HEMT Noise Model

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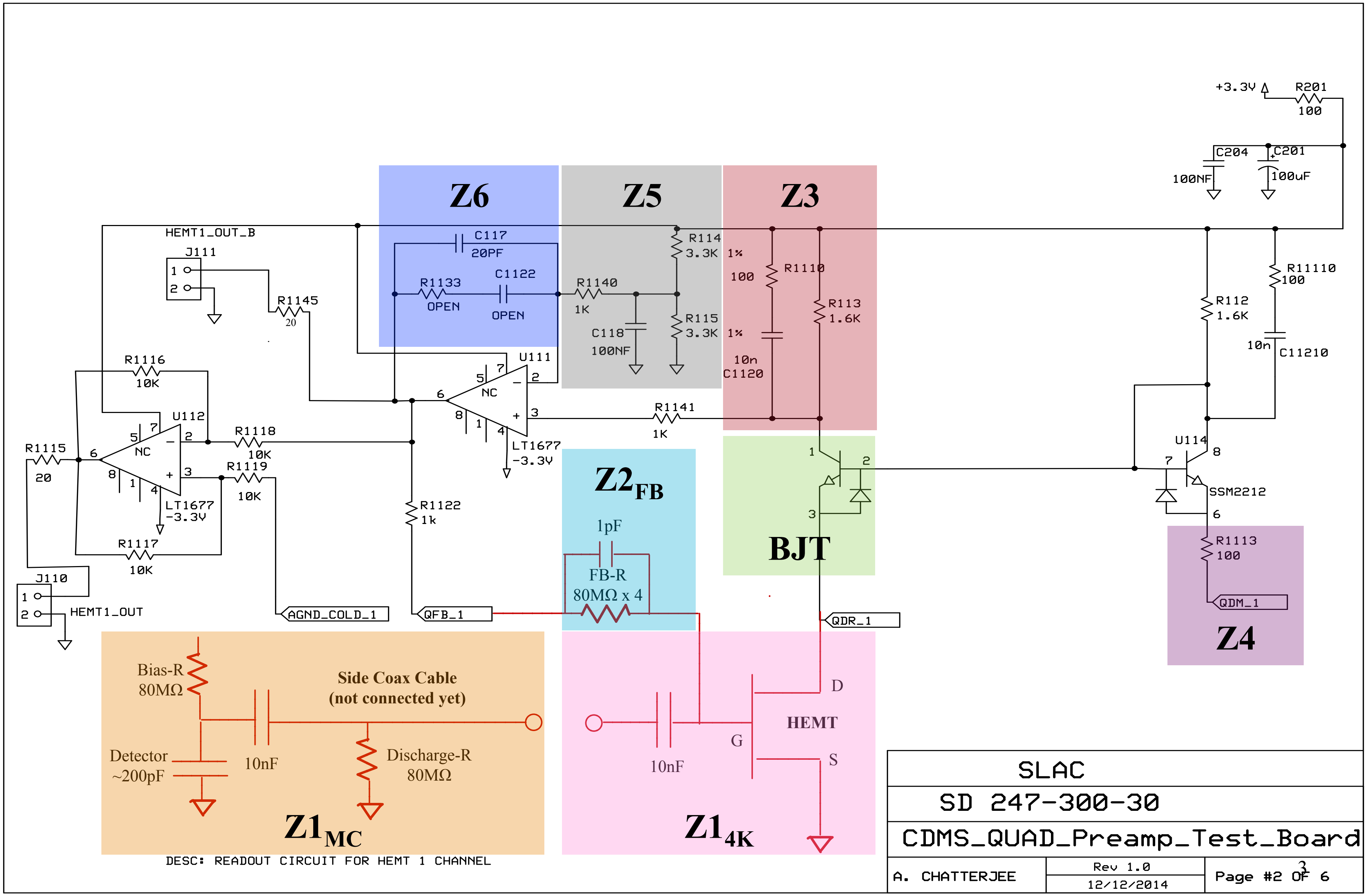
Outline

- Noise model was updated based on Gary's note
- New HEMT chips were tested with simplified setup
  - No additional board to avoid unknown stray capacitance etc.
  - V_{gs} ~ -170mV (was ~0mV) for I_d ~ 0.9mA as expected

Old (VFC#1) New (VFC#2)

