Big Data Analytics

Recommendation Systems

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Mining of Massive Datasets by Jure Leskovec et. al Stanford University http://www.mmds.org

Outline

- Introduction
- Context-based Systems
- Collaborative Filtering
- Latent Factor Models
- The Netflix Challenge: 2006-09
- Summary

High Dimensional Data

High dim. data

Locality sensitive hashing

Clustering

Dimensional ity reduction

Graph data

Community

Detection

Spam

Detection

Infinite data

Machine learning

Apps

Filtering

streams

Web advertising

Queries on streams

Decision Trees

Perceptron, kNN Recommen der systems

Association Rules

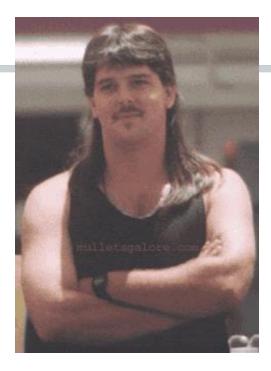
Duplicate document detection

J. Leskovec, A. Rajaraman, J. Ullman: Mining of

Massive Datascis, http://www.mmis.org

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Example: Recommender Systems

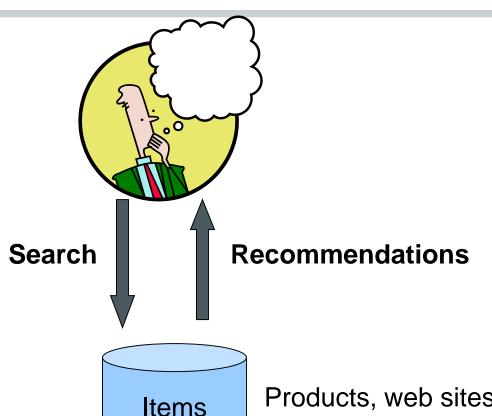


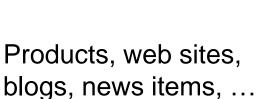
- Customer X
 - Buys Metallica CD
 - Buys Megadeth CD



- Customer Y
 - Does search on Metallica
 - Recommender system suggests
 Megadeth from data collected about customer X

Recommendations











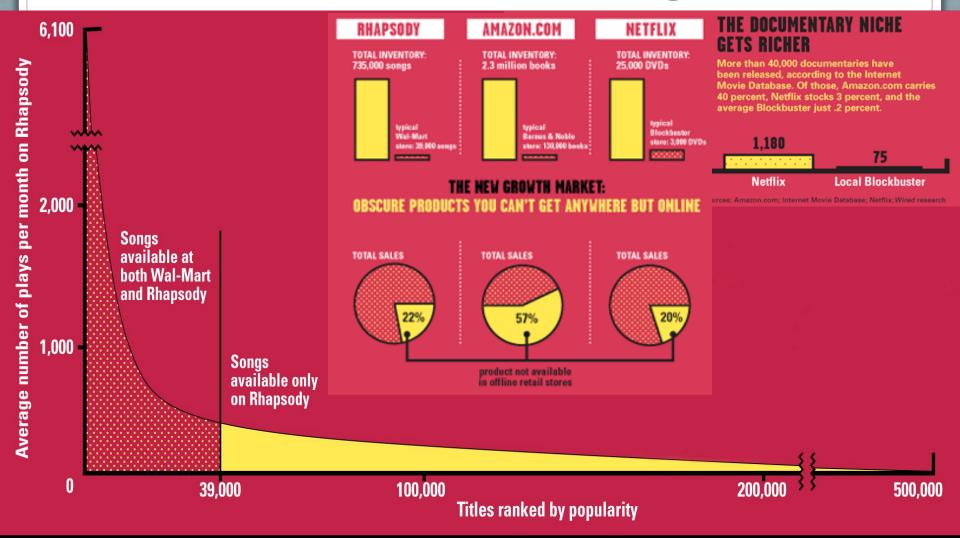




From Scarcity to Abundance

- Shelf space is a scarce commodity for traditional retailers
 - Also: TV networks, movie theaters,...
- Web enables near-zero-cost dissemination of information about products
 - From scarcity to abundance
- More choice necessitates better filters
 - Recommendation engines
 - How Into Thin Air made Touching the Void a bestseller: http://www.wired.com/wired/archive/12.10/tail.html

Sidenote: The Long Tail

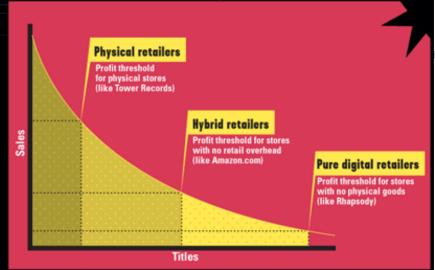


Physical vs. Online

THE BIT PLAYER ADVANTAGE

Beyond bricks and mortar there are two main retail models – one that gets halfway down the Long Tail and another that goes all the way. The first is the familiar hybrid model of Amazon and Netflix, companies that sell physical goods online. Digital catalogs allow them to offer unlimited selection along with search, reviews, and recommendations, while the cost savings of massive warehouses and no walk-in customers greatly expands the number of products they can sell profitably.

Pushing this even further are pure digital services, such as iTunes, which offer the additional savings of delivering their digital goods online at virtually no marginal cost. Since an extra database entry and a few megabytes of storage on a server cost effectively nothing, these retailers have no economic reason not to carry everything available.





Read http://www.wired.com/wired/archive/12.10/tail.html to learn more!

Types of Recommendations

- Editorial and hand curated
 - List of favorites
 - Lists of "essential" items
- Simple aggregates
 - Top 10, Most Popular, Recent Uploads
- Tailored to individual users
 - Amazon, Netflix, ...

Formal Model

- X = set of Customers
- S = set of Items
- Utility function $u: X \times S \rightarrow R$
 - R = set of ratings
 - R is a totally ordered set
 - e.g., 0-5 stars, real number in [0,1]

Utility Matrix

LOTR Avatar **Matrix Pirates** 0.2 Alice Bob 0.5 0.3 0.2 **Carol David**

Key Problems

- (1) Gathering "known" ratings for matrix
 - How to collect the data in the utility matrix
- (2) Extrapolate unknown ratings from the known ones
 - Mainly interested in high unknown ratings
 - We are not interested in knowing what you don't like but what you like
- (3) Evaluating extrapolation methods
 - How to measure success/performance of recommendation methods

(1) Gathering Ratings

Explicit

- Ask people to rate items
- Doesn't work well in practice people can't be bothered

• Implicit

- Learn ratings from user actions
 - E.g., purchase implies high rating
- What about low ratings?

(2) Extrapolating Utilities

- Key problem: Utility matrix U is sparse
 - Most people have not rated most items
 - Cold start:
 - New items have no ratings
 - New users have no history
- Three approaches to recommender systems:
 - 1) Content-based
 - 2) Collaborative
 - 3) Latent factor based

Today!

Content-based Recommender Systems

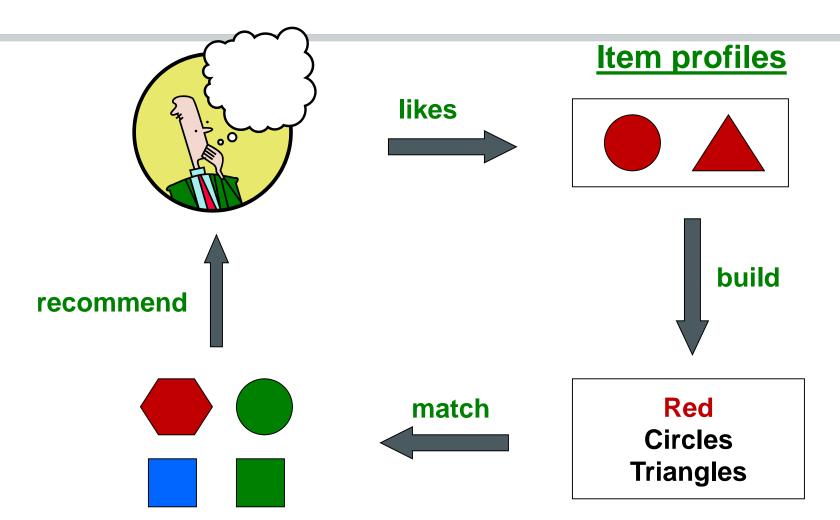
Content-based Recommendations

• Main idea: Recommend items to customer x similar to previous items rated highly by x

Example:

- Movie recommendations
 - Recommend movies with same actor(s), director, genre, ...
- Websites, blogs, news
 - Recommend other sites with "similar" content

Plan of Action



User profile

Item Profiles

- For each item, create an item profile
- Profile is a set (vector) of features
 - Movies: author, title, actor, director,...
 - Text: Set of "important" words in document
- How to pick important features?
 - Usual heuristic from text mining is TF-IDF (Term frequency * Inverse Doc Frequency)
 - Term ... Feature
 - Document ... Item

Sidenote: TF-IDF

$$TF_{ij} = rac{f_{ij}}{\max_k f_{kj}}$$
doc (item) j

Note: we normalize TF to discount for "longer" documents

 n_i = number of docs that mention term i

$$IDF_i = \log \frac{N}{n_i}$$

TF-IDF score: $w_{ij} = TF_{ij} \times IDF_i$

Doc profile = set of words with highest TF-IDF scores, together with their scores

User Profiles and Prediction

• User profile possibilities:

- Weighted average of rated item profiles
- Variation: weight by difference from average rating for item

•

• Prediction heuristic:

• Given user profile x and item profile i, estimate $u(x, i) = \cos(x, i) = \frac{x \cdot i}{||x|| \cdot ||i||}$

Pros: Content-based Approach

- +: No need for data on other users
 - No cold-start or sparsity problems
- +: Able to recommend to users with unique tastes
- +: Able to recommend new & unpopular items
 - No first-rater problem
- +: Able to provide explanations
 - Can provide explanations of recommended items by listing content-features that caused an item to be recommended

Cons: Content-based Approach

- -: Finding the appropriate features is hard
 - E.g., images, movies, music
- -: Recommendations for new users
 - How to build a user profile?
- -: Overspecialization
 - Never recommends items outside user's content profile
 - People might have multiple interests
 - Unable to exploit quality judgments of other users

