

# Huffman Coding

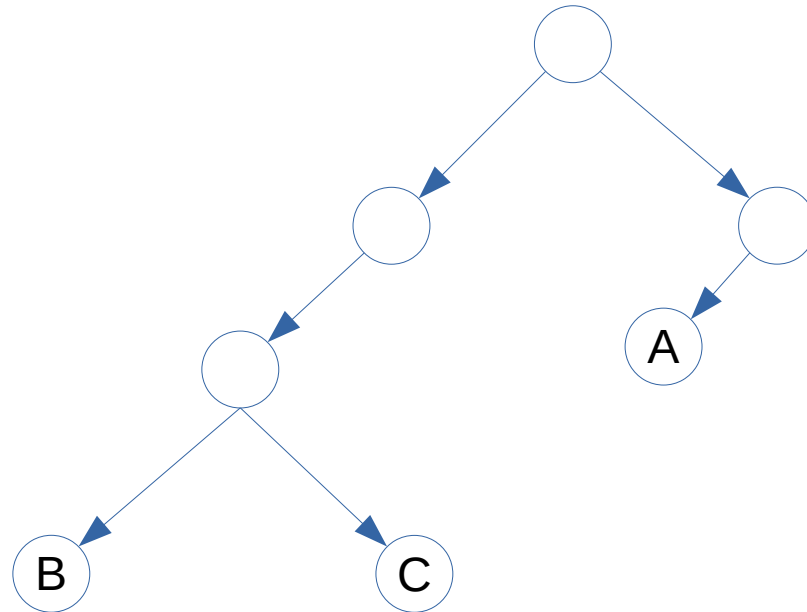
Example: Encoding for text

A B C A B

A: 10

B: 000

C: 001



encoded text => A B C A B  
10 000 001 10 000

# Huffman Coding

Create an encoding for text

A B R A C A D A B R A

# Huffman Coding

Create an encoding for text

A B R A C A D A B R A

Create a container where each element x contains a distinct letter of the text and its frequency  
(keep the contained sorted in ascendant order by the frequency)

(C,1)	(D,1)	(B,2)	(R,2)	(A,5)
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(C,1)	(D,1)	(B,2)	(R,2)	(A,5)
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While the container has more than 1 element:

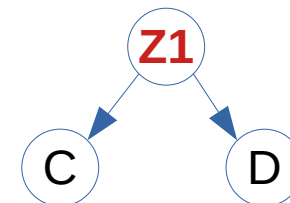
- Let  $n1$  and  $n2$  be the two elements with least frequency
- Create a tree node denoting an "intermediate" element  $Z$  that:
  - the frequency of " $Z$ " is  $n1 \rightarrow \text{freq} + n2 \rightarrow \text{freq}$
  - the left child of the node is  $n1 \rightarrow \text{letter}$
  - the right child of the node is  $n2 \rightarrow \text{letter}$
- Remove  $n1$  and  $n2$  from the container
- Insert  $Z$  in the container

(C,1)	(D,1)	(B,2)	(R,2)	(A,5)
-------	-------	-------	-------	-------

**Z1**



( <b>Z1</b> ,2)	(B,2)	(R,2)	(A,5)
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While the container has more than 1 element:

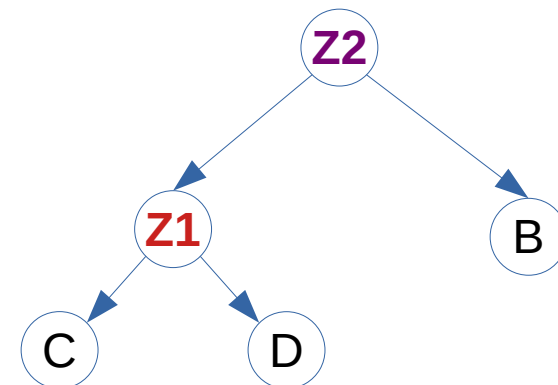
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( <b>Z1</b> ,2)	(B,2)	(R,2)	(A,5)
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**Z2**



(R,2)	( <b>Z2</b> ,4)	(A,5)
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# Huffman Coding

