```
?
??
Phantomization
STSCSTTS...
Phantomization Recovery Clean Up Phantomization
Phantomization Recovery Clean Up Phantomization Recovery Clean Up
Phantomization \ Phantomization
Recovery
Cleanup
R1Phantomization Phantomization Recovery
\ref{eq:control} \ref{eq:control} R1A12A rootsXreachableXroots PhantomizeRecoverQleanUpPhantomizationRecoveryRecoveryCleanUpPhantomizeRecoverCleanUp
G\alpha\alpha = \{A, B\}\alpha = \{A\}GG_AAG = G_A \cup G_BB\Gamma_B
\Gamma_B G_A \cap G_B G_A \cap G_B Recovery G_A \cap G_B A Clean Up \Gamma_B
Theorem 1 (Cycle Invariant) No strong cycles are possible, and all cycles formed in the graph should have at least one weak or p
Theorem 2 (Termination) Any mutations to a stable graph G will take O(N) time steps to form a new stable graph G', where N
PhantomizationG \\ ABGG_AG_BG_A \cap G_B
\pi_A \pi_B AB
Phantomization Phantomization \pi_B G_B G_B Phantomization O(N) N G_B
\label{eq:RecoveryGBP} \begin{split} Recovery G_B Phantomization Recovered Recovery O(N) \\ Recovery Clean Up \end{split}
Theorem 3 (Safety) Every node collected by our algorithm is indeed garbage and no nodes reachable by roots are collected.
RecoveryCleanup
V^{C}Root \xrightarrow{} \dots \xrightarrow{} V^{A} \xrightarrow{} V^{B} \xrightarrow{} \dots \xrightarrow{} V^{C}V^{A}V^{B}V^{A}V^{B}V^{B}V^{B}V^{B}V^{B}RecoveruV^{B}V^{C}
Theorem 4 (Liveness) For a graph of finite size, our algorithm eventually collects all unreachable nodes.
egin{aligned} live all \ Phantomization. Phantomization Recovery Cleanup. \end{aligned}
Phantomization Phantomization Phantomization
Softw., Pract. Exper.
SIGPLAN Not.
ECOOP
ACM Trans. Program. Lang. Syst.
ACM Trans. Program. Lang. Syst.
Functional Program Lang Languages and Computer Architecture Lecture Notes in Computer Science
Communications of the ACM
Software: Practice and Experience
Commun. ACM
Commun. ACM
Communications of the ACM
1981 ACM Symposium on Symbolic and Algebraic Computation
Garbage Collection and the Case for High-level Low- level Programming
Inf. Process. Lett.
The Computer Journal
SIGPLAN Not.
Garbage collection: algorithms for automatic dynamic memory management
ACM Trans. Program. Lang. Syst.
Inf. Process. Lett.
Inj. Frocess. Lew.
Inf. Process. Lett.
Inf. Process. Lett.
Commun. ACM
ACM
Commun. Acm
Commun. Alagory
A Cyclic Reference Counting Algorithm and Its Proof
```

 $\begin{array}{l} SIGPLAN\ Not. \\ SIGPLAN\ Not. \\ ISMM \\ IPDPS \\ Comparative\ Performance\ Evaluation\ of\ Garbage\ Collection\ Algorithms \end{array}$