Schematics



Z6
Z5
Z3
Z2FB
BJT
Z4
Z1MC
Z14K
HEMT1_OUT_B
J111
C117 20PF
R1133 OPEN
C1122 OPEN
R1140 1K
R114 3.3K 1%
R115 3.3K 1%
C118 100NF
R1110 100
C1120 10n
R113 1.6K
R1145 20
R1116 10K
U112
U111
LT1677 -3.3V
R1118 10K
R1119 10K
R1115 20
R1117 10K
R1122 1k
R1141 1K
J110
HEMT1_OUT
AGND_COLD_1
QFB_1
QDR_1
1pF
FB-R 80MΩ x 4
+3.3V
R201 100
C204 100NF
C201 100uF
R11110 100
R112 1.6K
C11210 10n
U114
SSM2212
R1113 100
QDM_1
Bias-R 80MΩ
Side Coax Cable (not connected yet)
Detector ~200pF
10nF
Discharge-R 80MΩ
HEMT
D
G
S
DESC: READOUT CIRCUIT FOR HEMT 1 CHANNEL
SLAC
SD 247-300-30
CDMS_QUAD_Preamp_Test_Board
A. CHATTERJEE
Rev 1.0
12/12/2014
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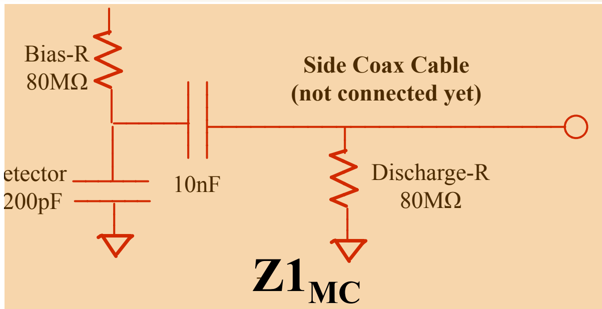
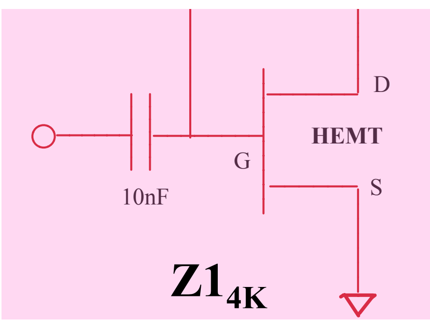
Impedance Calculation

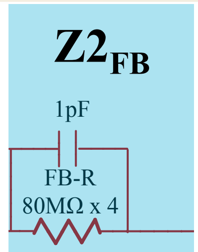


$$Z1_{MC} = \left(\left(\left(i\omega C_{det} + \frac{1}{R_{bias}} \right)^{-1} + \frac{1}{i\omega C_{cc}} \right)^{-1} + \frac{1}{R_{dis}} \right)^{-1}$$

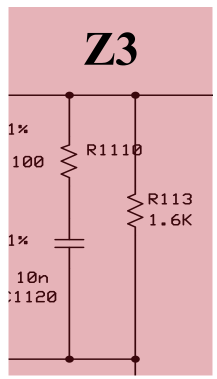


$$Z1_{4K} = \left(\left(R_{open} + \frac{1}{i\omega C_{cc}} \right)^{-1} + i\omega C_{HEMT} \right)^{-1}$$

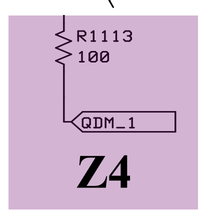
$$Z1_{total} = \left(\frac{1}{Z1_{MC}} + \frac{1}{Z1_{4K}} \right)^{-1} \qquad C_{HEMT} = 100\text{pF}$$



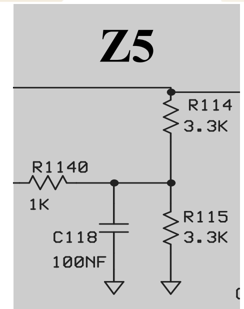
$$Z2_{FB} = \left(i\omega C_{FB} + \frac{1}{R_{FB}} \right)^{-1}$$



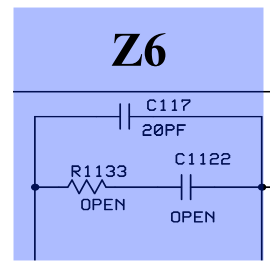
$$Z3 = \left(\frac{1}{R_{113}} + \left(R_{1110} + \frac{1}{i\omega C_{1120}} \right)^{-1} \right)^{-1}$$



$$Z4 = R_{1113}$$



$$Z5 = R_{1140} + \left(i\omega C_{118} + \frac{1}{R_{115}} + \frac{1}{R_{114}} \right)^{-1}$$

