

ON DETERMINING THE SPECTRUM OF PRIMORDIAL INHOMOGENEITY FROM THE COBE DMR SKY MAPS: RESULTS OF TWO-YEAR DATA ANALYSES

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ABSTRACT

Data analysis has been applied to the two-year COBE-DMR 53 and 90 GHz sky maps. The Bayesian power spectrum estimation results are consistent with the

Subject headings: cosmic microwave background — cosmology: observations — methods: statistical

1. INTRODUCTION

The determination of the power spectrum of primordial inhomogeneities and their consistency with the predictions of inflation are critical issues in contemporary cosmology. Standard inflationary scenarios imply a power-law spectrum $P(k) \propto k^n$ with $n \approx 1$ on the scales probed in the COBE DMR sky maps. Previous attempts to determine the primordial power spectrum from the DMR found both relatively steep spectra and sensitivity to the inclusion or exclusion of the quadrupole in their results. Most methods have employed approximate statistical techniques and have relied on Monte Carlo techniques to access and/or calibrate the final results.

In this *Letter* the COBE DMR two-year 53 and 90 GHz data are analyzed to determine the primordial power spectrum using the methods described in Grski (1994). Specifically, the sky maps are Fourier decomposed in the basis of orthonormal functions on the Galaxy-cut sky to yield a set of harmonic mode coefficients, which are linear in pixel temperatures. These are then used in a maximum likelihood analyses to infer the parameters of the theoretical anisotropy models. The merits of the present method are (1) harmonic mode coupling is explicitly accounted for by construction of the orthonormal functions of the Galaxy-cut sky, (2) since the harmonic modes have a Gaussian probability distribution an *exact* likelihood function for the model parameters can be employed, (3) the monopole and dipole components, which are physically irrelevant for the power spectrum estimation, are algebraically excluded, and (4) the technique permits a simultaneous analysis of different frequency maps taking full advantage of both the auto- and cross-correlation information in the data.

In this analysis we Fourier decompose the two-year DMR sky maps over the $\ell = 46$, where the DMR beam response has fallen to ≈ 0.2 , and the multipole amplitude is entirely noise dominated. No attempt is made to model and subtract formally the diffuse high-latitude Galactic emission, which is predominantly quadrupolar in nature. Therefore, in what follows, the power spectrum parameters are derived for two cases: one in which data spanning the multipole range $\ell \in [2, 46]$ are used, and the

other in which the quadrupole ($\ell = 2$) mode is excluded.

Hereafter, bold upper case letters denote matrices; vectors are denoted by an arrow above the letter; and p is

TABLE 1

Column 1	Column 2	Column 3	Column 4
Item 1	Item 2	Item 3	Item 4

NOTE. — Summary of main results.

a pixel label.

2. METHOD

Describe method. Define data model and likelihood. Outline how the likelihood was computed (grid or MCMC).

Define the power law model in terms of Q and n .

3. DATA

Summarize properties of data. Which data are used (experiment, frequencies etc.)? Pixel resolution (N_{side}), ℓ_{max} – everything necessary to repeat the analysis for other researchers.

Show a sky map of the smoothed data. Use the Healpix routine “smoothing” to do this; it works just like anafast. Smooth with a 7° beam, and plot with “map2gif”. Show the RMS pattern as well.

4. RESULTS

Show the 2D likelihood contours. Summarize constraints on Q and n .

5. CONCLUSIONS

Summarize results. Discuss their importance, referring to the discovery to the initial seeds for structure formation. Mention that these results are in good agreement with expectations from inflationary theory.

Who do you want to thank for helping out with this project?

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REFERENCES

- Górski, K. M., Hinshaw, G., Banday, A. J., Bennett, C. L., Wright, E. L., Kogut, A., Smoot, G. F., and Lubin, P. 1994, ApJL, 430, 89