



ESCOLA SUPERIOR
DE TECNOLOGIA
E GESTÃO

Polytechnic of Leiria
School of Technology and Management
Department of Electrical Engineering
Bachelor's Degree in Electrical and Computer Engineering

BATTAIHEALTH
BATTERY CONDITION ESTIMATION IN
AUTOMOTIVE AND RAILWAY APPLICATIONS USING
AI

PEDRO ANDRÉ SILVA FERREIRA

Leiria, Junho de 2025



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Final report of the Project Curricular Unit of the Bachelor's Degree in
Eletrotechnical and Computers Engineering, branch of Eletronics and Computers.

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RESUMO

Deverá conter de forma sucinta, clara e objetiva as questões mais importantes tratadas no corpo do trabalho.

Deverá ter, no máximo, 250 palavras.

A estimativa precisa do Estado de Saúde (SoH), Estado de Carga (SoC) e Vida Útil Restante (RUL) das baterias é crucial para aplicações automóveis e ferroviárias, dado o papel essencial das baterias na eficiência energética e fiabilidade dos sistemas de transporte. A gestão eficaz destes parâmetros pode prevenir falhas inesperadas, otimizar os ciclos de carga e descarga, e prolongar a vida útil das baterias, contribuindo assim para uma redução significativa nos custos operacionais e ambientais. A Inteligência Artificial (IA) tem mostrado grande potencial na tarefa de estimar SoH, SoC e RUL das baterias. Algoritmos de machine learning e redes neurais podem analisar grandes volumes de dados históricos e em tempo real, identificando padrões complexos que são difíceis de detectar com métodos tradicionais. A aplicação de IA permite uma previsão mais precisa e adaptativa das condições da bateria, melhorando a segurança e a eficiência operacional em veículos automóveis e ferroviários. Os datasets utilizados para a estimativa de SoH, SoC e RUL de baterias incluem uma variedade de dados recolhidos de ciclos de carga e descarga, condições de temperatura, tensões, correntes e outros parâmetros relevantes. Estes dados podem ser obtidos a partir de testes laboratoriais controlados, bem como de operações reais em campo. A qualidade e a abrangência dos datasets são essenciais para o treino eficaz dos modelos de IA, garantindo que eles possam generalizar bem para diferentes tipos de baterias e condições de operação. O desenvolvimento deste projeto envolve várias etapas-chave. Inicialmente, serão identificados os datasets e pré-processados os dados relevantes das baterias. Em seguida, serão desenvolvidos e treinados modelos de IA utilizando técnicas de machine learning supervisionado e não supervisionado. A validação dos modelos será realizada através de testes exaustivos com datasets distintos, assegurando a sua robustez e precisão. Finalmente, será implementado um sistema protótipo capaz de estimar em tempo real o SoH, SoC e RUL das baterias, com o objetivo de ser integrado em aplicações automóveis e ferroviárias, promovendo a inovação e a

sustentabilidade nos sistemas de transporte.

ABSTRACT

Escrever o resumo em inglês.

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GLOSSARY

LIST OF ABBREVIATIONS

CNN Convolutional Neural Network. xv, 25

EKF Extended Kalman Filter. xv, 23, 24

LSTM Long Short-Term Memory. xv, 25

SoC State of Charge. xv, 23, 24

SoH State of Health. xv, 23

INTRODUCTION

BACKGROUND MATERIAL AND SUPPORTING TECHNOLOGIES

This chapter presents the foundational background material and supporting technologies that were used in the project. The first section introduces the analytical frameworks used for battery data processing, including time series and spectral analysis techniques that are essential for understanding temporal patterns in battery behavior. Following this, we describe the comprehensive suite of software tools and platforms that facilitated the research and development process, from hyperparameter optimization and experiment tracking to data visualization and version control. The chapter then transitions to the core theoretical concepts fundamental to battery health monitoring, including detailed explanations of key battery parameters such as State of Charge (SoC), State of Health (SoH), and Remaining Useful Life (RUL). Additionally, we cover the essential evaluation metrics used to assess model performance and provide an in-depth discussion of battery degradation mechanisms that directly impact health estimation accuracy. Finally, the chapter addresses the technical challenges inherent in battery health monitoring, from the complexity of electrochemical processes to the practical difficulties of real-world implementation. This comprehensive background establishes the technical foundation necessary for understanding the methodologies and results presented in subsequent chapters.

2.1 TIME SERIES ANALYSIS OF BATTERY DATA

Time series analysis focuses on the temporal evolution of battery parameters such as voltage, current, and SoC. This approach models and forecasts battery behavior, identifies trends, and detects anomalies in the time domain.

2.2 SPECTRAL ANALYSIS OF BATTERY DATA

Spectral analysis is a frequency-domain technique used to characterize the dynamic behavior of battery systems by analyzing signals such as voltage, current, or impedance. This approach decomposes time-series data into its frequency components, revealing periodic patterns, noise characteristics, or system resonances that may not be evident in the time domain. Spectral analysis is particularly useful for understanding battery degradation, thermal effects, and electrochemical processes.

2.3 OPTUNA

Optuna is an open-source hyperparameter optimization framework used to search for the best hyperparameters in machine learning models Akiba et al., 2019. It employs efficient algorithms like Tree-structured Parzen Estimator (TPE) to systematically explore hyperparameter spaces, supporting parallel and distributed optimization. In this work, Optuna was utilized to automate the tuning process, enhancing model performance by identifying optimal hyperparameter configurations with reduced manual effort.

2.4 WEIGHTS AND BIASES (WANDB)

Weights & Biases (WandB) is a machine learning platform designed for experiment tracking and visualization *Weights & Biases* 2025. It enables real-time logging and monitoring of training metrics, hyperparameters, and model outputs. In this study, WandB was employed to keep track of training processes and visualize losses, providing interactive dashboards to analyze experiments, debug models, and ensure reproducible workflows across iterations.