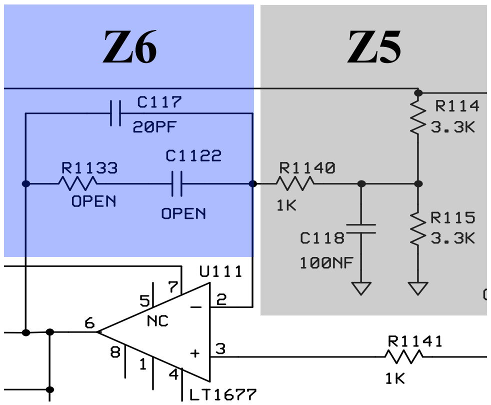


$$Z6 = \left(i\omega C_{117} + \frac{1}{R_{open}} \right)^{-1}$$

$$R_{open} \sim 10^{15}\,\Omega$$

Gain Calculation

Op-Amp gain



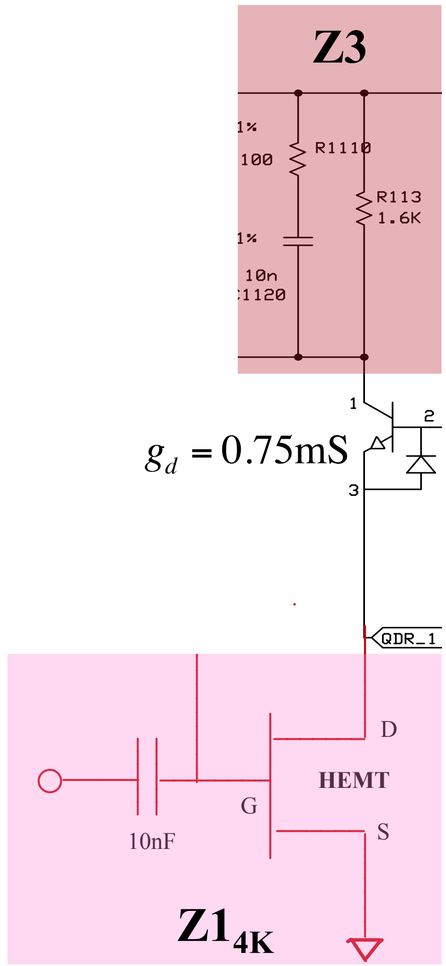
$$A = \frac{A_{open}}{1 + A_{open} B_1}$$

$$A_{open} = \frac{2 \cdot 10^7}{\left(1 + i\frac{\omega}{\omega_1}\right)\left(1 + i\frac{\omega}{\omega_2}\right)}$$

