

PERFAIT AKAKA SHISOKA

17G01ACS059

**AUTOMATA THEORY ASSIGNMENT 3**

1.

$S \rightarrow aXbX$   
 $X \rightarrow aY \mid bY$   
 $Y \rightarrow X \mid c$

**Step 1:**

No start symbol appears on the right, so we move to step 2

**Step 2:**

It has no null productions, so we move to step 3

**Step 3:**

Remove the Unit production  $Y \rightarrow X$

$S \rightarrow aXbX$   
 $X \rightarrow aY \mid bY$   
 $Y \rightarrow aY \mid bY \mid c$

**Step 4:**

Remove productions with more than 2 variables on the right-hand side.

$S \rightarrow aXbX$

$S \rightarrow EF$   
 $X \rightarrow aY \mid bY$   
 $Y \rightarrow aY \mid bY \mid c$   
 $E \rightarrow ax$   
 $F \rightarrow bx$

**Step 5:**

Remove productions with one terminal and variable together.

$X \rightarrow ay$     $X \rightarrow by$     $Y \rightarrow aY$     $Y \rightarrow bY$     $E \rightarrow aX$     $F \rightarrow bX$

$S \rightarrow EF$   
 $X \rightarrow AY \mid BY$   
 $Y \rightarrow AY \mid BY \mid c$   
 $E \rightarrow Ax$   
 $F \rightarrow Bx$   
 $A \rightarrow a$   
 $B \rightarrow b$

2. a) Left most derivation

E  
→E \* E  
→F \* E  
→a \* E  
→a \* (E)  
→a \* (E + E)  
→a \* (F + E)  
→a \* (aF + E)  
→a \* (abF + E)  
→a \* (ab + E)  
→a \* (ab + F)  
→a \* (ab + 1F)  
→a \* (ab + 10F)  
→a \* (ab + 10)

b) Parse tree