Collaborative Filtering

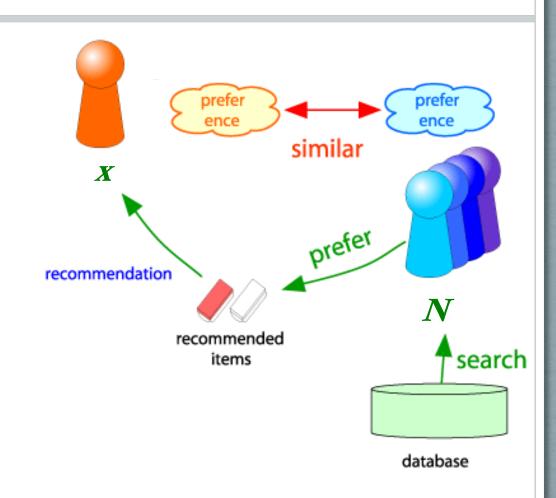
Harnessing quality judgments of other users

Collaborative Filtering

• Consider user x

• Find set Nof other users whose ratings are "similar" to x's ratings

• Estimate x's ratings based on ratings of users in N



Finding "Similar" Users

$$r_x = [*, _, _, *, ***]$$
Let r_x be the vector of user x 's ratings
$$r_y = [*, _, **, ***, _]$$

- Jaccard similarity measure
 - Problem: Ignores the value of the rating
- Cosine similarity measure
 - $sim(x, y) = cos(r_x, r_y) = \frac{r_x \cdot r_y}{||r_x|| \cdot ||r_y||}$
 - Problem: Treats missing ratings as "negative"
- Pearson correlation coefficient
 - S_{xy} = items rated by both users x and y

$$r_y = \{1, 3, 4\}$$

 r_x , r_y as sets:

 $r_{\rm x} = \{1, 4, 5\}$

$$r_x$$
, r_y as points:
 $r_x = \{1, 0, 0, 1, 3\}$
 $r_y = \{1, 0, 2, 2, 0\}$

$$\overline{\mathbf{r}}_{\mathbf{x}}, \overline{\mathbf{r}}_{\mathbf{y}} \dots$$
 avg. rating of \mathbf{x}, \mathbf{y}

$$sim(x,y) = \frac{\sum_{s \in S_{xy}} (r_{xs} - \overline{r_x}) (r_{ys} - \overline{r_y})}{\sqrt{\sum_{s \in S_{xy}} (r_{xs} - \overline{r_x})^2} \sqrt{\sum_{s \in S_{xy}} (r_{ys} - \overline{r_y})^2}}}$$

Similarity Metric

| | HP1 | HP2 | HP3 | TW | SW1 | SW2 | SW3 | |
|----------------|-----|-----|-----|----|-----|-----|-----|--|
| \overline{A} | 4 | | | 5 | 1 | | | |
| B | 5 | 5 | 4 | | | | | |
| C | | | | 2 | 4 | 5 | | |
| D | | 3 | | | | | 3 | |

- Intuitively we want: sim(A, B) > sim(A, C)
- Jaccard similarity: 1/5 < 2/4
- Cosine similarity: 0.386 > 0.322
 - Considers missing ratings as "negative"
 - Solution: subtract the (row) mean

| | I | | HP3 | TW | SW1 | SW2 | SW3 | |
|---|------------|-----|------|------|------|-----|-----|--|
| A | 2/3 1/3 | | | 5/3 | -7/3 | | | |
| B | 1/3 | 1/3 | -2/3 | | | | | |
| C | | | | -5/3 | 1/3 | 4/3 | | |
| D | | 0 | | | | | 0 | |

sim A,B vs. A,C:

0.092 > -0.559

Notice cosine sim. is correlation when data is centered at 0

Rating Predictions

From similarity metric to recommendations:

- Let r_x be the vector of user x's ratings
- Let N be the set of k users most similar to x who have rated item i
- Prediction for item s of user x:

•
$$r_{xi} = \frac{1}{k} \sum_{y \in N} r_{yi}$$

•
$$r_{xi} = \frac{\sum_{y \in N} s_{xy} \cdot r_{yi}}{\sum_{y \in N} s_{xy}}$$

- Other options?
- Many other tricks possible...

Shorthand:

 $s_{xy} = sim(x, y)$

Item-Item Collaborative Filtering

- So far: User-user collaborative filtering
- Another view: Item-item
 - For item *i*, find other similar items
 - Estimate rating for item *i* based on ratings for similar items
 - Can use same similarity metrics and prediction functions as in user-user model

$$r_{xi} = \frac{\sum_{j \in N(i;x)} S_{ij} \cdot r_{xj}}{\sum_{j \in N(i;x)} S_{ij}}$$

 s_{ij} ... similarity of items i and j r_{xj} ...rating of user u on item j N(i;x)... set items rated by x similar to i

users

| | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|--------|---|---|---|---|---|---|---|---|---|---|----|----|----|
| | 1 | 1 | | 3 | | | 5 | | | 5 | | 4 | |
| | 2 | | | 5 | 4 | | | 4 | | | 2 | 1 | 3 |
| movies | 3 | 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | |
| H | 4 | | 2 | 4 | | 5 | | | 4 | | | 2 | |
| | 5 | | | 4 | 3 | 4 | 2 | | | | | 2 | 5 |
| | 6 | 1 | | 3 | | 3 | | | 2 | | | 4 | |

- unknown rating



- rating between 1 to 5

users

| | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|--------|---|---|---|---|---|---|---|---|---|---|----|----|----|
| | 1 | 1 | | 3 | | ? | 5 | | | 5 | | 4 | |
| | 2 | | | 5 | 4 | | | 4 | | | 2 | 1 | 3 |
| movies | 3 | 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | |
| H | 4 | | 2 | 4 | | 5 | | | 4 | | | 2 | |
| | 5 | | | 4 | 3 | 4 | 2 | | | | | 2 | 5 |
| | 6 | 1 | | 3 | | 3 | | | 2 | | | 4 | |



- estimate rating of movie 1 by user 5

users

| | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | sim(1,m) |
|--|----------|---|---|---|---|---|---|---|---|---|----|----|----|-------------|
| | 1 | 1 | | 3 | | ? | 5 | | | 5 | | 4 | | 1.00 |
| | 2 | | | 5 | 4 | | | 4 | | | 2 | 1 | 3 | -0.18 |
| movies | <u>3</u> | 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | | <u>0.41</u> |
| THE CONTRACT OF THE CONTRACT O | 4 | | 2 | 4 | | 5 | | | 4 | | | 2 | | -0.10 |
| | 5 | | | 4 | 3 | 4 | 2 | | | | | 2 | 5 | -0.31 |
| | <u>6</u> | 1 | | 3 | | 3 | | | 2 | | | 4 | | 0.59 |

Neighbor selection:

Identify movies similar to movie 1, rated by user 5 31

Here we use Pearson correlation as similarity:

- 1) Subtract mean rating m_i from each movie i $m_1 = (1+3+5+5+4)/5 = 3.6$ row 1: [-2.6, 0, -0.6, 0, 0, 1.4, 0, 0, 1.4, 0, 0.4, 0]
- 2) Compute cosine similarities between rows

users

| | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | sim(1,m) |
|--------|----------|---|---|---|---|---|---|---|---|---|----|----|----|-------------|
| | 1 | 1 | | 3 | | ? | 5 | | | 5 | | 4 | | 1.00 |
| | 2 | | | 5 | 4 | | | 4 | | | 2 | 1 | 3 | -0.18 |
| movies | <u>3</u> | 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | | <u>0.41</u> |
| B | 4 | | 2 | 4 | | 5 | | | 4 | | | 2 | | -0.10 |
| | 5 | | | 4 | 3 | 4 | 2 | | | | | 2 | 5 | -0.31 |
| | <u>6</u> | 1 | | 3 | | 3 | | | 2 | | | 4 | | <u>0.59</u> |

Compute similarity weights:

users

| | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|--------|----------|---|---|---|---|-----|---|---|---|---|----|----|----|
| | 1 | 1 | | 3 | | 2.6 | 5 | | | 5 | | 4 | |
| | 2 | | | 5 | 4 | | | 4 | | | 2 | 1 | 3 |
| movies | <u>3</u> | 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | |
| Ħ | 4 | | 2 | 4 | | 5 | | | 4 | | | 2 | |
| | 5 | | | 4 | 3 | 4 | 2 | | | | | 2 | 5 |
| | <u>6</u> | 1 | | 3 | | 3 | | | 2 | | | 4 | |

Predict by taking weighted average:

$$r_{1.5} = (0.41^{*}2 + 0.59^{*}3) / (0.41 + 0.59) = 2.6$$

$$r_{ix} = \frac{\sum_{j \in N(i;x)} s_{ij} \cdot r_{jx}}{\sum s_{ij}}$$

CF: Common Practice

- Define similarity s_{ij} of items i and j
- Select k nearest neighbors N(i; x)
 - Items most similar to i, that were rated by x
- Estimate rating r_{xi} as the weighted average:

$$r_{xi} = b_{xi} + \frac{\sum_{j \in N(i;x)} s_{ij} \cdot (r_{xj} - b_{xj})}{\sum_{j \in N(i;x)} s_{ij}}$$

baseline estimate for r_{xi}

$$b_{xi} = \mu + b_x + b_i$$

• μ = overall mean movie rating

• b_x = rating deviation of user x= $(avg. rating of user x) - \mu$

 \mathbf{b}_{i} = rating deviation of movie \mathbf{i}

Before:

$$r_{xi} = \frac{\sum_{j \in N(i;x)} s_{ij} r_{xj}}{\sum_{j \in N(i;x)} s_{ij}}$$

Item-Item vs. User-User

| | Avatar | LOTR | Matrix | Pirates |
|-------|--------|------|--------|---------|
| Alice | 1 | | 0.8 | |
| Bob | | 0.5 | | 0.3 |
| Carol | 0.9 | | 1 | 0.8 |
| David | | | 1 | 0.4 |

- In practice, it has been observed that <u>item-item</u> often works better than user-user
- Why? Items are simpler, users have multiple tastes