$$f_1 = 0.2\text{Hz}, \quad f_2 = 10\text{kHz}$$

$$B_1 = \frac{Z5}{Z5 + Z6}$$

HEMT gain

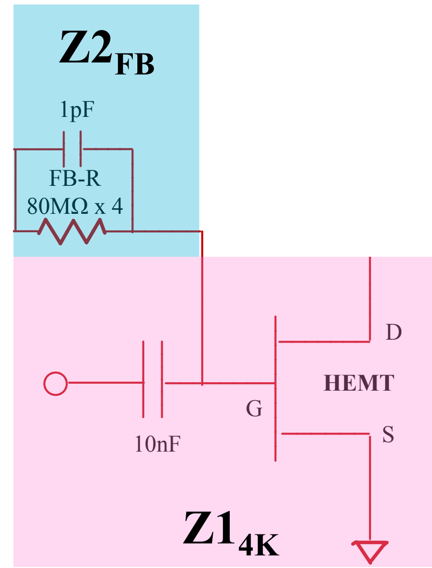


$$g_d = 0.75\text{mS}$$

$$A_{HEMT} = g_m Z3$$

$$g_m = 35\text{mS}$$

Total gain



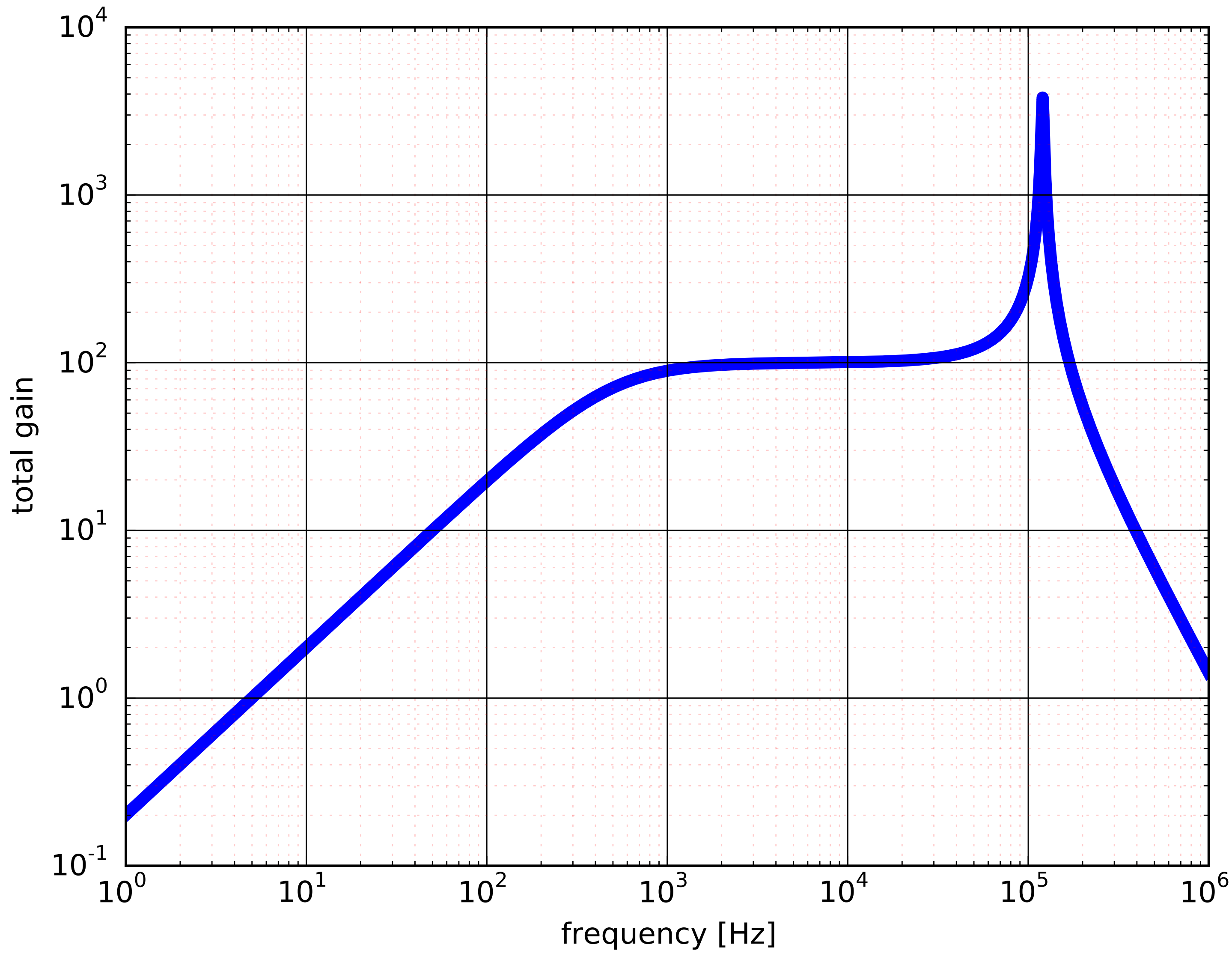
$$gain = -\frac{A_{total}\left(1 - B_2\right)}{1 + A_{total} B_2}$$