2.5 PLOTJUGGLER

PlotJuggler is an open-source time series visualization tool designed for fast, intuitive, and extensible data analysis Faconti, 2025. It features a user-friendly drag-and-drop interface, enabling efficient visualization of large datasets, both offline and in real-time. In this work, PlotJuggler was highly effective for exploring and analyzing data within datasets, allowing for the visualization of time series, identification of patterns, and application of transformations like derivatives or moving averages through its Transform Editor. Its compatibility with formats such as CSV, ROS, and MQTT, along with plugin extensibility, made it a valuable tool for detailed data inspection and analysis.

2.6 ORANGE DATA MINING

Orange Data Mining is an open-source data visualization and analysis platform designed for exploratory data analysis and machine learning workflows *biolab/orange3: :bulb: Orange: Interactive data analysis* 2025. It provides a visual programming interface with drag-and-drop widgets that enable users to build data analysis pipelines without extensive coding. Orange offers comprehensive tools for data preprocessing, feature selection, correlation analysis, and outlier detection through interactive visualizations and statistical methods. In this work, Orange was instrumental for exploring correlations within battery datasets and identifying outliers that could potentially skew model performance. Its intuitive interface allowed for rapid prototyping of data cleaning pipelines, enabling efficient removal of anomalous data points while preserving the integrity of temporal relationships in battery time series data. The platform's correlation analysis capabilities were particularly valuable for understanding feature relationships and selecting relevant variables for subsequent machine learning models.

2.7 GIT VERSION CONTROL

Git is a distributed version control system designed to handle projects of all sizes with speed and efficiency *Git* 2025. It tracks changes in source code and files during software

development, enabling multiple contributors to work on the same project simultaneously while maintaining a complete history of modifications. Git provides features such as branching, merging, and distributed workflows that facilitate collaborative development and experimentation. In this work, Git was employed to ensure robust version control throughout the research process, maintaining a comprehensive history of code changes, experimental iterations, and documentation updates. All project files, including machine learning models, data processing scripts, and analysis notebooks, were systematically committed and pushed to GitHub repositories. This approach guaranteed that all work was safely preserved, enabled rollback to previous versions when needed, and facilitated reproducible research by maintaining clear documentation of the project’s evolution and experimental milestones.

2.8 PYTORCH

PyTorch is an open-source machine learning framework developed by Facebook’s AI Research lab, designed for deep learning applications with a focus on flexibility and ease of use Ansel et al., 2024. It provides dynamic computational graphs, allowing for intuitive model development and debugging through its eager execution model. PyTorch features automatic differentiation capabilities through its autograd system, enabling efficient gradient computation for backpropagation in neural networks. The framework supports GPU acceleration through CUDA, making it suitable for training large-scale models efficiently. In this work, PyTorch served as the primary framework for developing and training deep learning models for the use case of the project. PyTorch is able to seamlessly integrate with other tools in the machine learning pipeline, such as Optuna for hyperparameter optimization and WandB for experiment tracking.

2.9 CONDA ENVIRONMENTS

Conda is an open-source package management and environment management system that simplifies the installation, running, and updating of packages and their dependencies Conda, 2025. It creates isolated environments where different versions of Python, libraries, and dependencies can coexist without conflicts, making it particularly valuable

for this projects. This approach ensured that version conflicts between packages were avoided, enabled seamless collaboration across different development machines, and guaranteed that the exact software environment could be recreated for reproducibility.

2.10 CORE CONCEPTS

Battery technology serves as the foundation for energy storage systems across numerous applications, from portable electronics to electric vehicles and grid-scale storage. Modern batteries primarily fall into several categories, including lithium-ion, lead-acid, nickel-metal hydride, and flow batteries, each with distinct electrochemical properties, energy densities, and lifecycle characteristics. The health of these batteries is characterized by parameters such as state of charge (SoC), state of health (SoH), capacity fade, internal resistance, and degradation rates, which collectively determine performance and longevity. Monitoring these parameters presents unique challenges due to the complex, nonlinear relationships between observable measurements and underlying battery conditions. Artificial intelligence and machine learning approaches offer powerful solutions to these challenges by enabling pattern recognition across multidimensional battery data. Supervised learning algorithms can predict remaining useful life, while unsupervised methods can detect anomalies indicative of impending failure. Deep learning architectures, particularly recurrent neural networks and transformers, have demonstrated exceptional capability in extracting temporal patterns from battery operational data, making them especially valuable for health prognostics in dynamic usage scenarios.

2.10.1 *State of Charge (SoC)*

The State of Charge represents the amount of energy remaining in a battery relative to its maximum capacity. It can be expressed as:

$$\text{SoC} = \frac{\text{Remaining Charge or Energy}}{\text{Maximum Charge or Energy Capacity}} \times 100\% \quad (1)$$

However, due to the chemical complexity of batteries and variations among individual cells, the SoC is always an approximate estimate. One factor contributing to the nonlinearity

in its estimation is the formation of impurity layers in the pores of the electrodes. When these pores are blocked by impurities, electron movement is hindered, leading to irregular voltages and currents.

2.10.2 *State of Health (SoH)*

The State of Health reflects the battery's ability to store and deliver energy compared to its original specifications. It can be expressed as:

$$\text{SoH} = \frac{\text{Current Maximum Capacity}}{\text{Original Maximum Capacity}} \times 100\% \quad (2)$$

The nonlinearity in SoH estimation primarily arises from the progressive degradation of electrode materials. As impurities accumulate in the electrode pores, the available surface area for electrochemical reactions decreases, reducing the battery's effective capacity. This process is highly dependent on the number of charge/discharge cycles and operational conditions, making it difficult to model SoH linearly over time.