Create an encoding for text

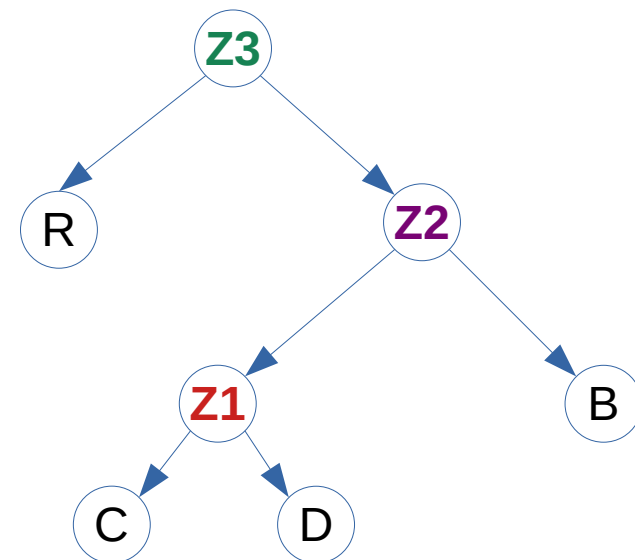
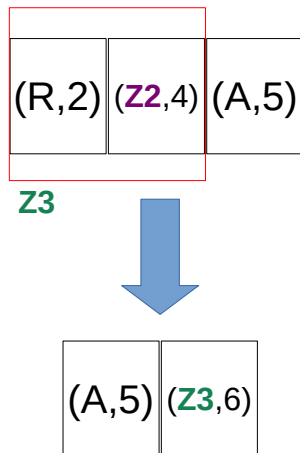
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Create a container where each element  $x$  contains a distinct letter of the text and its frequency  
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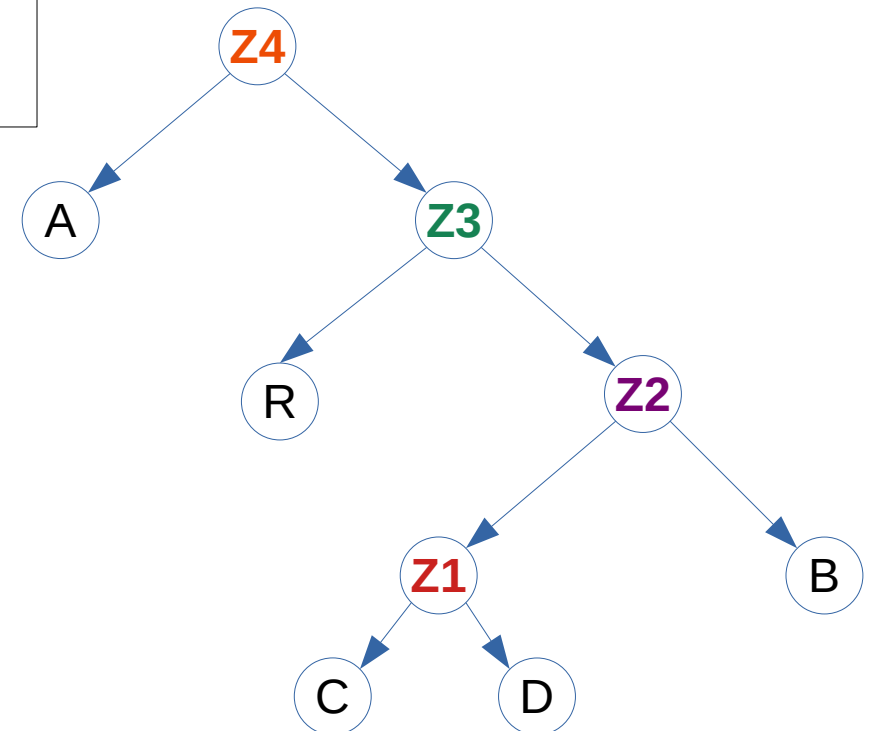
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(A,5)	(Z3,6)
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Z4