$$B_2 = \frac{Z1}{Z1 + Z2}$$

$$A_{total} = A_{HEMT} A$$

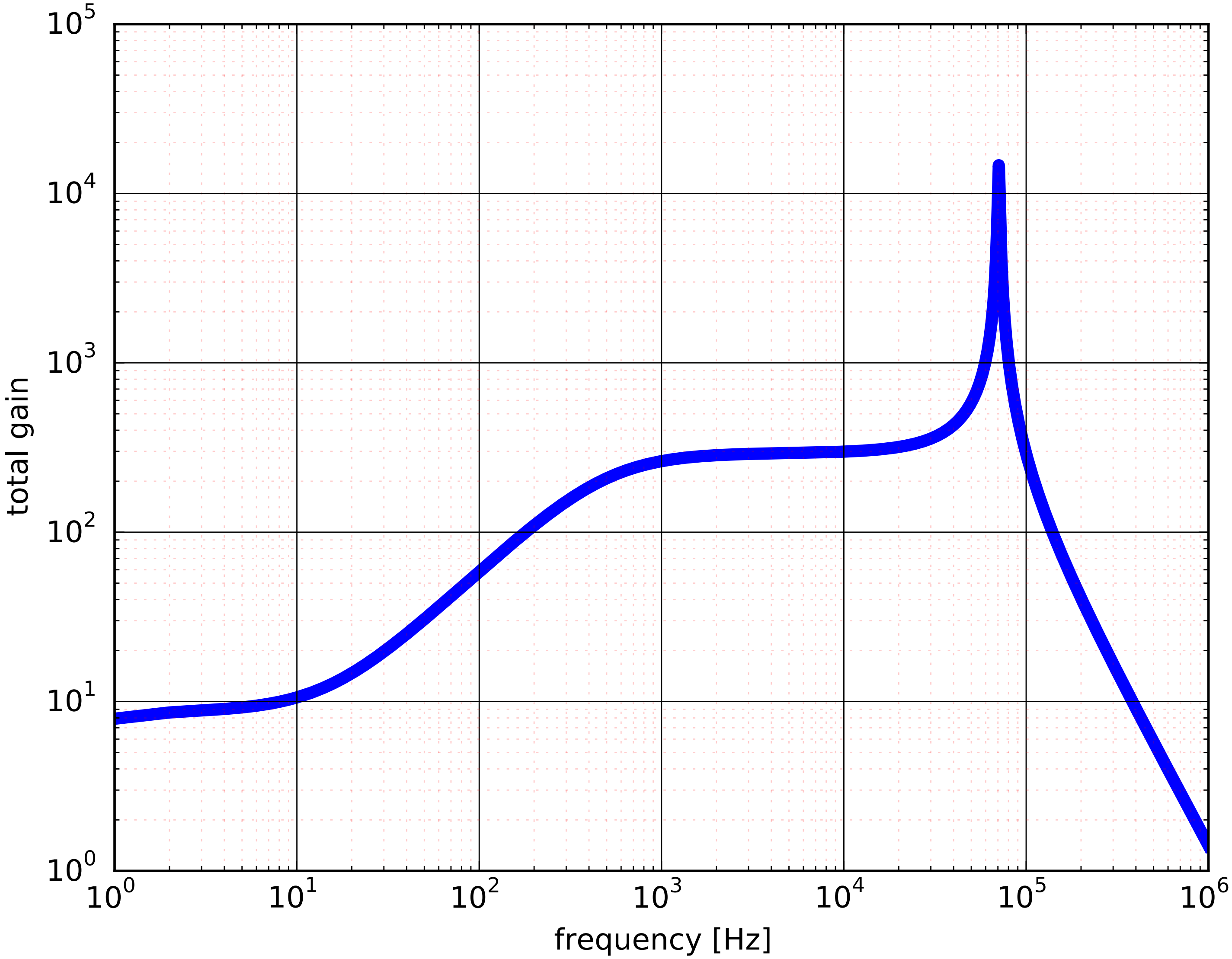
Gain vs. Frequency

No detector, discharge-R, bias-R, T_{4K} = 5.5K



Gain vs. Frequency

$C_{det} = 200pF$ $R_{dis} = 80M\Omega$, $R_{bias} = 80M\Omega$, $T_{4K} = 4K$, $T_{MC} = 30mK$



Noise Calculation (at HEMT input)

Thermal Johnson Noise at Z1

$$v_1 = \sqrt{4kT_{MC}\operatorname{Re}(Z1_{MC}) + 4kT_{4K}\operatorname{Re}(Z1_{4K})}$$

Thermal Johnson Noise at Z2_FB

