heap[x], heap[x / 2]);
            x /= 2;
        }
        else
            break;
    }
}

void move_down(int x)
{
    int y = x * 2;
    while (y <= heapsize)
    {
        if (y < heapsize && heap[y + 1] < heap[y]) ++y;
        if (heap[y] < heap[x])
            swap(heap[x], heap[y]);
        else
            break;
        x = y; y = x * 2;
    }
}

int get_top() { return heap[1]; }

int remove_top()
{
    heap[1] = heap[heapsize--];
    move_down(1);
}

void add_heap(int x)
{
    heap[++heapsize] = x;
    move_up(heapsize);
}

void build_heap()
{
    for (int i = heapsize; i > 0; --i) move_down(i);
}
```

## 1.5 Winner Tree

## 1.6 Digital Tree

## 1.7 Segment Tree

## 1.8 Union-Find Set



## **1.9 Quick Sort**

## **1.10 Merge Sort**

## **1.11 Radix Sort**

## **1.12 Select Kth Smallest Element**

## **1.13 KMP**

## **1.14 Suffix Sort**

## 2 Graph Theory and Network Algorithms

### 2.1 Adjacency List

```
const int MAXNV = 10000, MAXNE = 100000;
int nv, ne, tot;
int head[MAXNV], next[MAXNE], adj[MAXNE];
int value[MAXNE];

void init()
{
    tot = 0;
    for (int i = 0; i != nv; ++i) head[i] = -1;
}

void add_edge(int x, int y, int z)
{
    next[tot] = head[x];
    adj[tot] = y;
    value[tot] = z;
    head[x] = tot;
    ++tot;
}
```

### 2.2 SSSP (Dijkstra + Binary Heap)

*//need Adjacency List, alorithm*

```
const int INF = 1000000000;
int heapsize;
int dist[MAXNV], heap[MAXNV], ref[MAXNV];
bool v[MAXNV];

void update(int x)
{
    while (x > 1 && dist[heap[x]] < dist[heap[x >> 1]])
    {
        swap(ref[heap[x]], ref[heap[x >> 1]]);
        swap(heap[x], heap[x >> 1]);
        x = x >> 1;
    }
}

int getmin()
{
    int x = 1, y = 2;
    swap(ref[heap[heapsize]], ref[heap[1]]);
    swap(heap[heapsize], heap[1]);
    --heapsize;
    while (y <= heapsize)
    {
        if (y < heapsize && dist[heap[y + 1]] < dist[heap[y]]) ++y;
        if (dist[heap[y]] < dist[heap[x]])
        {

```

```

        swap(ref[heap[x]], ref[heap[y]]);
        swap(heap[x], heap[y]);
    }
    else
        break;
    x = y; y = x << 1;
}
return heap[heapsize + 1];
}

int Dijkstra(int x, int y)
{
    int z, temp;
    memset(ref, 0xff, sizeof(ref));
    for (int i = 0; i != nv; ++i) dist[i] = INF;
    dist[x] = 0;
    heapsize = 1;
    heap[heapsize] = x; ref[x] = heapsize;
    memset(v, false, sizeof(v));
    while (!v[y])
    {
        for (int i = 0; i != nv; ++i) cout << dist[i] << " "; cout << endl;
        if (!heapsize) break;
        z = getmin(); v[z] = true;
        cout << z << endl;
        for (int i = 1; i <= heapsize; ++i) cout << heap[i] << " "; cout << endl;
        temp = head[z];
        while (temp != -1)
        {
            if (!v[adj[temp]] && dist[z] + value[temp] < dist[adj[temp]])
            {
                if (ref[adj[temp]] == -1)
                {
                    heap[++heapsize] = adj[temp];
                    ref[adj[temp]] = heapsize;
                }
                dist[adj[temp]] = dist[z] + value[temp];
                update(ref[adj[temp]]);
                for (int i = 1; i <= heapsize; ++i) cout << heap[i] << " "; cout <<
endl;
            }
            temp = next[temp];
        }
    }
    return dist[y];
}

```

## 2.3 SSSP (SPFA)

*//need Adjacency List*

```

const int INF = 1000000000;
int qs, ql, temp;
int q[MAXNV], dist[MAXNV], vtime[MAXNV];
bool v[MAXNV];

```

```

int SPFA(int x, int y)
{
    qs = 0;
    ql = 1;
    q[qs] = x;
    memset(v, false, sizeof(v));
    v[q[qs]] = true;
    for (int i = 0; i != nv; ++i) dist[i] = INF;
    dist[q[qs]] = 0;
    memset(vtime, 0, sizeof(vtime));
    vtime[q[qs]] = 1;
    while (ql)
    {
        temp = head[q[qs]];
        while (temp != -1)
        {
            if (dist[q[qs]] + value[temp] < dist[adj[temp]])
            {
                dist[adj[temp]] = dist[q[qs]] + value[temp];
                if (!v[adj[temp]])
                {
                    v[adj[temp]] = true;
                    ++ql;
                    q[(qs + ql - 1) % nv] = adj[temp];
                    ++vtime[adj[temp]];
                    if (vtime[adj[temp]] > nv) return -1;
                }
            }
            temp = next[temp];
        }
        v[q[qs]] = false;
        qs = (qs + 1) % nv;
        --ql;
    }
    return dist[y];
}

```

## 2.4 MST (Kruskal)

## 2.5 Minimum Directed Spanning Tree

## 2.6 Maximum Matching on Bipartite Graph

## 2.7 Maximum Cost Perfect Matching on Bipartite Graph ( $n^4$ )

## 2.8 Maximum Cost Perfect Matching on Bipartite Graph ( $n^3$ )

## 2.9 Maximum Matching on General Graph

**2.10 Maximum Flow (Dinic in Matrix)**

**2.11 Maximum Flow (Dinic in Link)**

**2.12 Minimum Cost Maximim Flow (in Matrix)**

**2.13 Minimum Cost Maximim Flow (in Link)**

**2.14 Bridge (DFS)**

**2.15 Cutvertex (DFS)**

**2.16 Block (DFS)**

**2.17 Topological Sort (DFS)**

**2.18 Strongly Connected Component (DFS)**

**2.19 Disjoint Set**

## **3 Number Theory**

### **3.1 Greatest Common Diviser**

### **3.2 China Remainder Theorem**

### **3.3 Prime Generator**

### **3.4 Phi generator (Eular Function)**

### **3.5 Discrete Logarithm**

### **3.6 Square Roots in $\mathbb{Z}_p$**

## **4 Algebraic Algorithms**

### **4.1 Linear Equations in $Z_2$**

### **4.2 Linear Equations in $Z$**

### **4.3 Linear Equations in $Q$**

### **4.4 Linear Equations in $R$**

### **4.5 Roots of Polynomial**

### **4.6 Roots of Cubic and Quartic**

### **4.7 Fast Fourier Transform**

### **4.8 FFT - Polynomial Multiplication**

### **4.9 FFT - Convolution**

### **4.10 FFT - Reverse Bits**

### **4.11 Linear Programming - Primal Simplex**

## **5 Computational Geometry**

### **5.1 Basic Operations**

### **5.2 Extended Operations**

### **5.3 Convex Hull**

### **5.4 Point Set Diameter**

### **5.5 Closest Pair**

### **5.6 Circles**

### **5.7 Largest Empty Convex Polygon**

### **5.8 Triangle Centers**

### **5.9 Polyhedron Volume**

### **5.10 Planar Graph Contour**

### **5.11 Rectangles Area**

### **5.12 Rectangles Perimeter**

### **5.13 Smallest Enclosing Circle**

### **5.14 Smallest Enclosing Ball**