

# KMP-Algorithm

Finding a pattern in a text  
The idea is similar to Z-Algorithm  
Re-use “information” from previous windows.

Look for pat in text[0...]

text:	a	a	a	a	a	b	a	a	a	b	a
	0	1	2	3	4	5	6	7	8	9	10

pat:    a    a    a    a

pat found in position 0 of text!

Now, we start to look for pat in text[1...]

# KMP-Algorithm

Finding a pattern in a text  
The idea is similar to Z-Algorithm  
Re-use “information” from previous windows.

Look for pat in text[0...]

text:	a	a	a	a	a	b	a	a	a	b	a
	0	1	2	3	4	5	6	7	8	9	10

pat:    a    a    a    a

pat found in position 0 of text!

Now, we start to look for pat in text[1...]

text:	a	a	a	a	a	b	a	a	a	b	a
	0	1	2	3	4	5	6	7	8	9	10

pat:		a	a	a	a						

If we save “information” from previous iteration, we then  
already know that text[1...3] = pat[0..2]  
So we only need to **compare** text[4] = part[3]

# KMP-Algorithm

Finding a pattern in a text  
The idea is similar to Z-Algorithm  
Re-use “information” from previous windows.

Look for pat in text[0...]

text:	a	a	a	a	a	b	a	a	a	b	a
	0	1	2	3	4	5	6	7	8	9	10

pat:    a    a    a    a

pat found in position 0 of text!

Now, we start to look for pat in text[1...]

text:	a	a	a	a	a	b	a	a	a	b	a
	0	1	2	3	4	5	6	7	8	9	10

pat:		a	a	a	a						

If we save “information” from previous iteration, we then  
already know that text[1...3] = pat[0..2]  
So we only need to **compare** text[4] = part[3]

# KMP-Algorithm

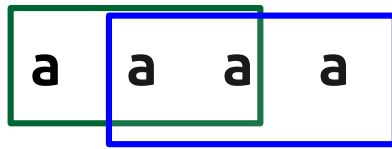
How many characters to skip?

To know this, we construct a vector `lps` of `pat.size()`

`lps[i]` = size of longest prefix of `pat[0...i]` which is also a suffix of `pat[0...i]`

pat:    a   a   a   a

`lps[3]` = longest prefix of `lps[0...3]` which is also a suffix of `pat[0...3]`



`lps[3]` = 3

# KMP-Algorithm

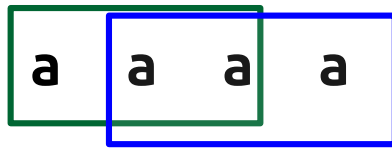
How many characters to skip?

To know this, we construct a vector `lps` of `pat.size()`

`lps[i]` = size of longest prefix of `pat[0...i]` which is also a suffix of `pat[0...i]`

pat:    a   a   a   a

`lps[3]` = longest prefix of `lps[0...3]` which is also a suffix of `pat[0...3]`



`lps[3] = 3`

i	longest prefix/suffix in <code>pat[0..i]</code>	size
0		<code>lps[0] =</code>
1		<code>lps[1] =</code>
2		<code>lps[2] =</code>
3		<code>lps[3] =</code>

# KMP-Algorithm

How many characters to skip?

To know this, we construct a vector `lps` of `pat.size()`

`lps[i]` = size of longest prefix of `pat[0...i]` which is also a suffix of `pat[0...i]`

pat:     **a**   **a**   **b**   **a**   **a**   **c**   **a**   **a**   **b**   **a**   **a**  
          0   1   2   3   4   5   6   7   8   9   10

i	longest prefix/suffix in pat[0..i]	size
0		<code>lps[0] =</code>
1		<code>lps[1] =</code>
2		<code>lps[2] =</code>
3		<code>lps[3] =</code>
...		...
8		<code>lps[8] =</code>
9		<code>lps[9] =</code>
10		<code>lps[10] =</code>

## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:								

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:    a   a   a   c   a   a   a   a  
      0   1   2   3   4   5   6   7  
lps:    0

i=1:

pat:    a   a   ..  
      0   1  
      ↑   ↑  
      len i

```
pat[i] = pat[len]
len = 1
lps[i] = 1
i++;
```