Pros/Cons of Collaborative Filtering

- + Works for any kind of item
 - No feature selection needed
- Cold Start:
 - Need enough users in the system to find a match
- - Sparsity:
 - The user/ratings matrix is sparse
 - Hard to find users that have rated the same items
- - First rater:
 - Cannot recommend an item that has not been previously rated
 - New items, Esoteric items
- - Popularity bias:
 - Cannot recommend items to someone with unique taste
 - Tends to recommend popular items

Hybrid Methods

- Implement two or more different recommenders and combine predictions
 - Perhaps using a linear model
- Add content-based methods to collaborative filtering
 - Item profiles for new item problem
 - Demographics to deal with new user problem

Remarks & Practical Tips

- Evaluation
- Error metrics
- Complexity / Speed

Evaluation

movies

users

| 1 | 3 | 4 | | | |
|---|---|---|---|---|---|
| | 3 | 5 | | | 5 |
| | | 4 | 5 | | 5 |
| | | 3 | | | |
| | | 3 | | | |
| 2 | | | 2 | | 2 |
| | | | | 5 | |
| | 2 | 1 | | | 1 |
| | 3 | | | 3 | |
| 1 | | | | | |

Evaluation

movies users

Test Data Set

Evaluating Predictions

- Compare predictions with known ratings
 - Root-mean-square error (RMSE)
 - $\sqrt{\sum_{xi}(r_{xi}-r_{xi}^*)^2}$ where r_{xi} is predicted, r_{xi}^* is the true rating of x on i
 - Precision at top 10:
 - % of those in top 10
 - Rank Correlation:
 - Spearman's correlation between system's and user's complete rankings
- Another approach: 0/1 model
 - Coverage:
 - Number of items/users for which system can make predictions
 - Precision:
 - Accuracy of predictions
 - Receiver operating characteristic (ROC)
 - Tradeoff curve between false positives and false negatives

Problems with Error Measures

- Narrow focus on accuracy sometimes misses the point
 - Prediction Diversity
 - Prediction Context
 - Order of predictions
- In practice, we care only to predict high ratings:
 - RMSE might penalize a method that does well for high ratings and badly for others

Collaborative Filtering: Complexity

- Expensive step is finding k most similar customers: O(|X|)
- Too expensive to do at runtime
 - Could pre-compute
- Naïve pre-computation takes time $O(k \cdot |X|)$
 - X ... set of customers
- We already know how to do this!
 - Near-neighbor search in high dimensions (LSH)
 - Clustering
 - Dimensionality reduction

Tip: Add Data

- Leverage all the data
 - Don't try to reduce data size in an effort to make fancy algorithms work
 - Simple methods on large data do best
- Add more data
 - e.g., add IMDB data on genres
- More data beats better algorithms

http://anand.typepad.com/datawocky/2008/03/more-datausual.html

The Netflix Prize

Training data

- 100 million ratings, 480,000 users, 17,770 movies
- 6 years of data: 2000-2005

Test data

- Last few ratings of each user (2.8 million)
- Evaluation criterion: Root Mean Square Error (RMSE) =

$$\frac{1}{|R|} \sqrt{\sum_{(i,x)\in R} (\hat{r}_{xi} - r_{xi})^2}$$

• Netflix's system RMSE: 0.9514

Competition

- 2,700+ teams
- \$1 million prize for 10% improvement on Netflix

The Netflix Utility Matrix R

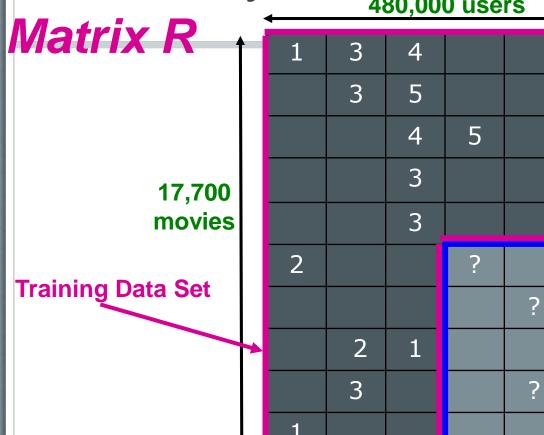
Matrix R

17,700 movies

480,000 users

| 1 | 3 | 4 | | | |
|---|---|---|---|---|---|
| | 3 | 5 | | | 5 |
| | | 4 | 5 | | 5 |
| | | 3 | | | |
| | | 3 | | | |
| 2 | | | 2 | | 2 |
| | | | | 5 | |
| | 2 | 1 | | | 1 |
| | 3 | | | 3 | |
| 1 | | | | | |





Test Data Set

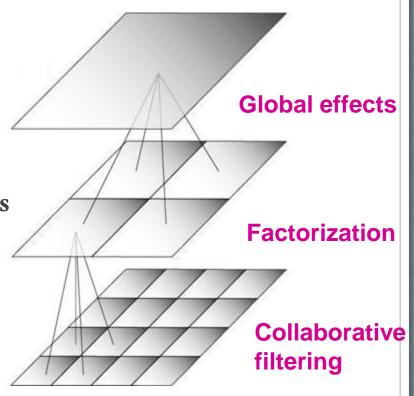
 $r_{3.6}$

True rating of user **x** on item

$$\mathbf{RMSE} = \frac{1}{|\mathbf{R}|} \sqrt{\sum_{\substack{(i,x) \in R}} (\hat{r}_{xi} - r_{xi})^2}$$
Predicted rating

BellKor Recommender System

- The winner of the Netflix Challenge!
- Multi-scale modeling of the data: Combine top level, "regional" modeling of the data, with a refined, local view:
 - Global:
 - Overall deviations of users/movies
 - Factorization:
 - Addressing "regional" effects
 - Collaborative filtering:
 - Extract local patterns



Modeling Local & Global Effects

Global:

- Mean movie rating: 3.7 stars
- The Sixth Sense is 0.5 stars above avg.
- Joe rates 0.2 stars below avg.
 ⇒ Baseline estimation:
 Joe will rate The Sixth Sense 4 stars
- Local neighborhood (CF/NN):
 - Joe didn't like related movie Signs
 - ⇒ Final estimate:

 Joe will rate The Sixth Sense 3.8 stars







Recap: Collaborative Filtering (CF)

- Earliest and most popular collaborative filtering method
- Derive unknown ratings from those of "similar" movies (item-item variant)
- Define similarity measure s_{ii} of items i and j
- Select k-nearest neighbors, compute the rating
 - N(i; x): items most similar to i that were rated by x

$$\hat{r}_{xi} = \frac{\sum_{j \in N(i;x)} S_{ij} \cdot r_{xj}}{\sum_{j \in N(i;x)} S_{ij} \cdot \sum_{j \in N(i;x)} S_{ij}}$$

s_{ij}... similarity of items *i* and *j*r_{xj}...rating of user *x* on item *j*N(i;x)... set of items similar to
item *i* that were rated by x

Modeling Local & Global Effects

• In practice we get better estimates if we model deviations:

$$r_{xi} = b_{xi} + \frac{\sum_{j \in N(i;x)} s_{ij} \cdot (r_{xj} - b_{xj})}{\sum_{j \in N(i;x)} s_{ij}}$$

baseline estimate for r_{xi}

$$b_{xi} = \mu + b_x + b_i$$

 μ = overall mean rating

 b_x = rating deviation of user x

= $(avg. rating of user x) - \mu$

 $\mathbf{b}_{i} = (avg. \ rating \ of \ movie \ \mathbf{i}) - \boldsymbol{\mu}$

Problems/Issues:

- 1) Similarity measures are "arbitrary"
- 2) Pairwise similarities neglect interdependencies among users
- **3)** Taking a weighted average can be restricting

Solution: Instead of s_{ij} use w_{ij} that we estimate directly from data

Idea: Interpolation Weights

Wij

• Use a weighted sum rather than weighted avg.:

$$\widehat{r_{xi}} = b_{xi} + \sum_{j \in N(i;x)} w_{ij} (r_{xj} - b_{xj})$$

- A few notes:
 - N(i; x) ... set of movies rated by user x that are similar to movie i
 - w_{ij} is the interpolation weight (some real number)
 - We allow: $\sum_{j \in N(i,x)} w_{ij} \neq 1$
 - w_{ij} models interaction between pairs of movies (it does not depend on user x)

Idea: Interpolation Weights

W_{ij}

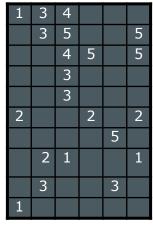
•
$$\widehat{r_{xi}} = b_{xi} + \sum_{j \in N(i,x)} w_{ij} (r_{xj} - b_{xj})$$

- How to set w_{ij} ?
 - Remember, error metric is: $\frac{1}{|R|} \sqrt{\sum_{(i,x) \in R} (\hat{r}_{xi} r_{xi})^2}$ or equivalently SSE: $\sum_{(i,x) \in R} (\hat{r}_{xi} r_{xi})^2$
 - Find w_{ii} that minimize SSE on training data!
 - Models relationships between item i and its neighbors j
 - w_{ij} can be learned/estimated based on x and all other users that rated i

Why is this a good idea?

Recommendations via Optimization

- Goal: Make good recommendations
 - Quantify goodness using RMSE:
 Lower RMSE ⇒ better recommendations
 - Want to make good recommendations on items that user has not yet seen. Can't really do this!