$$v_2 = \frac{\sqrt{4kT_{MC}\operatorname{Re}(Z2_{FB})}}{|gain|}$$

Thermal Johnson Noise at Z3

$$v_3 = \frac{\sqrt{4kT_{MC}\operatorname{Re}(Z3)}}{|A_{HEMT}|}$$

Thermal Johnson Noise at Z4

$$v_4 = \frac{g_d}{g_m}\sqrt{4kT_{MC}\operatorname{Re}(Z4)}$$

Op-amp (LT1677) noise

$$v_{amp} = \sqrt{\left(1.8\cdot 10^{-9}\right)^2 + \left(30\cdot 10^{-9}\right)^2 \frac{2\pi}{\omega}}$$

Shot noise at BJT

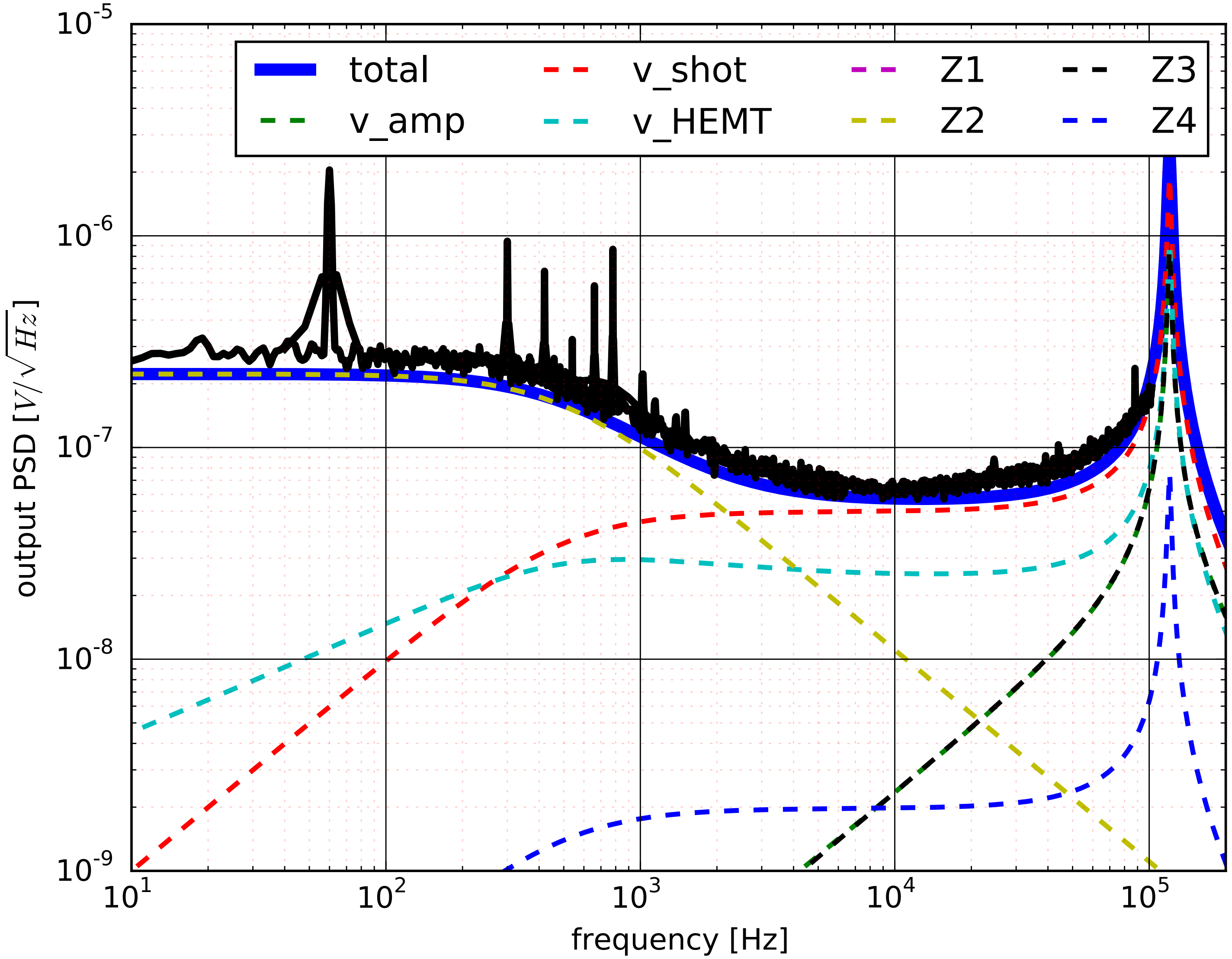
$$v_{shot} = \frac{\sqrt{2\cdot 2qI_d}}{g_m}$$