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```



## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:	0	1						

i=2:

pat:	a	a	a	..
	0	1	2	
		↑	↑	
		len	i	

```
pat[i] = pat[len]
len = 2
lps[i] = 2
i++;
```

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:	0	1	2					

i=3:

pat:	a	a	a	c	..
	0	1	2	3	
			↑	↑	
			len	i	

pat[i] != pat[len]

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:	0	1	2					

i=3:

pat:	a	a	a	c	..
	0	1	2	3	

↑    ↑

len i

pat[i] != pat[len]

len = lps[len - 1] = 1

Move back pointer "len" to the  
last character of previous  
longest/prefix suffix

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:	0	1	2					

i=3:

pat:	a	a	a	c	..
	0	1	2	3	

↑            ↑

len        i

pat[i] != pat[len]

len = lps[len - 1] = 0

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:	0	1	2	0				

i=3:

pat:	a	a	a	c	..
	0	1	2	3	

↑                    ↑

len                    i

pat[i] != pat[len] and len == 0

lps[3] = 0

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:	0	1	2	0	1			

i=4:

pat:	a	a	a	c	a	...
	0	1	2	3	4	

↑                      ↑

len                      i

```
pat[i] = pat[len]
len = 1
lps[i] = 1
i++;
```

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
Lps:	0	1	2	0	1	2		

i=5:

pat:	a	a	a	c	a	a	...
	0	1	2	3	4	5	

↑                      ↑

len                      i

```
pat[i] = pat[len]
len = 2
lps[i] = 2
i++;
```

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:	0	1	2	0	1	2	3	

i=6:

pat:	a	a	a	c	a	a	a	...
	0	1	2	3	4	5	6	

          ↑                  ↑

len                        i

```
pat[i] = pat[len]
len = 3
lps[i] = 3
i++;
```

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```



## KMP-Algorithm

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7
lps:	0	1	2	0	1	2	3	

i=7:

pat:	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7

          ↑                  ↑

          len                i

pat[i] != pat[len]

```
1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }
```

## KMP-Algorithm

pat:	<b>a</b>	<b>a</b>	<b>a</b>	<b>c</b>	<b>a</b>	<b>a</b>	<b>a</b>	<b>a</b>
	0	1	2	3	4	5	6	7
lps:	0	1	2	0	1	2	3	

i=7:

pat:

a	a	a	c	a	a	a	a
0	1	2	3	4	5	6	7

↑

len

↑

i

```
pat[i] != pat[len]
```

```
len = lps[len - 1] = 1
     = lps[ 3 - 1] = 2
```

Move back pointer "len" to the last character of previous longest/prefix suffix

```

1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }

```

19


## KMP-Algorithm

pat:	<b>a</b>	<b>a</b>	<b>a</b>	<b>c</b>	<b>a</b>	<b>a</b>	<b>a</b>	<b>a</b>
	0	1	2	3	4	5	6	7
Lps:	0	1	2	0	1	2	3	3


i=7:

pat:

	a	a	a	c	a	a	a	a
	0	1	2	3	4	5	6	7



len



i

```
pat[i] = pat[len]
len = 3
lps[i] = 3
i++;
```

```

1  std::vector<int> computeLPS(const std::string& pat)
2  {
3      std::vector<int> lps;
4      for(int i = 0; i < pat.size(); i++)
5          lps.push_back(0);
6
7      // length of longest prefix/suffix in pat
8      int len = 0;
9
10     lps[0] = 0;
11
12     int i = 1;
13
14     while( i < pat.size() )
15     {
16         if( pat[i] == pat[len] )
17         {
18             len++;
19             lps[i] = len;
20             i++;
21         }
22         else // pat[i] != pat[len]
23         {
24             if(len != 0)
25             {
26                 len = lps[len - 1];
27             }
28             else // len == 0
29             {
30                 lps[i] = 0;
31                 i++;
32             }
33         }
34     }
35
36     return lps;
37 }

```

20