 Let's set build a system such that it works well on known (user, item) ratings
 And hope the system will also predict well the unknown ratings

Recommendations via Optimization

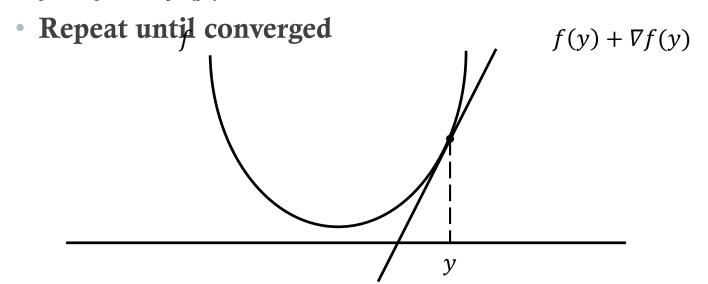
- Idea: Let's set values w such that they work well on known (user, item) ratings
- How to find such values w?
- Idea: Define an objective function and solve the optimization problem
- Find w_{ii} that minimize SSE on training data!

$$J(w) = \sum_{x,i} \left(\left[b_{xi} + \sum_{j \in N(i;x)} w_{ij} (r_{xj} - b_{xj}) \right] - r_{xi} \right)^{2}$$
Predicted rating
True rating

• Think of w as a vector of numbers

Detour: Minimizing a function

- A simple way to minimize a function f(x):
 - Compute the take a derivative ∇f
 - Start at some point y and evaluate $\nabla f(y)$
 - Make a step in the reverse direction of the gradient: $y = y \nabla f(y)$



Interpolation Weights

• We have the optimization problem, now what?

$$J(w) = \sum_{x} \left(\left[b_{xi} + \sum_{j \in N(i;x)} w_{ij} (r_{xj} - b_{xj}) \right] - r_{xi} \right)^{2}$$

- Gradient decent:
 - Iterate until convergence: $w \leftarrow w \eta \nabla_w J$ η ... learning rate
 - where $\nabla_w J$ is the gradient (derivative evaluated on data):

$$\nabla_{w}J = \left[\frac{\partial J(w)}{\partial w_{ij}}\right]$$

$$= 2\sum_{x,i} \left(\left[b_{xi} + \sum_{k \in N(i;x)} w_{ik}(r_{xk} - b_{xk})\right] - r_{xi}\right) (r_{xj} - b_{xj})$$

$$\text{for } j \in \{N(i;x), \forall i, \forall x\}$$

$$\text{else } \frac{\partial J(w)}{\partial w_{ij}} = \mathbf{0}$$

$$\text{while } |w_{new} - w_{old}| > \varepsilon:$$

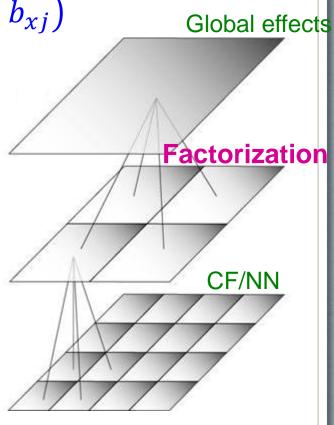
$$w_{old} = w_{new}$$

$$w_{new} = w_{old} - \eta \cdot \nabla w_{old}$$

• Note: We fix movie i, go over all r_{xi} , for every movie $j \in N(i; x)$, we compute $\frac{\partial J(w)}{\partial w_{ij}}$

Interpolation Weights

- So far: $\widehat{r_{xi}} = b_{xi} + \sum_{j \in N(i;x)} w_{ij} (r_{xj} b_{xj})$
 - Weights w_{ij} derived based on their role; no use of an arbitrary similarity measure $(w_{ij} \neq s_{ij})$
 - Explicitly account for interrelationships among the neighboring movies
- Next: Latent factor model
 - Extract "regional" correlations



Performance of Various

Methods Global average: 1.1296

User average: 1.0651

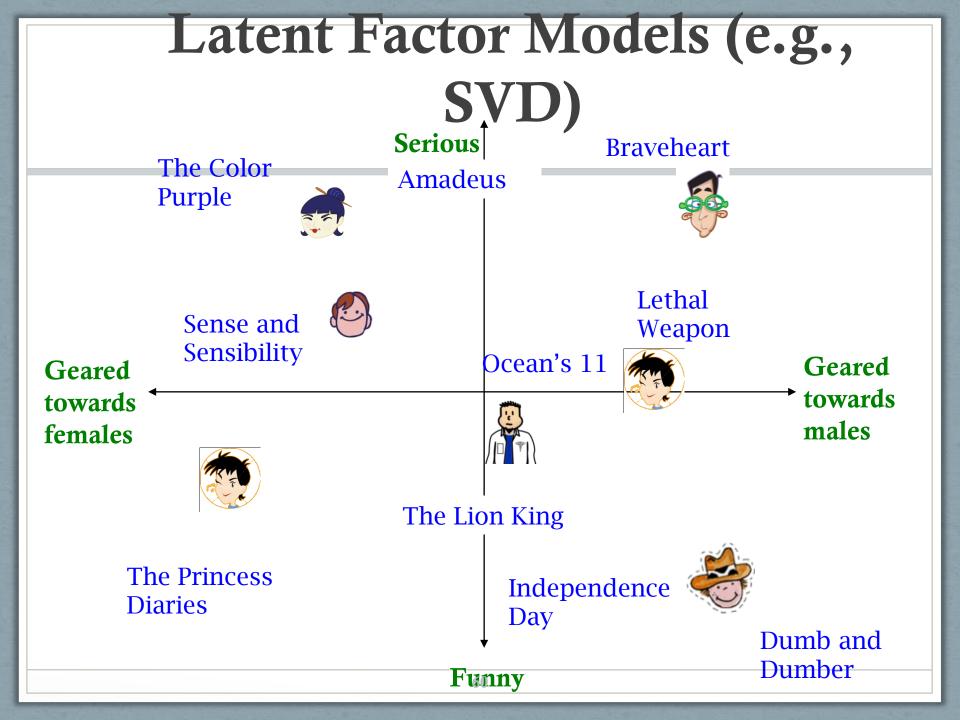
Movie average: 1.0533

Netflix: 0.9514

Basic Collaborative filtering: 0.94

CF+Biases+learned weights: 0.91

Grand Prize: 0.8563

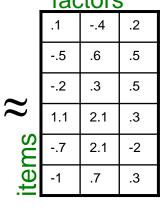


Latent Factor Models

• "SVD" on Netflix data: $\mathbf{R} \approx \mathbf{Q} \cdot \mathbf{P}^T$

SVD: $A = U \Sigma V^T$

| | users | | | | | | | | | | | |
|---|-------|---|---|---|---|---|---|---|---|---|---|---|
| | 1 | | 3 | | | 5 | | | 5 | | 4 | |
| | | | 5 | 4 | | | 4 | | | 2 | 1 | 3 |
| I | 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | |
| | | 2 | 4 | | 5 | | | 4 | | | 2 | |
| | | | 4 | 3 | 4 | 2 | | | | | 2 | 5 |
| I | 1 | | 3 | | 3 | | | 2 | | | 4 | |
| 1 | | | | | | | | | | | | |



| 1.1 | 2 | .3 | .5 | -2 | 5 | .8 | 4 | .3 | 1.4 | 2.4 |
|-----|----|----|-----|-----|----|-----|-----|----|-----|-----|
| 8 | .7 | .5 | 1.4 | .3 | -1 | 1.4 | 2.9 | 7 | 1.2 | 1 |
| 2.1 | 4 | .6 | 1.7 | 2.4 | .9 | 3 | .4 | .8 | .7 | 6 |

PT

R

Q

- For now let's assume we can approximate the rating matrix R as a product of "thin" $Q \cdot P^{T}$
 - R has missing entries but let's ignore that for now!
 - Basically, we will want the reconstruction error to be small on known ratings and we don't care about the values on the missing

ones

Ratings as Products of Factors

• How to estimate the missing rating of user x for item i?

items

| users | | | | | | | | | | | |
|-------|---|---|---|---|---|---|---|---|---|---|---|
| 1 | | 3 | | | 5 | | | 5 | | 4 | |
| | | 5 | 4 | ? | | 4 | | | 2 | 1 | 3 |
| 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | |
| | 2 | 4 | | 5 | | | 4 | | | 2 | |
| | | 4 | 3 | 4 | 2 | | | | | 2 | 5 |
| 1 | | 3 | | 3 | | | 2 | | | 4 | |

-.4

~

| $\hat{r}_{xi} =$ | $= q_i \cdot$ | p_x |
|------------------|-------------------------------|----------------|
| $=\sum$ | \mathbf{q}_{if} | $\cdot p_{xf}$ |
| | = row <i>i</i> of = columr | |

-.5 .6 .5 -.2 .3 .5 1.1 2.1 .3 -.7 2.1 -2 -1 .7 .3

.2

-.2 .3 .5 -.5 1.4 2.4 -.9 1.1 -2 -.4 .7 .5 1.4 -1 1.4 2.9 -.7 1.2 -.1 1.3 -.4 1.7 2.4 -.3 .4 -.6 .1

users

PT

factors

Q

Ratings as Products of Factors

• How to estimate the missing rating of user x for item i?

items

| 1 | users | | | | | | | | | | | |
|---|-------|---|---|---|---|---|---|---|---|---|---|---|
| | 1 | | 3 | | | 5 | | | 5 | | 4 | |
| | | | 5 | 4 | ? | | 4 | | | 2 | 1 | 3 |
| | 2 | 4 | | 1 | 2 | | თ | | 4 | თ | 5 | |
| | | 2 | 4 | | 5 | | | 4 | | | 2 | |
| | | | 4 | 3 | 4 | 2 | | | | | 2 | 5 |
| | 1 | | 3 | | 3 | | | 2 | | | 4 | |

≈

| $\hat{r}_{xi} =$ | $= q_i \cdot$ | p_x |
|------------------|-------------------------------|----------------|
| $=\sum$ | \mathbf{q}_{if} | $\cdot p_{xf}$ |
| | = row <i>i</i> of = columr | |

| (0 | 5 | .6 | .5 |
|-------|-----|-----|----|
| items | 2 | .3 | .5 |
| ite | 1.1 | 2.1 | .3 |
| | 7 | 2.1 | -2 |
| | | _ | |

2 1.1 -.2 .3 .5 -.8 .7 .5 1.4 2.1 -.4 .6 1.7

.3 -1 1.4 2.4 .9 -.3

-.5

users

 .8
 -.4
 .3
 1.4
 2.4

 1.4
 2.9
 -.7
 1.2
 -.1

 -.3
 .4
 .8
 .7
 -.6

-.9

1.3

PT

factors

Q

Ratings as Products of **Factors**

 How to estimate the missing rating of user x for item ?