HEMT noise
(fit to Yon Jin's plot by Gary)

$$v_{HEMT} = 0.24\cdot 10^{-9}\sqrt{2\left(1+850\frac{2\pi}{\omega}\right)}$$

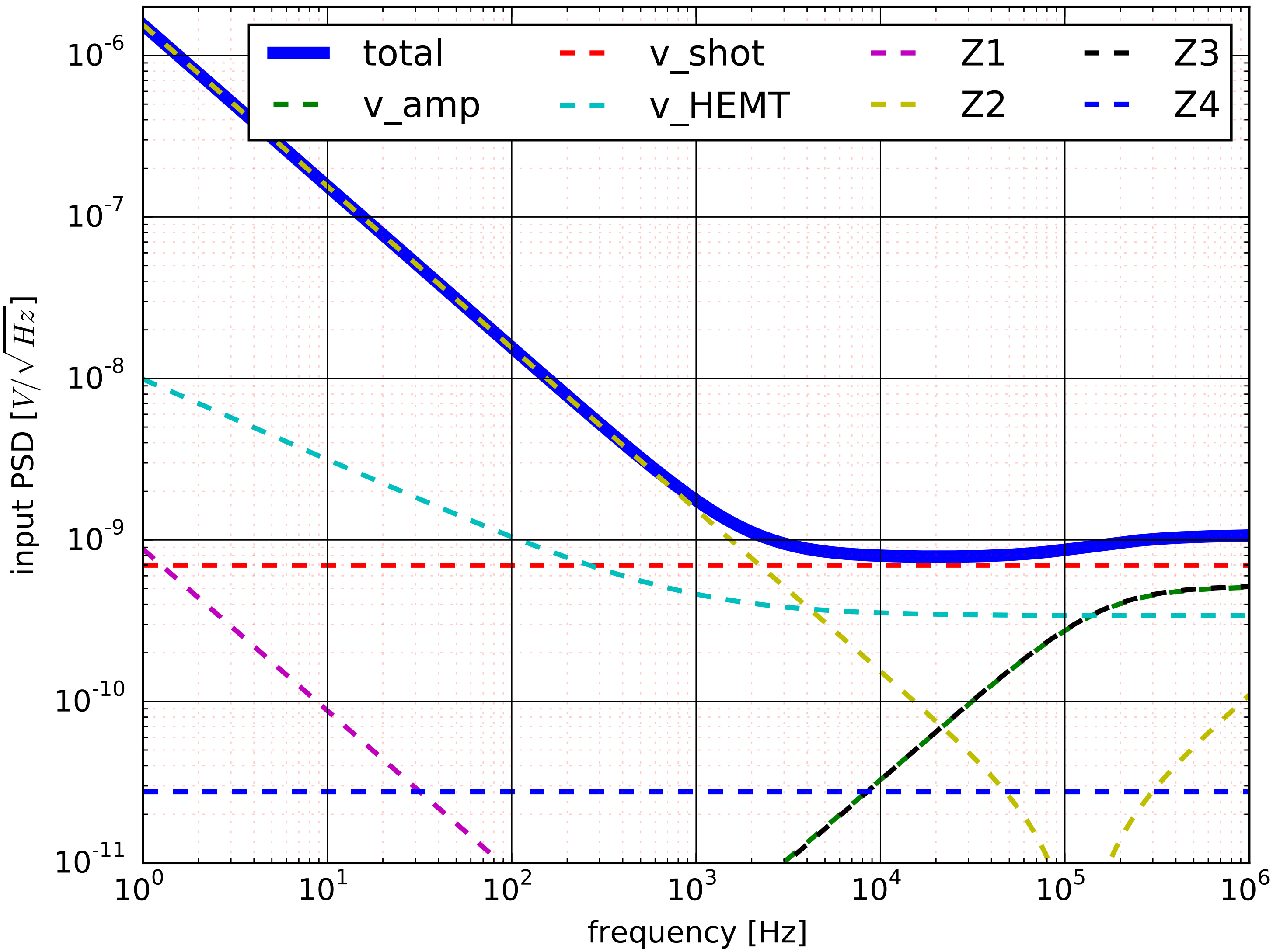
HEMT Output Noise

No detector, discharge-R, bias-R, T_{4K} = 5.5K



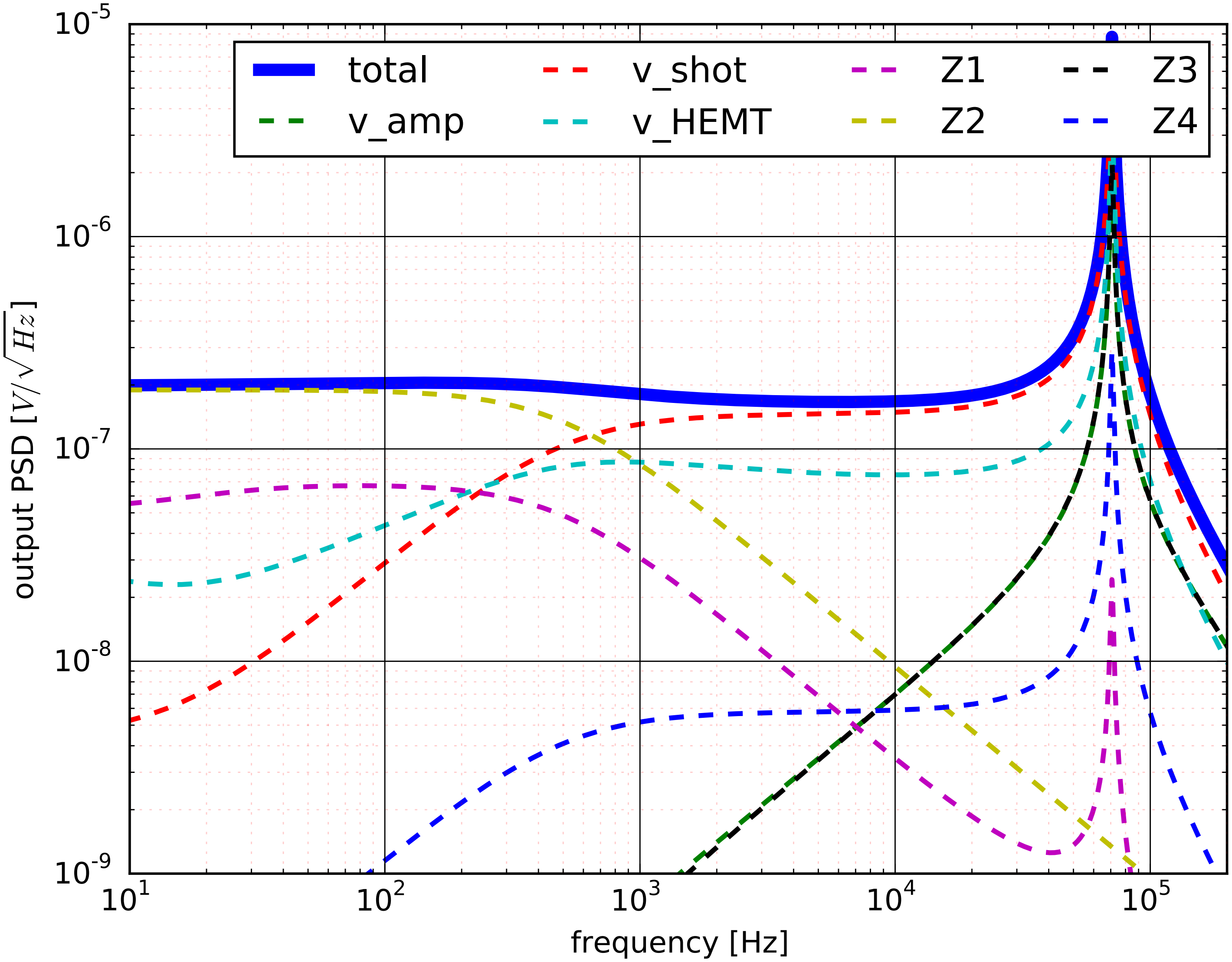
HEMT Input Noise

No detector, discharge-R, bias-R, $T_{4K} = 5.5K$



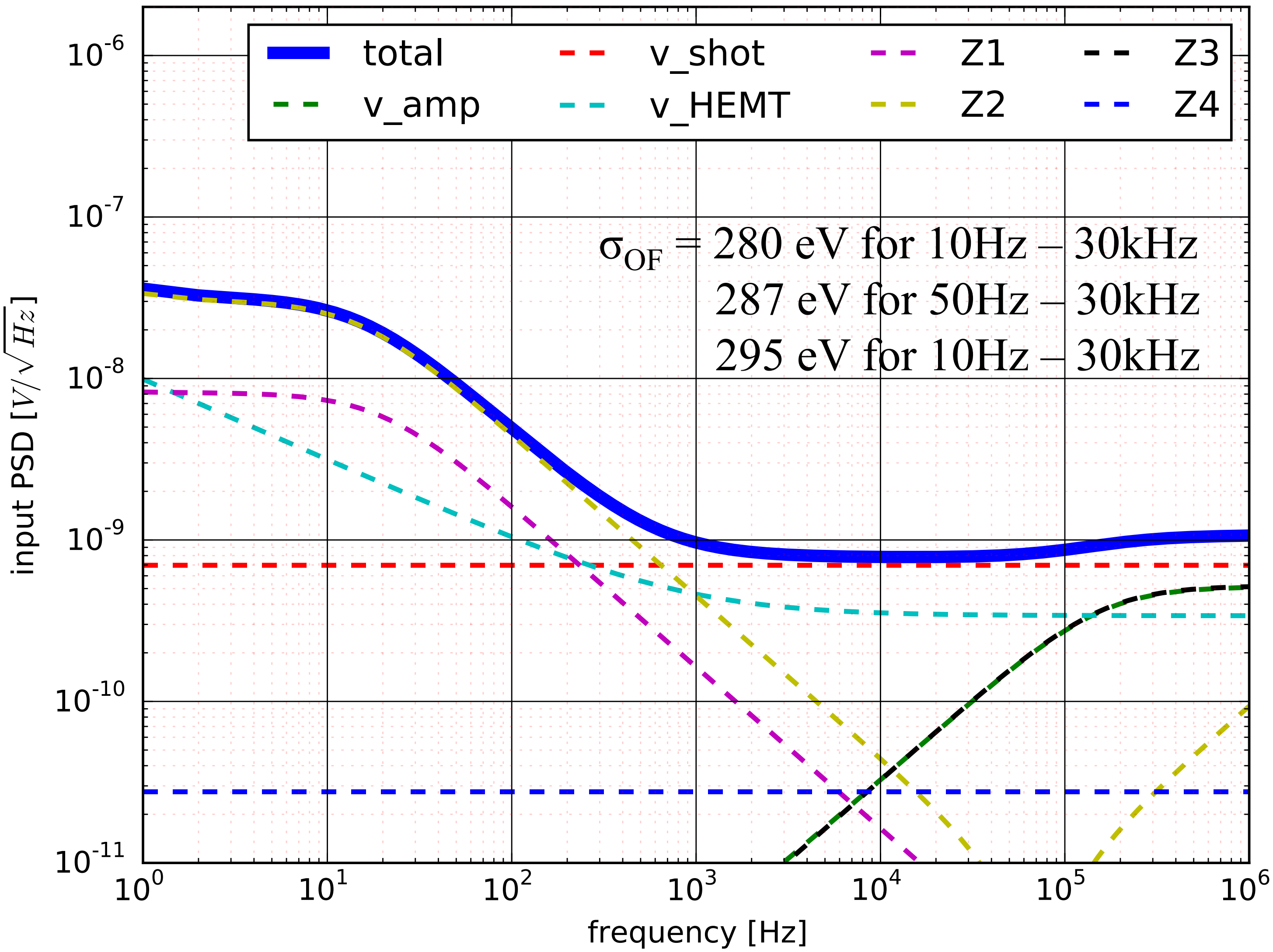
HEMT Output Noise

C_{det} = 200pF R_{dis} = 80MΩ, R_{bias} = 80MΩ, T_{4K} = 4K, T_{MC} = 30mK



HEMT Input Noise

C_{det} = 200pF R_{dis} = 80MΩ, R_{bias} = 80MΩ, T_{4K} = 4K, T_{MC} = 30mK



Summary

- With a HEMT chip (and no additional board), we obtained a consistent HEMT noise result with the calculated model.
- Future plan
  - Add more components (C_{det}, R_{dis}, R_{bias}) and compare the noise with the model
  - Measure noise with Vacuum Coax Cable
    - Vibration susceptibility test
    - Vacuum Coax Cable vs. Twisted Pair of Wires
  - Active reset test