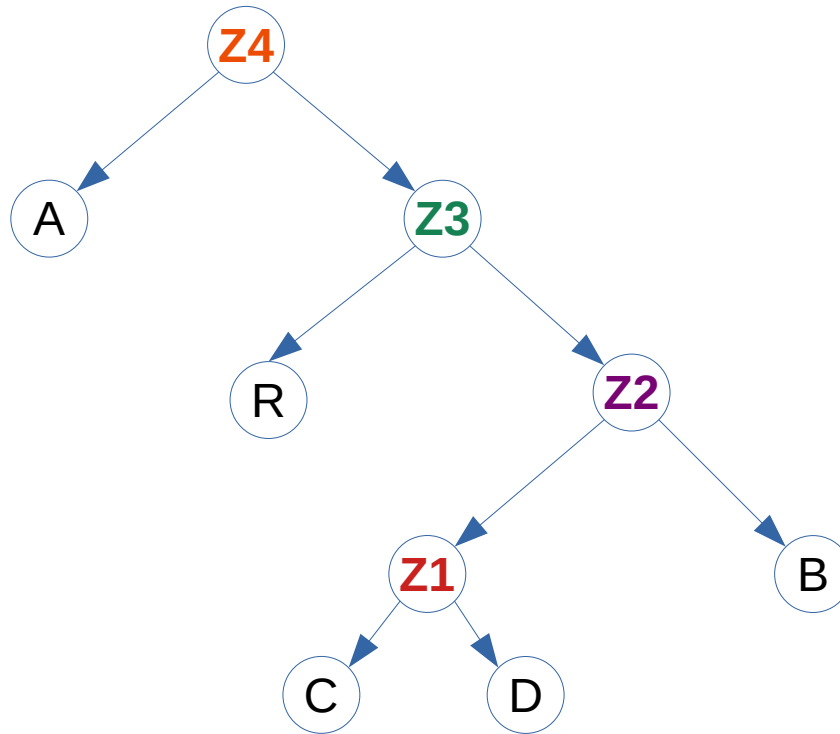
(Z4,11)
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# Huffman Coding

Create an encoding for text

A B R A C A D A B R A



A: 0  
R: 10  
B: 111  
C: 1100  
D: 1101



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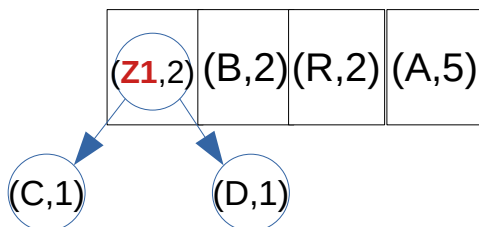
(C,1)	(D,1)	(B,2)	(R,2)	(A,5)
-------	-------	-------	-------	-------

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(C,1)	(D,1)	(B,2)	(R,2)	(A,5)
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**Z1**



**Idea:**

- Our elements in the container can be actually nodes of the tree.

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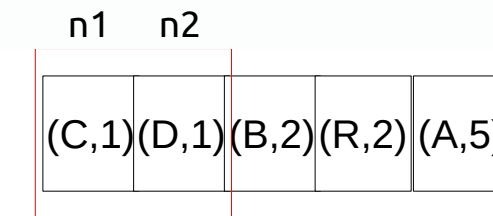
```
class HuffmanNode
{
public:
    char letter; // '\0' for non-leaf nodes
    int freq;

    HuffmanNode* leftChild;
    HuffmanNode* rightChild;

    HuffmanNode(char letter, int freq, HuffmanNode* leftChild = nullptr, HuffmanNode* rightChild = nullptr)
        : letter(letter), freq(freq), leftChild(leftChild), rightChild(rightChild) {}

    HuffmanNode(const HuffmanNode& node)
        : letter(node.letter), freq(node.freq), leftChild(node.leftChild), rightChild(node.rightChild) {}

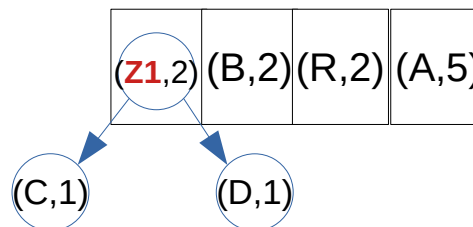
    bool operator<(const HuffmanNode& node) const
    {
        return this->freq <= node.freq;
    }
};
```



**Z1**

**Z1**

s.insert(HuffmanNode('\0', n1->freq + n2->freq, n1, n2));



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-------	-------	-------	-------	-------

```
std::multiset<HuffmanNode> s = { {'D',1}, {'C',1}, {'R',2}, {'B',2}, {'A',5} };
```