items

| users | | | | | | | | | | | |
|-------|---|---|---|----|---|---|---|---|---|---|---|
| 1 | | 3 | | | 5 | | | 5 | | 4 | |
| | | 5 | 4 | 2. | 4 | 4 | | | 2 | 1 | 3 |
| 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | |
| | 2 | 4 | | 5 | | | 4 | | | 2 | |
| | | 4 | 3 | 4 | 2 | | | | | 2 | 5 |
| 1 | | 3 | | 3 | | | 2 | | | 4 | |

| $\hat{r}_{xi} =$ | $= q_i$ | p_x |
|------------------|------------------------------|----------------|
| $=\sum$ | \mathbf{q}_{if} | $\cdot p_{xf}$ |
| | = row <i>i</i> o = columr | |

| | .1 | 4 | .2 |
|-------|-----|-----|----|
| () | 5 | .6 | .5 |
| items | 2 | .3 | .5 |
| ite | 1.1 | 2.1 | .3 |
| | 7 | 2.1 | -2 |
| | -1 | .7 | .3 |

users

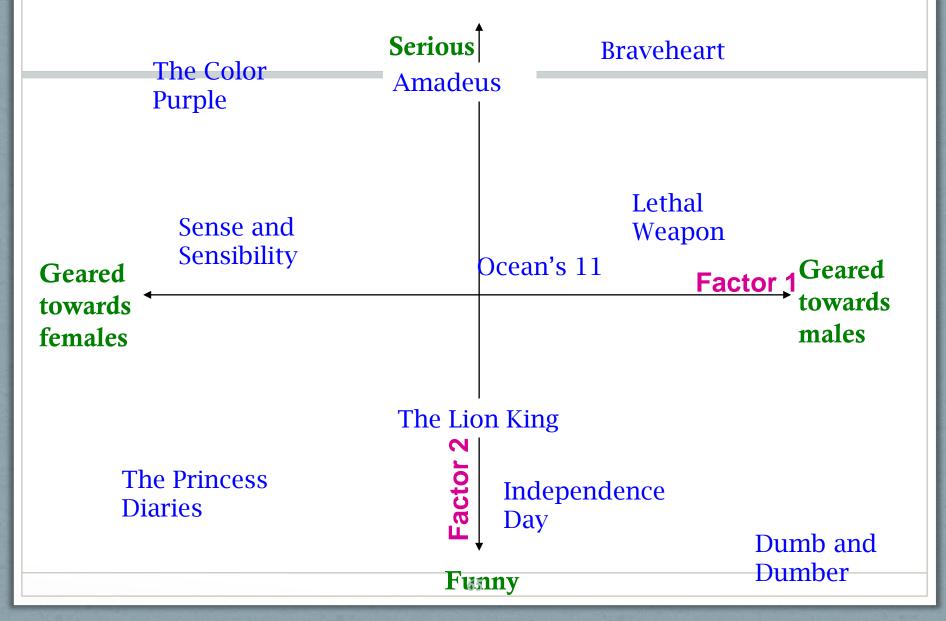
| ors | 1.1 | 2 | .3 | .5 | -2 | 5 -1 .9 | .8 | 4 | .3 | 1.4 | 2.4 | 9 |
|-----|-----|----|----|-----|-----|---------------|-----|-----|----|-----|-----|-----|
| act | 8 | .7 | .5 | 1.4 | .3 | -1 | 1.4 | 2.9 | 7 | 1.2 | 1 | 1.3 |
| ff | 2.1 | 4 | .6 | 1.7 | 2.4 | .9 | 3 | .4 | .8 | .7 | 6 | .1 |

PT

f factors



Latent Factor Models



Latent Factor Models

The Color Purple



Serious

Braveheart

Amadeus



Sense and Sensibility



Lethal Weapon

Ocean's 11



Factor

Geared towards males



Geared

towards





The Lion King



Independence Day



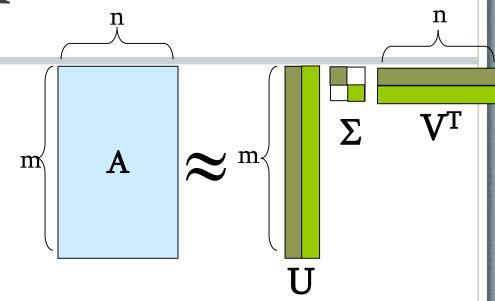
Dumb and Dumber

Funny

Recap: SVD

Remember SVD:

- A: Input data matrix
- U: Left singular vecs
- V: Right singular vecs
- Σ : Singular values



So in our case:

"SVD" on Netflix data:
$$R \approx Q \cdot P^T$$

 $A = R$, $Q = U$, $P^T = \Sigma V^T$

$$\hat{r}_{xi} = q_i \cdot p_x$$

SVD: More good stuff

• We already know that SVD gives minimum reconstruction error (Sum of Squared Errors):

$$\min_{U,V,\Sigma} \sum_{ij \in A} \left(A_{ij} - [U\Sigma V^{\mathrm{T}}]_{ij} \right)^{2}$$

- Note two things:
 - SSE and RMSE are monotonically related:
 - $RMSE = \frac{1}{c}\sqrt{SSE}$ Great news: SVD is minimizing RMSE
 - Complication: The sum in SVD error term is over all entries (no-rating in interpreted as zero-rating). But our *R* has missing entries!

Latent Factor Models

| | users . | | | | | | | | | | | | | factors | | |
|---|---------|---|----------------------|---------------|--|---|---|---|---|---|---|---|---|--|---|--|
| 1 | | 3 | | | 5 | | | 5 | | 4 | | | .1 | 4 | .2 | |
| | | 5 | 4 | | | 4 | | | 2 | 1 | 3 | | 5 | .6 | .5 | |
| 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | | | 2 | ფ. | .5 | |
| | 2 | 4 | | 5 | | | 4 | | | 2 | | pprox | 1.1 | 2.1 | .3 | |
| | | 4 | 3 | 4 | 2 | | | | | 2 | 5 | ns | 7 | 2.1 | -2 | |
| 1 | | 3 | | 3 | | | 2 | | | 4 | | ter | -1 | .7 | .3 | |
| | | 2 | 5 2 4 2 4 4 | 2 4 1 1 2 4 3 | 1 3 2 4 2 4 2 4 3 4 4 3 4 | 1 3 5 5 4 6 2 4 1 2 2 4 5 6 4 3 4 2 | 1 3 5 5 4 4 4 2 4 1 2 3 3 3 4 3 4 2 4 3 4 2 4 4 3 4 2 4 | 1 3 5 2 4 4 2 4 3 4 5 4 5 4 4 6 4 5 4 7 4 4 4 8 4 4 4 9 4 4 4 4 | 2 4 1 2 4 4 2 4 1 2 3 4 4 4 4 4 4 4 4 4 5 4 4 4 4 3 4 2 4 4 | 1 3 5 5 5 5 6 2 2 2 2 4 2 2 2 4 3 4 3 3 4 3 3 3 4 3 3 4 3 4 3 4 2 4 | 1 3 5 5 5 4 4 4 2 1 2 4 1 2 3 4 3 5 2 4 5 4 2 4 2 2 4 3 4 2 5 4 2 2 | 1 3 5 5 4 6 7 6 7 6 7 7 6 7 | 1 3 5 4 5 5 4 2 1 3 5 4 2 5 5 4 5 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 | 1 3 5 5 4 1 1 5 2 4 1 2 1 3 5 5 2 2 4 1 2 3 4 3 5 2 2 2 4 3 4 2 2 5 1.1 4 3 4 2 2 5 7 | 1 3 5 5 4 1 4 2 4 1 2 1 3 5 .6 2 4 1 2 3 4 3 5 2 .3 2 4 5 4 2 2 5 1.1 2.1 4 3 4 2 5 2 5 7 2.1 | |

| users | | | | | | | | | | | |
|-------|----|----|-----|-----|----|-----|-----|----|-----|-----|-----|
| 1.1 | 2 | .3 | .5 | -2 | 5 | .8 | 4 | .3 | 1.4 | 2.4 | 9 |
| 8 | .7 | .5 | 1.4 | .3 | -1 | 1.4 | 2.9 | 7 | 1.2 | 1 | 1.3 |
| 2.1 | 4 | .6 | 1.7 | 2.4 | .9 | 3 | .4 | .8 | .7 | 6 | .1 |

PT

O

- SVD isn't defined when entries are missing!
- Use specialized methods to find P, Q

•
$$\min_{P,Q} \sum_{(i,x)\in\mathbb{R}} (r_{xi} - q_i \cdot p_x)^2$$

$$\hat{r}_{xi} = q_i \cdot p_x$$

- Note:
 - We don't require cols of P, Q to be orthogonal/unit length
 - P, Q map users/movies to a latent space
 - The most popular model among Netflix contestants

Finding the Latent Factors

Latent Factor Models

• Our goal is to find P and Q such tat:

$$\min_{P,Q} \sum_{(i,x)\in R} (r_{xi} - q_i \cdot p_x)^2$$

users

| | | | | | | | | | | | | _ |
|---|---|---|---|---|---|---|---|---|---|---|---|-----|
| 1 | | 3 | | | 5 | | | 5 | | 4 | | |
| | | 5 | 4 | | | 4 | | | 2 | 1 | 3 | |
| 2 | 4 | | 1 | 2 | | 3 | | 4 | 3 | 5 | | |
| | 2 | 4 | | 5 | | | 4 | | | 2 | | ~ |
| | | 4 | 3 | 4 | 2 | | | | | 2 | 5 | Swe |
| 1 | | 3 | | 3 | | | 2 | | | 4 | | 140 |
| | | | | | | | | | | | | |

factors

| .1 | 4 | .2 | |
|-----|-----|----|----|
| 5 | .6 | .5 | ١. |
| 2 | .3 | .5 | |
| 1.1 | 2.1 | .3 | |
| 7 | 2.1 | -2 | |
| -1 | .7 | .3 | |

users

| 1.1 | 2 | .3 | .5 | -2 | 5 | .8 | 4 | .3 | 1.4 | 2.4 | 9 |
|-----|----|----|-----|-----|----|-----|-----|----|-----|-----|-----|
| 8 | .7 | .5 | 1.4 | .3 | -1 | 1.4 | 2.9 | 7 | 1.2 | 1 | 1.3 |
| 2.1 | 4 | .6 | 1.7 | 2.4 | .9 | 3 | .4 | .8 | .7 | 6 | .1 |

PT

Back to Our Problem

- Want to minimize SSE for unseen test data
- Idea: Minimize SSE on training data
 - Want large k (# of factors) to capture all the signa
 - But, SSE on test data begins to rise for k > 2

| 1 | 3 | 4 | | | |
|---|---|---|---|---|---|
| | 3 | 5 | | | 5 |
| | | 4 | 5 | | 5 |
| | | 3 | | | |
| | | 3 | | | |
| 2 | | | ? | | ? |
| | | | | ? | |
| | 2 | 1 | | | ? |
| | 3 | | | ? | |
| 1 | | | | | |
| | | | | | |