2.10.3 *Remaining Useful Life (RUL)*

The Remaining Useful Life quantifies the number of cycles remaining before the battery's performance degrades below a specified threshold. It can be expressed as:

$$\text{RUL} = \text{Total Expected Useful Life} - \text{Current Age} \quad (3)$$

Predicting RUL is particularly challenging due to the accumulation of impurities in the electrode pores. As the pores become obstructed, the degradation rate accelerates, leading to a sudden drop in battery performance. This nonlinear dynamic makes it difficult to accurately predict the exact point at which the battery will reach its end of useful life.

2.10.4 Mean Absolute Error (MAE)

The Mean Absolute Error measures the average magnitude of errors in a set of predictions, without considering their direction. It is calculated as:

$$\text{MAE} = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i| \quad (4)$$

where y_i is the actual value, \hat{y}_i is the predicted value, and n is the number of observations. MAE is intuitive and robust to outliers, as it does not square the errors, but it does not penalize larger errors as heavily as other metrics. This makes it less sensitive to extreme deviations in predictions, which can be a limitation in contexts like battery performance where large errors may indicate critical failures.

2.10.5 Mean Squared Error (MSE)

The Mean Squared Error quantifies the average of the squared differences between predicted and actual values. It is expressed as:

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad (5)$$

MSE emphasizes larger errors due to the squaring of differences, making it sensitive to outliers. In battery modeling, this can be useful for detecting significant deviations in predictions of parameters like State of Charge or State of Health, but its sensitivity to outliers may amplify the impact of irregular data points caused by factors like electrode impurities or sensor noise.

2.10.6 Root Mean Squared Error (RMSE)

The Root Mean Squared Error is the square root of the MSE, providing an error metric in the same units as the original data. It is defined as:

$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n y_i - \mathcal{G}^2} \quad (6)$$

RMSE balances the emphasis on larger errors from MSE while being more interpretable due to its unit consistency with the data. In battery applications, RMSE is often used to evaluate prediction accuracy for metrics like SoC or RUL, but its sensitivity to outliers can be a drawback when dealing with nonlinear degradation patterns caused by electrode pore blockages.

2.10.7 Mean Absolute Percentage Error (MAPE)

The Mean Absolute Percentage Error measures the average percentage error between predicted and actual values. It is calculated as:

$$\text{MAPE} = \frac{1}{n} \sum_{i=1}^n \left| \frac{y_i - \mathcal{G}}{y_i} \right| \times 100\% \quad (7)$$

MAPE is useful for comparing prediction accuracy across datasets with different scales, as it normalizes errors relative to the actual values. However, it can become problematic when actual values are close to zero, as in some battery SoC scenarios, leading to large percentage errors. Additionally, its reliance on relative errors may mask significant absolute deviations in critical battery performance metrics.

2.10.7.1 Deep Learning Training Fundamentals

Key training parameters that impact model performance in battery state estimation:

- **Epochs:** Complete passes through the training dataset. For battery data, 50–500 epochs are typical, balancing underfitting (too few) and overfitting (too many) on temporal sequences.
- **Batch Size:** Number of samples processed simultaneously. Smaller batches (16–32) help with nonlinear patterns, while larger batches (128–256) provide stable gradients but may struggle with irregular battery data.
- **Patience (Early Stopping):** Epochs to wait without validation improvement before stopping. Values of 5–20 epochs prevent overfitting while allowing models to generalize across different battery systems.
- **Learning Rate:** Controls parameter adjustment magnitude. Battery degradation requires careful tuning: too high (>0.01) misses subtle patterns, too low (<0.0001) causes slow convergence.
- **Optimizers:** Adam optimizer is commonly used for adaptive learning rates. SGD with momentum provides stable convergence but requires more tuning for battery applications.
- **Regularization:** L1/L2 regularization and dropout prevent overfitting on limited battery datasets. Particularly important when training data comes from few battery types or conditions.
- **Loss Functions:** MSE for regression tasks (SoC, capacity), MAE for robustness against outliers, cross-entropy for classification (fault detection). Custom losses can incorporate domain knowledge.
- **Validation:** Time-based splitting ensures models tested on future data. Cross-validation must account for temporal dependencies in degradation sequences.

2.10.8 *Battery Degradation and Capacity Fade*

Battery degradation refers to the gradual loss of a battery's ability to store and deliver energy, driven by chemical reactions, temperature fluctuations, charge/discharge cycles, and aging. This degradation manifests as capacity fade, resulting in reduced device runtime or diminished electric vehicle driving range. The key mechanisms include:

- **Solid Electrolyte Interphase (SEI) Growth:** A layer forms on the anode, consuming lithium ions and reducing capacity. This process is accelerated at high temperatures and currents, leading to an initial irreversible capacity loss of approximately 10% during formation cycles.
- **Lithium Plating:** At low temperatures or high charge rates, lithium deposits on the anode, forming “dead lithium” that contributes to irreversible capacity loss and increases safety risks.
- **Particle Fracture:** Mechanical stress from cycling causes cracks in electrode materials, reducing active material availability and exacerbating capacity decline.
- **Positive Electrode (PE) Decomposition:** Structural changes in the cathode, such as spinel/rock salt phase formation, degrade performance and contribute to active material loss.
- **Impedance Increase:** Rising interfacial resistance, predominantly at the positive electrode, limits efficient charge transfer and indirectly reduces usable capacity. After 800 cycles, electrode resistance can increase tenfold.

2.10.9 *Capacity Fade*

The Zhang et al., 2000 paper studies and explains very well the capacity fade refers to the progressive decline in a lithium-ion battery’s ability to store energy, manifesting as reduced device runtime or diminished electric vehicle driving range. This phenomenon is driven by several key mechanisms:

Studies report capacity losses ranging from 12.4% to 32% after 500–800 cycles, corresponding to an average loss of 0.025–0.05% per cycle Zhang et al., 2000.

