



Aalto University

# Stationarity of Stochastic Processes

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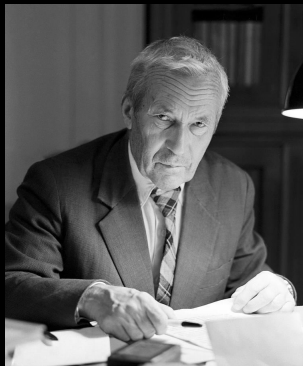
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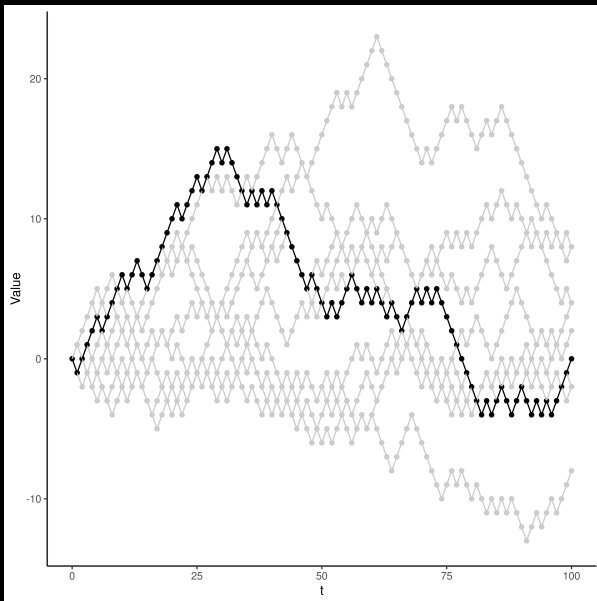
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- For a rigorous treatment of probability theory, see (Kallenberg 1997).



**Figure:** Andrey Kolmogorov (1903 - 1987)

**Stochastic Process and Time Series?**  
**(Brockwell and Davis 2009)**



**Figure:** 10 realizations of the simple random walk. Here  $t \in T = \{0, 1, \dots, 100\}$ .



**(Weak) Stationarity**

# References

- Brockwell, Peter J. and Richard A. Davis (2009). *Time Series: Theory and Methods*. Springer Science & Business Media.
- Kallenberg, Olav (1997). *Foundations of modern probability*. Vol. 2. Springer.