- This is a classical example of overfitting:
 - With too much freedom (too many free parameters) the model starts fitting noise
 - That is it fits too well the training data and thus not generalizing well to unseen test data

Dealing with Missing Entries

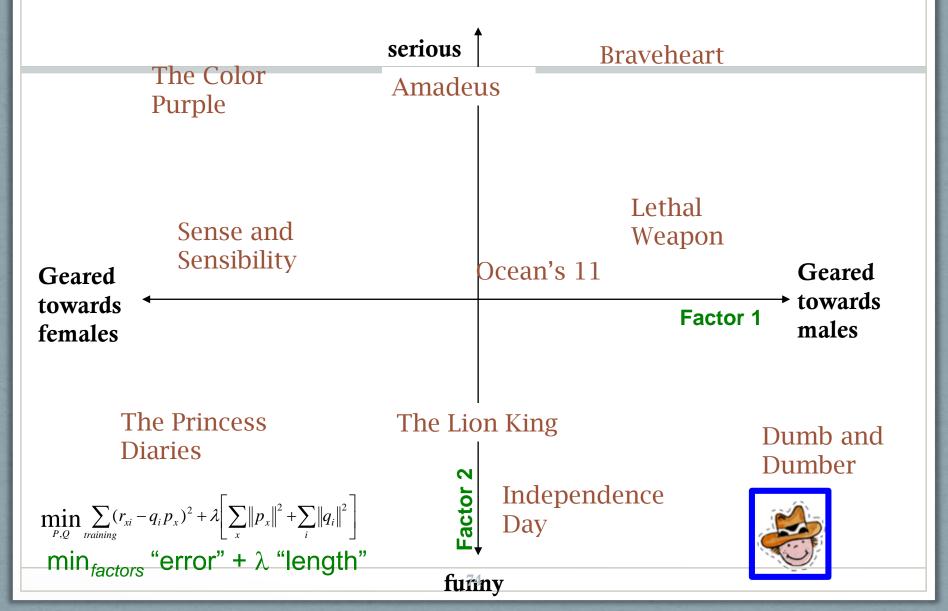
- To solve overfitting we introduce regularization:
 - Allow rich model where there are sufficient data
 - Shrink aggressively where data are scarce

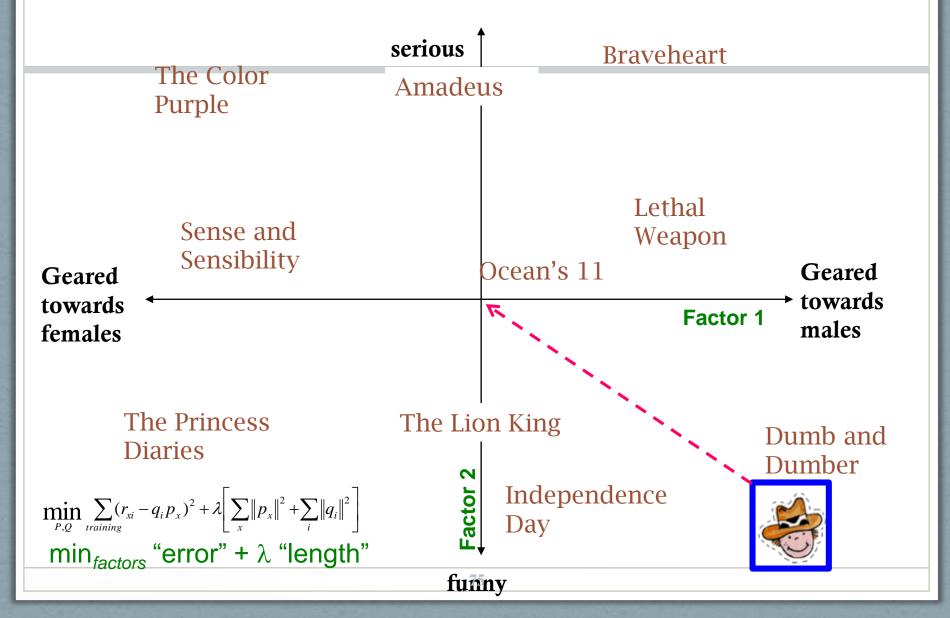
| 1 | 3 | 4 | | | |
|---|---|---|---|---|---|
| | 3 | 5 | | | 5 |
| | | 4 | 5 | | 5 |
| | | 3 | | | |
| | | 3 | | | |
| 2 | | | ? | | ? |
| | | | | ? | |
| | 2 | 1 | | | ? |
| | 3 | | | ? | |
| 1 | | | | | |

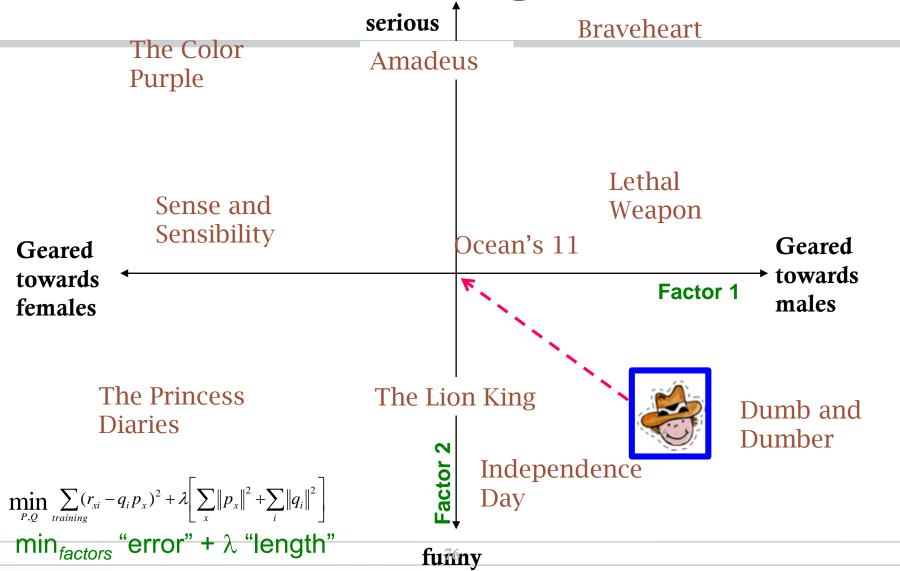
$$\min_{P,Q} \sum_{training} (r_{xi} - q_i p_x)^2 + \left[\lambda_1 \sum_{x} \|p_x\|^2 + \lambda_2 \sum_{i} \|q_i\|^2 \right]$$
"error" "length"

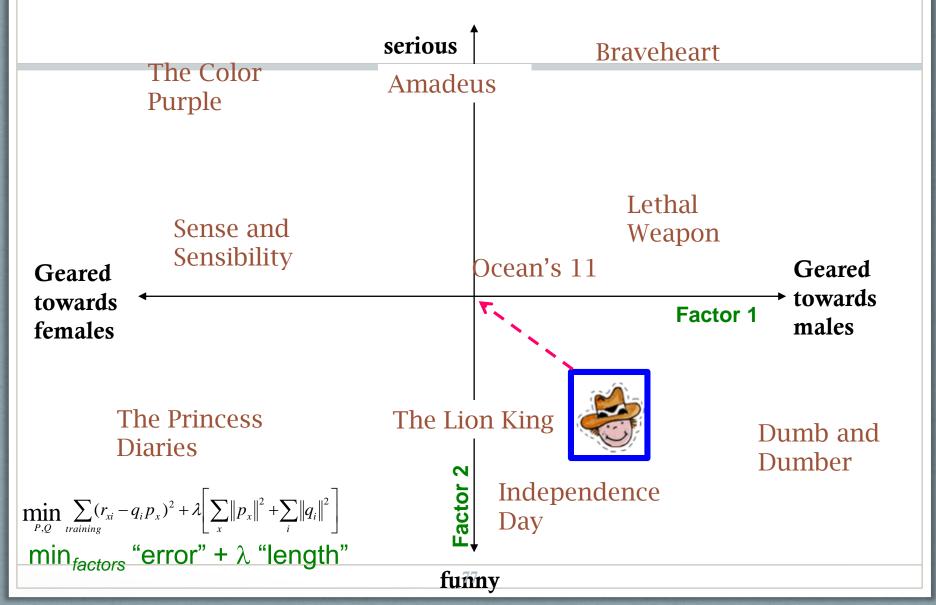
 $\lambda_1, \lambda_2 \dots$ user set regularization parameters

Note: We do not care about the "raw" value of the objective function, but we care in P,Q that achieve the minimum of the objective

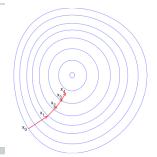








Stochastic Gradient Descent



• Want to find matrices P and Q:

$$\min_{P,Q} \sum_{training} (r_{xi} - q_i p_x)^2 + \left[\lambda_1 \sum_{x} ||p_x||^2 + \lambda_2 \sum_{i} ||q_i||^2 \right]$$

- Gradient decent:
 - Initialize P and Q (using SVD, pretend missing ratings are
 How to compute gradien
 - Do gradient descent:

•
$$P \leftarrow P - \eta \cdot \nabla P$$

•
$$Q \leftarrow Q - \eta \cdot \nabla Q$$

• where ∇Q is gradient/derivative of matrix Q:

$$\nabla Q = [\nabla q_{if}]$$
 and $\nabla q_{if} = \sum_{x,i} -2(r_{xi} - q_i p_x)p_{xf} + 2\lambda_2 q_{if}$

• Here q_{if} is entry f of row q_i of matrix Q

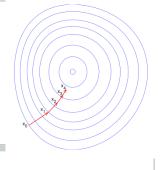
Observation: Computing gradients is slow!

How to compute gradient of a matrix?

Compute gradient of every

element independently!