2.10.10 *Internal Resistance Degradation in Lithium-Ion Batteries*

As lithium-ion batteries age, their internal resistance increases, adversely affecting power delivery, charging efficiency, and thermal management. This degradation is particularly

pronounced during calendar ageing, as detailed in the study by Stroe et al., 2018 on LFP/C-based batteries. The primary mechanisms contributing to this increase include:

- **Solid Electrolyte Interface (SEI) Growth:** The SEI layer on the graphite anode thickens over time, reducing Li ion permeability. This growth follows a power law dependence (approximately $t^{0.8}$) and is accelerated at high temperatures and high state-of-charge (SOC) levels, leading to increased resistance and contact loss within the anode.
- **Lithium Plating:** Deposition of metallic lithium on the anode clogs electrode pores, impeding ion transport and elevating resistance, particularly under high SOC conditions.
- **Cathode Structural Degradation:** At the LFP cathode, binder decomposition, oxidation of conductive agents, and corrosion of current collectors reduce inter-particle conductivity, contributing to resistance increase, especially at elevated temperatures.
- **Electrolyte Decomposition:** Decomposition products form resistive surface layers on both electrodes, further increasing internal resistance, with effects amplified at high temperatures and SOC levels.

The study demonstrates that internal resistance increases nonlinearly with storage time, with exponential acceleration due to higher storage temperatures (e.g., 55°C) and SOC levels (e.g., 90%). For instance, after 20 years at 25°C and 50% SOC, resistance may rise by approximately 71%, doubling at 100% SOC. This increased resistance results in slower charging, diminished power output, and accelerated degradation due to enhanced heat generation, impacting battery performance and lifespan.

2.10.11 *Battery Health Monitoring*

Battery health monitoring is critical for ensuring reliability, safety, and longevity of battery systems. Monitoring involves assessing key parameters such as the state of charge and the state of health (SoH), which provide essential insights into battery performance and remaining operational capacity.

2.10.11.1 *Technical Challenges*

The technical challenges in monitoring battery health arise from the complex nature of battery systems and the difficulties in accurately estimating SOC and SOH.

2.10.11.2 *Complexity of Battery Chemistry*

Batteries, particularly lithium-ion batteries, have intricate internal chemistries that are difficult to model and monitor. Factors such as temperature, charge-discharge rates, and depth of discharge influence degradation, making accurate SOH estimation challenging. The nonlinear and complex degradation processes vary with usage conditions, environmental factors, and battery design, complicating predictive modeling.

2.10.11.3 *Measurement Difficulties*

Measuring individual battery parameters, such as internal resistance, temperature, and voltage, is technically challenging, especially in real-time applications. This requires precise sensors and sophisticated equipment, which may not be feasible in real-world scenarios. For instance, accurately measuring internal resistance or temperature in a moving vehicle is far more complex than in a controlled lab environment.

2.10.11.4 *Modeling and Estimation*

rever isto !!!

Developing accurate models for SOH estimation is complex. Electrochemical models, which simulate battery behavior based on physical and chemical principles, require extensive computational resources and detailed parameter inputs (e.g., electrolyte properties, reaction rates). Semi-empirical models often oversimplify electrochemical processes, reducing their effectiveness under extreme conditions. Equivalent circuit models (ECMs) may lack precision during high-rate charging/discharging or extreme temperatures due to their simplified nature.

2.10.11.5 *Limitations of Data-Driven Methods*

Data-driven approaches, such as machine learning techniques (e.g. Support Vector Regression, Gaussian Process Regression, Artificial Neural Networks), rely on large, high-quality datasets, which can be difficult to obtain. These methods also lack physical interpretability, making it difficult to understand their predictions. Additionally, issues like overfitting and high computational demands pose challenges for real-time applications.

2.10.11.6 *Complexity of Hybrid Methods*

Hybrid approaches, which combine model-based and data-driven methods, can improve accuracy but increase system complexity and computational costs. Interpreting errors in these systems remains a challenge, requiring further research to enhance transparency and efficiency.

2.10.12 *Laboratory vs Real World Conditions*

There is a significant discrepancy between laboratory-simulated conditions and actual operational environments. Laboratory settings often use sophisticated equipment that is not available in real-world applications, limiting the applicability of monitoring methods. For example, real-world conditions like varying temperatures or road vibrations are difficult to replicate in a lab, affecting SOH estimation accuracy.

2.10.13 *Real-Time Monitoring*

Achieving real-time, reliable SOH monitoring is crucial for safety-critical applications but is technically demanding. Battery management systems (BMS) must balance accuracy with computational efficiency to provide timely insights without overloading system resources.

2.10.14 *Environmental Factors*

Batteries are sensitive to environmental conditions such as temperature, humidity, and vibration. Monitoring systems must account for these factors, which can significantly impact battery health and performance. For example, high temperatures can accelerate battery degradation, while low temperatures may reduce capacity, complicating health estimation.

2.10.15 *Cost of Monitoring Systems*

Implementing sophisticated battery health monitoring systems can be expensive, both in terms of initial setup and ongoing maintenance. This includes the cost of sensors, data storage, and computational infrastructure, which can be prohibitive for smaller organizations or applications.

2.10.16 *Data and Computational Costs*

AI and data-driven methods require significant computational resources and high-quality data, which can be costly to acquire and process. The high demand for data and computing power presents challenges, particularly for real-time monitoring applications and edge devices.

STATE OF THE ART

The accurate estimation of SoC, SoH, and RUL is critical for optimizing battery performance in automotive and railway applications. These metrics, defined as follows, underpin the reliability and efficiency of battery management systems (BMS):

- **SoC:** The ratio of remaining charge to maximum capacity, expressed as $\text{SoC} = \frac{\text{Remaining Charge}}{\text{Maximum Capacity}} \times 100\%$.
- **SoH:** The ratio of current maximum capacity to original capacity, given by $\text{SoH} = \frac{\text{Current Maximum Capacity}}{\text{Original Maximum Capacity}} \times 100\%$.
- **RUL:** The number of cycles remaining before the battery's performance falls below a specified threshold, defined as $\text{RUL} = \text{Total Expected Life} - \text{Current Age}$.

Traditional methods, such as Coulomb Counting and Kalman Filters, often struggle with nonlinearities and dynamic operating conditions. Recent advancements in Artificial Intelligence (AI), particularly machine learning and deep learning, offer promising solutions by capturing complex patterns in battery data. This chapter reviews the state of the art in SoC, SoH, and RUL estimation, focusing on AI-based approaches.

3.0.1 *Traditional Methods for SoC, SoH, and RUL Estimation*

Traditional methods for battery state estimation can be categorized into physics-based and statistical approaches, each with inherent limitations.

3.0.1.1 *Physics-Based Methods*

Physics-based methods model the electrochemical and electrical behavior of batteries. Key approaches include:

- **Equivalent Circuit Models (ECMs):** Represent batteries using electrical components (e.g., resistors, capacitors) to simulate voltage and current dynamics. ECMs are computationally efficient but lack precision under varying conditions.
- **Electrochemical Models:** Simulate internal chemical reactions, offering high accuracy but requiring significant computational resources and detailed parameter knowledge.

3.0.1.2 *Statistical Methods*

Statistical techniques rely on empirical data to estimate battery states. Common methods include:

- **Coulomb Counting:** Integrates current over time to estimate SoC. This method is sensitive to measurement errors and initial SoC inaccuracies.
- **Kalman Filters:** Use recursive algorithms to refine state estimates by combining model predictions with noisy measurements. While effective for linear systems, they struggle with the nonlinear dynamics of batteries.

These methods often fail to capture subtle variations in battery behavior under dynamic operating conditions, necessitating advanced approaches.

3.0.2 *AI-Based Methods for Battery State Estimation*

AI-based methods leverage machine learning and deep learning to model complex, non-linear relationships in battery data. This section reviews key approaches, datasets, and their applications in the context of the project.

3.0.2.1 *Machine Learning Techniques*

Supervised machine learning algorithms, such as Support Vector Machines (SVMs) and Random Forests, have been applied to predict SoC and SoH using features like voltage, current, and temperature. For instance, Sun et al., 2022 demonstrates SVMs achieving high accuracy in SoH estimation (98.26%) for lead-acid batteries under controlled

conditions. However, these methods require extensive feature engineering and struggle with temporal dependencies.

3.0.2.2 *Deep Learning Architectures*

Deep learning models excel at capturing temporal and spatial patterns in battery data. Key architectures include:

- **Convolutional Neural Networks (CNNs):** Extract spatial features from battery data, such as voltage profiles. Combining CNNs with Long Short-Term Memory (LSTM) units, as implemented in the «[Combined CNN-LSTM Network for State-of-Charge Estimation of Lithium-Ion Batteries](#)» 2025 paper, enhances forecasting accuracy by modeling temporal dependencies.
- **Recurrent Neural Networks (RNNs) and LSTMs:** Designed for sequential data, LSTMs are particularly effective for RUL prediction, as they capture long-term degradation trends. Studies using the NASA Battery Dataset [NASA Battery Dataset n.d.](#) report LSTM-based models outperforming traditional methods in RUL estimation as implemented in the Hong et al., 2023.
- **Transformer Models:** Emerging in battery state estimation, transformers leverage attention mechanisms to model complex dependencies, showing promise in handling variable-length sequences Yilmaz et al., 2025.

3.0.2.3 *Datasets for AI-Based Estimation*

The quality and diversity of datasets are critical for training robust AI models. Notable datasets include:

- **NASA Battery Dataset** [NASA Battery Dataset n.d.](#) Provides voltage, current, temperature, and impedance data under various operating conditions, widely used for SoC and RUL estimation due to its diversity.
- **CALCE Battery Dataset** [Battery Data / Center for Advanced Life Cycle Engineering 2025](#):
- **MATR Battery Dataset** [Experimental Data Platform \(MATR\) 2025](#):

- **HKUST Battery Dataset** Pepe, 2025:

These datasets highlight the importance of incorporating real-world operating conditions and diagnostic measurements to improve model generalizability.

3.0.2.4 *Hybrid Approaches*

Hybrid models combine physics-based and data-driven methods to enhance accuracy. For example, <empty citation> integrates ECMs with neural networks to refine SoC estimates, leveraging physical constraints to reduce training data requirements. Such approaches are particularly relevant for railway applications, where operational conditions vary widely.

3.0.3 *Challenges and Research Gaps*

Despite advancements, several challenges persist in battery state estimation:

- **Data Requirements:** AI models, particularly deep learning, require large, diverse datasets, which are often limited or proprietary .
- **Operational Variability:** Battery performance varies due to temperature, load profiles, and aging, complicating model generalization .
- **Computational Complexity:** Real-time estimation in automotive and railway systems demands low-latency models, a challenge for complex deep learning architectures.
- **Lack of Standardized Datasets:** The absence of universal, open-source datasets for railway applications limits model benchmarking.

The *BattAIHealth* project addresses these gaps by developing AI models trained on both synthetic and real-world datasets, optimizing for robustness and real-time applicability in transportation systems.

3.0.4 *Conclusion*

The state of the art in battery state estimation reveals a transition from traditional physics-based and statistical methods to AI-driven approaches. While machine learning and deep learning models, supported by datasets like the NASA Battery Dataset and Aging Dataset from EV, offer superior accuracy, challenges such as data scarcity and operational variability persist. This project builds on these advancements by developing robust AI models tailored for automotive and railway applications, aiming to enhance BMS reliability and efficiency.