Stochastic Gradient Descent



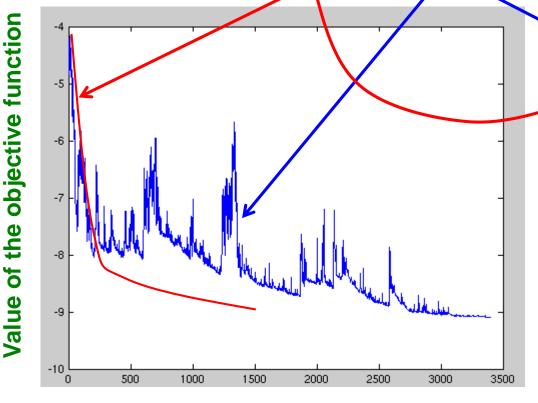
- Gradient Descent (GD) vs. Stochastic GD
 - Observation: $\nabla Q = [\nabla q_{if}]$ where

$$\nabla q_{if} = \sum_{x,i} -2(r_{xi} - q_{if}p_{xf})p_{xf} + 2\lambda q_{if} = \sum_{x,i} \nabla Q(r_{xi})$$

- Here q_{if} is entry f of row q_i of matrix Q
- $Q = Q \eta \nabla Q = Q \eta \left[\sum_{x,i} \nabla Q (r_{xi}) \right]$
- Idea: Instead of evaluating gradient over all ratings evaluate it for each individual rating and make a step
- GD: $Q \leftarrow Q \eta \left[\sum_{r_{xi}} \nabla Q(r_{xi}) \right]$
- SGD: $Q \leftarrow Q \mu \nabla Q(r_{xi})$
 - Faster convergence!
 - Need more steps but each step is computed much faster

SGD vs. GD

Convergence of GD vs. SGD



Iteration/step

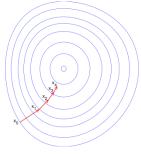
GD improves the value of the objective function at every step.

SGD improves the value but in a "noisy" way.

GD takes fewer steps to converge but each step takes much longer to compute.

In practice, **SGD** is much faster!

Stochastic Gradient Descen



- Stochastic gradient decent:
 - Initialize P and Q (using SVD, pretend missing ratings are
 0)
 - Then iterate over the ratings (multiple times if necessary) and update factors:

For each r_{xi} :

•
$$\varepsilon_{xi} = 2(r_{xi} - q_i \cdot p_x)$$

•
$$q_i \leftarrow q_i + \mu_1 \left(\varepsilon_{xi} p_x - \lambda_2 q_i \right)$$

•
$$p_x \leftarrow p_x + \mu_2 \left(\varepsilon_{xi} \ q_i - \lambda_1 \ p_x \right)$$

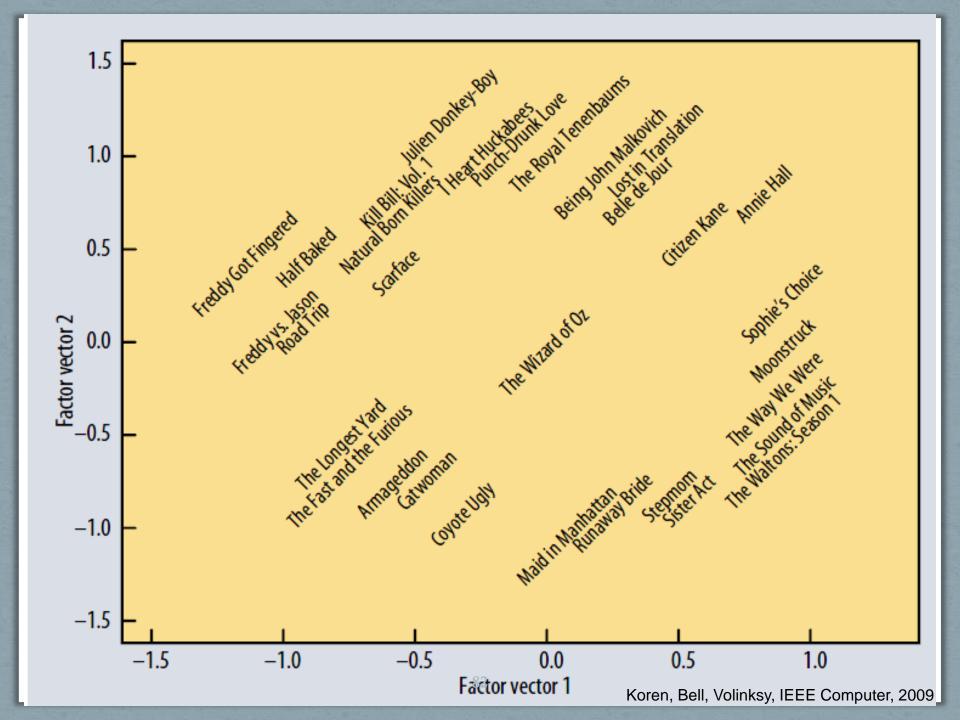
Compute gradient do a "sten"

(derivative of the "error")

(update equation)

(update equation) μ ... learning rate

- 2 for loops:
 - For until convergence:
 - For each r_{xi}



Extending Latent Factor Model to Include Biases

Modeling Biases and Interactions

user bias



movie bias



user-movie interaction



Baseline predictor

- Separates users and movies
- Benefits from insights into user's behavior
- Among the main practical contributions of the competition
 - $\blacksquare \mu = \text{overall mean rating}$
 - $\mathbf{b}_{\mathbf{x}}$ = bias of user \mathbf{x}
 - \mathbf{b}_{i} = bias of movie \mathbf{i}

User-Movie interaction

- Characterizes the matching between users and movies
- Attracts most research in the field
- Benefits from algorithmic and mathematical innovations

Baseline Predictor

• We have expectations on the rating by user *x* of movie *i*, even without estimating *x*'s attitude towards movies like *i*







- Rating scale of user x
- Values of other ratings user gave recently (day-specific mood, anchoring, multi-user accounts)

- (Recent) popularity of movie i
- Selection bias; related to number of ratings user gave on the same day ("frequency")

Putting It All Together

$$r_{xi} = \mu + b_x + b_i + q_i \cdot p_x$$

Mean rating user x movie i

Mean rating user x movie i

User-Movie interaction

• Example:

- Mean rating: $\mu = 3.7$
- You are a critical reviewer: your ratings are 1 star lower than the mean: $b_x = -1$
- Star Wars gets a mean rating of 0.5 higher than average movie: $b_i = +0.5$
- Predicted rating for you on Star Wars:

$$= 3.7 - 1 + 0.5 = 3.2$$

Fitting the New Model

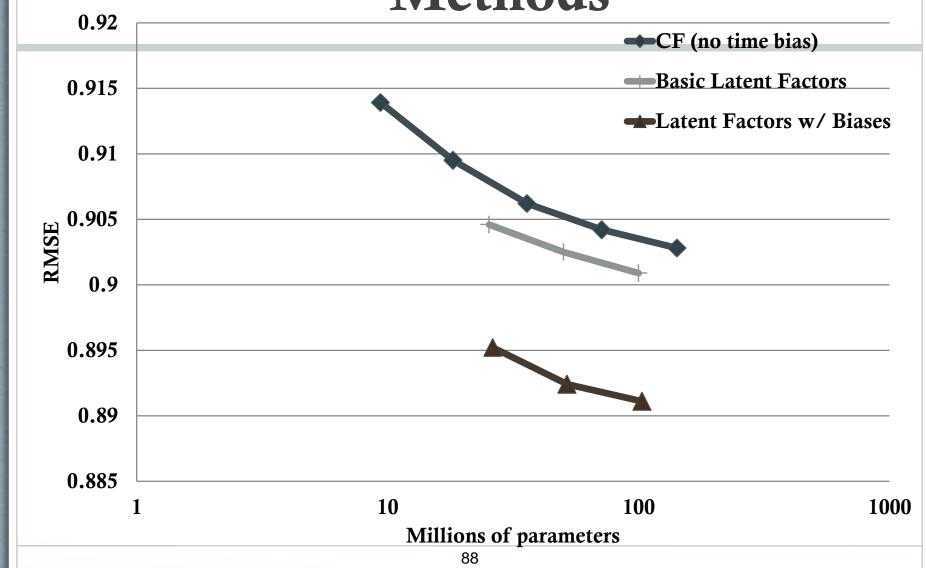
• Solve:

$$\min_{\mathcal{Q},P} \sum_{(x,i)\in R} \left(r_{xi} - (\mu + b_x + b_i + q_i \ p_x) \right)^2$$
 goodness of fit
$$+ \left(\lambda_1 \sum_i \left\| q_i \right\|^2 + \lambda_2 \sum_x \left\| p_x \right\|^2 + \lambda_3 \sum_x \left\| b_x \right\|^2 + \lambda_4 \sum_i \left\| b_i \right\|^2 \right)$$
 regularization

 λ is selected via gridsearch on a validation set

- Stochastic gradient decent to find parameters
 - Note: Both biases b_x , b_i as well as interactions q_i , p_x are treated as parameters (we estimate them)

Performance of Various Methods



Performance of Various

Methods Global average: 1.1296

User average: 1.0651

Movie average: 1.0533

Netflix: 0.9514

Basic Collaborative filtering: 0.94

Collaborative filtering++: 0.91

Latent factors: 0.90

Latent factors+Biases: 0.89

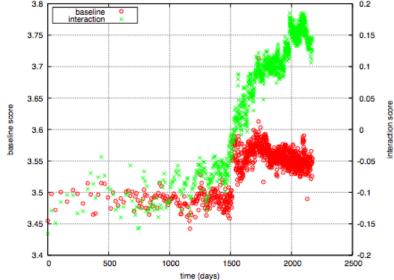
Grand Prize: 0.8563

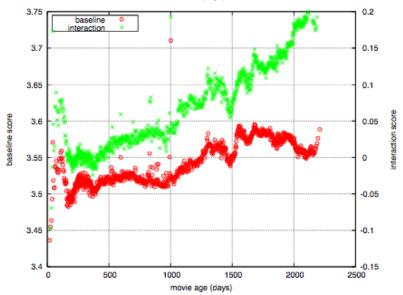
The Netflix Challenge: 2006-09

Temporal Biases Of Users

- Sudden rise in the average movie rating (early 2004)
 - Improvements in Netflix
 - GUI improvements
 - Meaning of rating changed
- Movie age
 - Users prefer new movies without any reasons
 - Older movies are just inherently better than newer ones