DEVELOPMENT

4.1 INTRODUCTION

This chapter details the development phases of the battery health prediction system, encompassing the complete progression from initial MATLAB modeling to advanced deep learning implementation. The project evolved through distinct phases: (1) MATLAB-based modeling and simulation using traditional methods, (2) exploration of hybrid neural network approaches, (3) transition to pure data-driven models, and (4) implementation of state-of-the-art deep learning architectures for time series forecasting.

The development process was guided by the need to create accurate, robust, and scalable battery health prediction models capable of handling real-world applications. Each phase built upon lessons learned from previous approaches, ultimately leading to the implementation of TimesNet, a cutting-edge time series analysis architecture that demonstrates superior performance in battery degradation prediction tasks.

4.2 MATLAB MODELING AND SIMULATION

The initial development phase focused on implementing traditional battery modeling approaches in MATLAB to establish baseline performance and understand the fundamental characteristics of battery degradation patterns.

4.2.1 *Kalman Filter Implementation*

The Extended Kalman Filter (Extended Kalman Filter (EKF)) was implemented as the primary estimation algorithm for State of Charge (SoC) and State of Health (SoH)

prediction. The EKF approach was chosen for its proven effectiveness in handling the nonlinear dynamics of battery systems and its ability to provide uncertainty quantification.

4.2.2 *Coulomb Counting Integration*

Coulomb counting was integrated as a complementary method for SoC estimation, providing a reference baseline for comparison with the Kalman filter results. The implementation considered:

- Current integration accuracy and drift compensation
- Temperature effects on coulombic efficiency
- Aging effects on capacity estimation
- Calibration procedures for initial SoC determination

4.2.3 *Batemo Model Integration*

The Batemo battery model was incorporated to provide physics-based battery behavior simulation. This integration enabled:

- Validation of estimation algorithms under controlled conditions
- Generation of synthetic data for algorithm testing
- Analysis of model sensitivity to various degradation mechanisms
- Comparison between model-based and data-driven approaches

The MATLAB implementation served as a foundation for understanding battery dynamics and provided insights that informed subsequent neural network development phases.

4.3 NEURAL NETWORK DEVELOPMENT EVOLUTION

The neural network development process evolved through multiple iterations, each addressing specific limitations identified in previous approaches and incorporating lessons learned from the MATLAB modeling phase.

4.3.1 *Initial CNN+LSTM Architecture*

The first neural network implementation combined Convolutional Neural Network (CNN) with Long Short-Term Memory (LSTM) networks to leverage both spatial feature extraction and temporal sequence modeling capabilities.

4.3.1.1 *Architecture Design*

The CNN+LSTM architecture was structured as follows:

- **CNN layers:** Extract local patterns and features from battery measurement sequences
- **LSTM layers:** Model long-term dependencies and temporal relationships
- **Dense layers:** Final prediction mapping with appropriate activation functions

4.3.1.2 *Training Challenges and Limitations*

Several challenges were encountered during the CNN+LSTM implementation:

- **Gradient vanishing:** Long sequences caused training instability
- **Overfitting:** High model complexity led to poor generalization
- **Computational efficiency:** Training time was prohibitively long for large datasets
- **Feature engineering:** Manual feature selection proved suboptimal

4.3.2 *Hybrid vs. Data-Driven Approach Evaluation*

A systematic comparison was conducted between hybrid approaches (combining physics-based models with neural networks) and pure data-driven methods.

4.3.2.1 *Hybrid Approach Implementation*

The hybrid approach integrated:

- Physics-based model outputs as additional input features
- Kalman filter estimates as regularization terms
- Domain knowledge constraints in loss function design

4.3.2.2 *Data-Driven Approach Focus*

The pure data-driven approach emphasized:

- End-to-end learning from raw sensor data
- Automatic feature extraction and representation learning
- Minimal domain-specific preprocessing requirements

4.3.2.3 *Comparative Analysis Results*

The evaluation revealed that data-driven approaches demonstrated:

- Superior generalization across different battery chemistries
- Reduced dependency on accurate physics model parameters
- Better scalability to large datasets
- More robust performance under varying operating conditions

This analysis motivated the transition to advanced pure data-driven architectures.

4.4 DATASET COLLECTION AND PREPROCESSING

The dataset development process was crucial for training robust and generalizable models, requiring careful consideration of data quality, diversity, and preprocessing strategies.

4.4.1 *Primary Dataset Selection*

The primary dataset utilized in this work is the CALCE (Center for Advanced Life Cycle Engineering) battery dataset, obtained from the University of Maryland’s public repository. This dataset was selected for its:

- Comprehensive cycle life data spanning multiple battery chemistries
- High-quality measurements with consistent sampling rates
- Well-documented experimental conditions and procedures
- Established use in battery research community for benchmarking

4.4.2 *Data Cleaning and Preprocessing*

Several preprocessing steps were implemented to ensure data quality and model training stability:

4.4.2.1 *Cycle Removal and Filtering*

- **Initial cycle removal:** The first charge-discharge cycle was removed from each battery file to avoid initialization artifacts and inconsistent starting conditions
- **Incomplete cycle filtering:** Cycles with insufficient data points or incomplete charge/discharge sequences were excluded from the training set
- **Outlier detection:** Statistical methods were applied to identify and remove measurement outliers that could negatively impact model training

Battery-level partitioning was employed to prevent data leakage, ensuring that cycles from the same battery appeared in only one partition.