Y. Koren, Collaborative filtering with temporal dynamics, KDD '09





Temporal Biases & Factors

Original model:

$$r_{xi} = \mu + b_x + b_i + q_i \cdot p_x$$

• Add time dependence to biases:

$$r_{xi} = \mu + b_x(t) + b_i(t) + q_i \cdot p_x$$

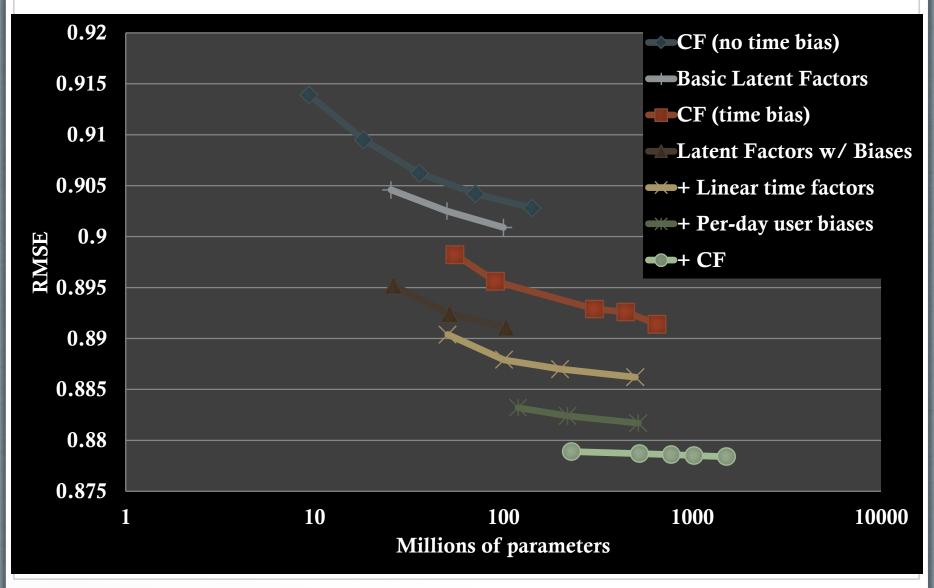
- Make parameters b_x and b_i to depend on time
- (1) Parameterize time-dependence by linear trends
 - (2) Each bin corresponds to 10 consecutive weeks

$$b_i(t) = b_i + b_{i,\operatorname{Bin}(t)}$$

- Add temporar dependence to factors
 - $p_x(t)$... user preference vector on day t

Y. Koren, Collaborative filtering with temporal dynamics, KDD '09

Adding Temporal Effects



Performance of Various Methods

Global average: 1.1296

User average: 1.0651

Movie average: 1.0533

Netflix: 0.9514

Basic Collaborative filtering: 0.94

Collaborative filtering++: 0.91

Latent factors: 0.90

Latent factors+Biases: 0.89

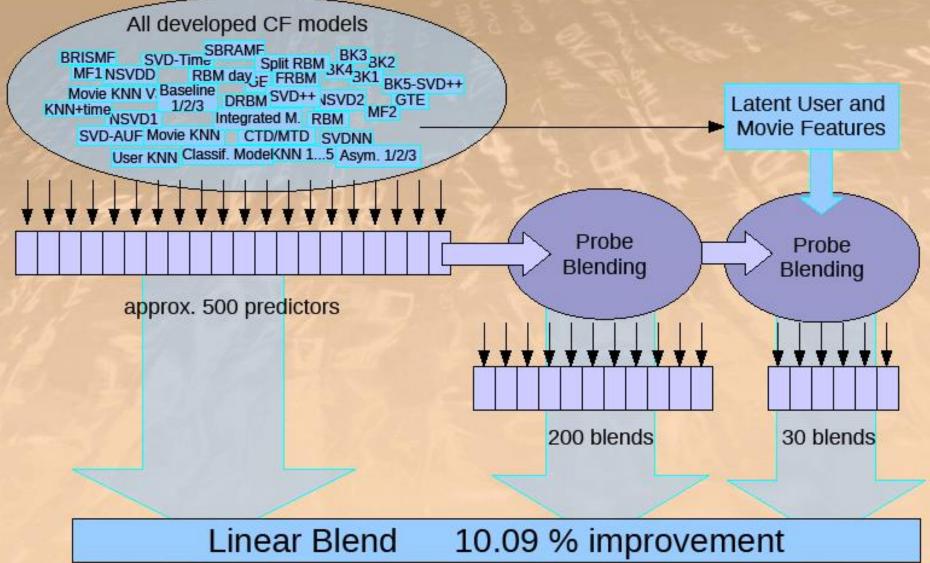
Latent factors+Biases+Time: 0.876

Still no prize! (2)
Getting desperate.
Try a "kitchen sink" approach!

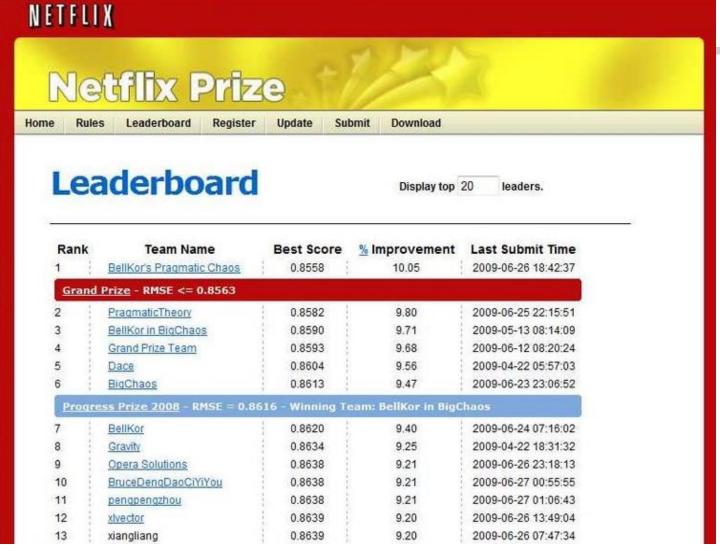
Grand Prize: 0.8563

The big picture

Solution of BellKor's Pragmatic Chaos



Standing on June 26th 2009



June 26th submission triggers 30-day "last call"

The Last 30 Days

Ensemble team formed

- Group of other teams on leaderboard forms a new team
- Relies on combining their models
- Quickly also get a qualifying score over 10%

BellKor

- Continue to get small improvements in their scores
- Realize that they are in direct competition with Ensemble

Strategy

- Both teams carefully monitoring the leaderboard
- Only sure way to check for improvement is to submit a set of predictions
 - This alerts the other team of your latest score

24 Hours from the Deadline

- Submissions limited to 1 a day
 - Only 1 final submission could be made in the last 24h
- 24 hours before deadline...
 - BellKor team member in Austria notices (by chance) that Ensemble posts a score that is slightly better than BellKor's
- Frantic last 24 hours for both teams
 - Much computer time on final optimization
 - Carefully calibrated to end about an hour before deadline
- Final submissions
 - BellKor submits a little early (on purpose), 40 mins before deadline
 - Ensemble submits their final entry 20 mins later
 -and everyone waits....

Netflix Prize



Home

Rules

Leaderboard

Update

Progress Prize 2007 - RMSE = 0.8723 - Winning Team: KorBell

Download

Leaderboard

Showing Test Score. Click here to show quiz score

Display top 20 ‡ leaders.

| Rank | Team Name | Best Test Score | % Improvement | Best Submit Time | | | |
|---|-------------------------------------|---------------------|---------------|---------------------|--|--|--|
| Grand | Prize - RMSE = 0.8567 - Winning Te | am: RellKor's Pragr | natic Chang | | | | |
| 1 | BellKor's Pragmatic Chaos | 0.8567 | 10.06 | 2009-07-26 18:18:28 | | | |
| 2 | The Ensemble | 0.8567 | 10.06 | 2009-07-26 18:38:22 | | | |
| 3 | Grand Prize Team | 3.8002 | J.9 | :4 | | | |
| 4 | Opera Solutions and Vandelay United | 0.8588 | 9.84 | 2009-07-10 01:12:31 | | | |
| 5 | Vandelay Industries ! | 0.8591 | 9.81 | 2009-07-10 00:32:20 | | | |
| 6 | PragmaticTheory | 0.8594 | 9.77 | 2009-06-24 12:06:56 | | | |
| 7 | BellKor in BigChaos | 0.8601 | 9.70 | 2009-05-13 08:14:09 | | | |
| 8 | <u>Dace</u> | 0.8612 | 9.59 | 2009-07-24 17:18:43 | | | |
| 9 | Feeds2 | 0.8622 | 9.48 | 2009-07-12 13:11:51 | | | |
| 10 | BigChaos | 0.8623 | 9.47 | 2009-04-07 12:33:59 | | | |
| 11 | Opera Solutions | 0.8623 | 9.47 | 2009-07-24 00:34:07 | | | |
| 12 | BellKor | 0.8624 | 9.46 | 2009-07-26 17:19:11 | | | |
| Progress Prize 2008 - RMSE = 0.8627 - Winning Team: BellKor in BigChaos | | | | | | | |
| 13 | xiangliang | 0.8642 | 9.27 | 2009-07-15 14:53:22 | | | |
| 14 | Gravity | 0.8643 | 9.26 | 2009-04-22 18:31:32 | | | |
| 15 | Ces | 0.8651 | 9.18 | 2009-06-21 19:24:53 | | | |
| 16 | Invisible Ideas | 0.8653 | 9.15 | 2009-07-15 15:53:04 | | | |
| 17 | Just a guy in a garage | 0.8662 | 9.06 | 2009-05-24 10:02:54 | | | |
| 18 | J Dennis Su | 0.8666 | 9.02 | 2009-03-07 17:16:17 | | | |
| 19 | Craig Carmichael | 0.8666 | 9.02 | 2009-07-25 16:00:54 | | | |
| 20 | acmehill | 0.8658 | 9.00 | 2009-03-21 16:20:50 | | | |

Million \$ Awarded Sept 21st 2009



Acknowledgments

- Some slides and plots borrowed from Yehuda Koren, Robert Bell and Padhraic Smyth
- Further reading:
 - Y. Koren, Collaborative filtering with temporal dynamics, KDD '09
 - http://www2.research.att.com/~volinsky/netflix/bpc.html
 - http://www.the-ensemble.com/

Any Questions?