4.4.3 *Input Data Formatting*

The input data structure was designed to optimize model performance:

- **Sequence length:** Fixed-length sequences of 100 time steps were extracted from continuous battery operation data
- **Feature vector:** Each time step included voltage, current, temperature, and derived features such as power and energy
- **Target variables:** State of Health (SOH) values were calculated based on capacity fade measurements
- **Sliding window:** Overlapping sequences were generated to maximize training data utilization

4.4.4 *Limitations of Previous Approaches*

The evaluation of CNN+LSTM and hybrid approaches revealed several critical limitations:

- **Temporal modeling constraints:** Traditional LSTM architectures struggled with very long sequences typical in battery degradation analysis
- **Multi-scale pattern recognition:** Difficulty in capturing both short-term fluctuations and long-term degradation trends simultaneously
- **Computational efficiency:** High computational requirements limited the scalability to large datasets
- **Generalization issues:** Poor performance when applied to battery chemistries or operating conditions not seen during training

4.4.5 Requirements for Advanced Architecture

The identified requirements for an improved architecture included:

- **Multi-periodicity detection:** Ability to automatically identify and exploit multiple periodic patterns in battery data
- **Long-range dependency modeling:** Effective capture of dependencies across extended time horizons
- **Parameter efficiency:** Reduced model complexity while maintaining or improving performance
- **Versatility:** Capability to handle various time series analysis tasks beyond just forecasting

These requirements led to the selection and implementation of TimesNet, a cutting-edge architecture specifically designed for general time series analysis.

4.5 UTILIZED MODEL (TIMESNET)

TimesNet is a state-of-the-art neural network architecture specifically designed for general time series analysis tasks Wu et al., 2023. This model addresses the fundamental challenge of temporal variation modeling by transforming the complex problem from 1D time series analysis into 2D space analysis. The key innovation of TimesNet lies in its ability to discover multi-periodicity patterns in time series data and decompose intricate temporal variations into intraperiod and interperiod variations.

The architecture works by converting 1D time series into a set of 2D tensors based on multiple identified periods. This transformation embeds intraperiod variations into the columns and interperiod variations into the rows of the 2D tensors, making temporal patterns more accessible for analysis through 2D convolution operations. The core component, TimesBlock, can adaptively discover multi-periodicity and extract complex temporal variations using parameter-efficient inception blocks.

TimesNet demonstrates superior performance across five mainstream time series analysis tasks: short-term and long-term forecasting, imputation, classification, and anomaly

detection. This versatility makes it particularly suitable for battery health prediction tasks, where complex temporal dependencies and multi-scale patterns are crucial for accurate state-of-health estimation. The model’s ability to handle various sequence lengths and its robust architecture for capturing temporal dynamics align well with the requirements of battery degradation modeling, where both short-term fluctuations and long-term trends must be considered simultaneously.

4.5.1 *Architecture Adaptation for Battery Health Prediction*

The TimesNet architecture was adapted for battery health prediction with several key modifications:

- **Input preprocessing:** Battery measurement sequences (voltage, current, temperature) were formatted to exploit the multi-periodicity detection capabilities
- **Output configuration:** Modified for regression tasks to predict continuous SOH values rather than classification outputs
- **Loss function:** Implemented Mean Squared Error (MSE) with additional regularization terms to prevent overfitting
- **Feature engineering:** Minimal manual feature engineering to leverage the model’s automatic pattern discovery capabilities

4.6 MODEL OPTIMIZATION

For model optimization, the Optuna tool was utilized, which enables hyperparameter optimization for machine learning models, integrated with Weights & Biases (WandB), which allows for result visualization and model comparison.

4.6.1 *Dataset Preparation for Optimization*

For this test, the dataset was reduced to only 1/10 of the data, equally distributed from the original dataset, with the objective of reducing the time required for finding the best hyperparameters, since this process took approximately one week even with this reduction.

4.6.2 *Optimization Process*

For the hyperparameter search, 50 trials were performed, with 50 epochs each, using an early stopping patience of 5 epochs to avoid overfitting and accelerate the optimization process.

4.6.3 *Optimized Parameters*

The parameters that were optimized through Optuna include:

- **e_layers**: Number of encoder layers (1–3) — controls the depth of the encoder stack
- **d_layers**: Number of decoder layers (1–3) — controls the depth of the decoder stack
- **factor**: Expansion factor for the FFN (1–5) — controls the complexity of frequency components in TimesNet
- **freq**: Frequency for time features encoding (“s”, “t”, “h”) — seconds, minutes, hours
- **d_model**: Model dimension (fixed at 16)
- **top_k**: Top-k dominant frequencies in TimesNet (1–5) — controls how many frequency components to consider

4.6.4 *Parameter Importance Analysis*

Through this optimization, it was possible to detect the importance of the hyperparameters. We observed that the importance factor of the **e_layers** parameter (number of encoder layers) is the parameter that most influences the result when changed, demonstrating that the depth of the encoder architecture is critical for model performance.

4.6.5 *Best Trial Results*

The most successful trial was trial 15, which presented the following results:

- **MSE Value:** 0.0015545075293630362
- **Optimal Parameters:**
 - e_layers: 2
 - factor: 4
 - d_model: 16
 - top_k: 9
 - n_heads: 16
- **Duration:** 7770232 ms (approximately 2 hours and 10 minutes)

The results show that using 2 encoder layers works better than deeper networks, likely avoiding overfitting on the battery dataset. The high expansion factor of 4 allows the model to capture more complex patterns, while setting top_k to 9 means the model considers more frequency components than the default range, which helps capture the various periodic behaviors in battery degradation cycles.

CONCLUSIONS

A apresentação das conclusões tem como objetivo realizar uma síntese, acompanhada de um conjunto de observações acerca do que foi escrito anteriormente.

BIBLIOGRAPHY

- Akiba, Takuya et al. (2019). *Optuna: A next-generation hyperparameter optimization framework*. Pages: 2623–2631 Publication Title: Proceedings of the 25th ACM SIGKDD international conference on knowledge discovery & data mining original-date: 2018-02-21T06:12:56Z. DOI: [10 . 1145 / 3292500 . 3330701](https://doi.org/10.1145/3292500.3330701). URL: <https://github.com/optuna/optuna> (visited on 06/23/2025).
- Ansel, Jason et al. (Apr. 2024). *PyTorch 2: Faster Machine Learning Through Dynamic Python Bytecode Transformation and Graph Compilation*. Publication Title: 29th ACM International Conference on Architectural Support for Programming Languages and Operating Systems, Volume 2 (ASPLOS '24) original-date: 2016-08-13T05:26:41Z. DOI: [10 . 1145 / 3620665 . 3640366](https://doi.org/10.1145/3620665.3640366). URL: <https://docs.pytorch.org/assets/pytorch2-2.pdf> (visited on 06/23/2025).
- Battery Data | Center for Advanced Life Cycle Engineering (2025). URL: <https://calce.umd.edu/battery-data> (visited on 06/22/2025).
- biolab/orange3: :bulb: Orange: Interactive data analysis (2025). URL: <https://github.com/biolab/orange3> (visited on 06/23/2025).
- «Combined CNN-LSTM Network for State-of-Charge Estimation of Lithium-Ion Batteries» (2025). en. In: *ResearchGate* (). DOI: [10 . 1109 / ACCESS . 2019 . 2926517](https://doi.org/10.1109/ACCESS.2019.2926517). URL: https://www.researchgate.net/publication/334119055_Combined_CNN-LSTM_Network_for_State-of-Charge_Estimation_of_Lithium-Ion_Batteries (visited on 06/22/2025).
- Conda (June 2025). *conda: A system-level, binary package and environment manager running on all major operating systems and platforms*. original-date: 2012-10-15T22:08:03Z. URL: <https://github.com/conda/conda> (visited on 06/23/2025).
- Experimental Data Platform (MATR) (2025). URL: <https://data.matr.io/1/projects/5c48dd2bc625d700019f3204> (visited on 06/22/2025).
- Faconti, Davide (June 2025). *facontidavide/PlotJuggler*. original-date: 2016-03-01T21:05:42Z. URL: <https://github.com/facontidavide/PlotJuggler> (visited on 06/23/2025).
- Git (2025). URL: <https://git-scm.com/> (visited on 06/23/2025).

BIBLIOGRAPHY

- Hong, Jiangnan et al. (Nov. 2023). «State-of-health estimation of lithium-ion batteries using a novel dual-stage attention mechanism based recurrent neural network». In: *Journal of Energy Storage* 72, p. 109297. ISSN: 2352-152X. DOI: [10.1016/j.est.2023.109297](https://doi.org/10.1016/j.est.2023.109297). URL: <https://www.sciencedirect.com/science/article/pii/S2352152X23026956> (visited on 06/22/2025).
- NASA Battery Dataset (n.d.). en. URL: <https://www.kaggle.com/datasets/patrickfleith/nasa-battery-dataset> (visited on 06/22/2025).
- Pepe, Simona Pepe (2025). *HKUST lithium ion battery dataset*. DOI: [10.21227/JH1V-5435](https://doi.org/10.21227/JH1V-5435). URL: <https://iee-dataport.org/documents/hkust-lithium-ion-battery-dataset> (visited on 06/22/2025).
- Stroe, Daniel-Ioan et al. (Jan. 2018). «Degradation Behavior of Lithium-Ion Batteries During Calendar Ageing—The Case of the Internal Resistance Increase». In: *IEEE Transactions on Industry Applications* 54.1, pp. 517–525. ISSN: 1939-9367. DOI: [10.1109/TIA.2017.2756026](https://doi.org/10.1109/TIA.2017.2756026). URL: <https://ieeexplore.ieee.org/abstract/document/8048537> (visited on 06/22/2025).
- Sun, Shu et al. (Dec. 2022). «Simultaneous Estimation of SOH and SOC of Batteries Based on SVM». In: *2022 4th International Conference on Smart Power & Internet Energy Systems (SPIES)*, pp. 1934–1938. DOI: [10.1109/SPIES55999.2022.10082477](https://doi.org/10.1109/SPIES55999.2022.10082477). URL: <https://ieeexplore.ieee.org/document/10082477> (visited on 06/22/2025).
- Weights & Biases (2025). en. URL: <https://github.com/wandb> (visited on 06/23/2025).
- Wu, Haixu et al. (Apr. 2023). *TimesNet: Temporal 2D-Variation Modeling for General Time Series Analysis*. arXiv:2210.02186 [cs]. DOI: [10.48550/arXiv.2210.02186](https://doi.org/10.48550/arXiv.2210.02186). URL: <http://arxiv.org/abs/2210.02186> (visited on 04/19/2025).
- Yilmaz, Metin, Eyüp Çinar, and Ahmet Yazıcı (2025). «A Transformer-Based Model for State of Charge Estimation of Electric Vehicle Batteries». In: *IEEE Access* 13, pp. 33035–33048. ISSN: 2169-3536. DOI: [10.1109/ACCESS.2025.3542961](https://doi.org/10.1109/ACCESS.2025.3542961). URL: <https://ieeexplore.ieee.org/document/10891541> (visited on 06/22/2025).
- Zhang, D et al. (Dec. 2000). «Studies on capacity fade of lithium-ion batteries». In: *Journal of Power Sources* 91.2, pp. 122–129. ISSN: 0378-7753. DOI: [10.1016/S0378-7753\(00\)00469-9](https://doi.org/10.1016/S0378-7753(00)00469-9). URL: <https://www.sciencedirect.com/science/article/pii/S0378775300004699> (visited on 06/22/2025).

APPENDICES

APPENDIX A

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APPENDIX B

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