

$$\text{In}[1]:= \text{ellipticlowpass} = \left(A + B * \left(\frac{W1^2}{s^2 + \frac{W1}{C} * s + W1^2} \right) \right) * \left(\frac{W2}{s + W2} \right)$$

$$\text{Out}[1]= \frac{\left(A + \frac{B W1^2}{s^2 + \frac{W1}{C} + W1^2} \right) W2}{s + W2}$$

$$\text{In}[2]:= \text{Together}[\text{ExpandAll}[\%]]$$

$$\text{Out}[2]= \frac{A C s^2 W2 + A s W1 W2 + A C W1^2 W2 + B C W1^2 W2}{(C s^2 + s W1 + C W1^2) (s + W2)}$$

$$\text{In}[3]:= \text{Expand}[\text{Numerator}[\%]]$$

$$\text{Out}[3]= A C s^2 W2 + A s W1 W2 + A C W1^2 W2 + B C W1^2 W2$$

$$\text{In}[4]:= \text{Expand}[\text{Denominator}[\%2]]$$

$$\text{Out}[4]= C s^3 + s^2 W1 + C s W1^2 + C s^2 W2 + s W1 W2 + C W1^2 W2$$

$$\text{In}[5]:= \text{Collect}[\text{Expand}[\%3 / C], s]$$

$$\text{Out}[5]= A s^2 W2 + \frac{A s W1 W2}{C} + A W1^2 W2 + B W1^2 W2$$

$$\text{In}[6]:= \text{Collect}[\text{Expand}[\%4 / C], s]$$

$$\text{Out}[6]= s^3 + W1^2 W2 + s^2 \left(\frac{W1}{C} + W2 \right) + s \left(W1^2 + \frac{W1 W2}{C} \right)$$

$$\text{In}[7]:= \text{sdomain} = \%5 / \%6$$

$$\text{Out}[7]= \frac{A s^2 W2 + \frac{A s W1 W2}{C} + A W1^2 W2 + B W1^2 W2}{s^3 + W1^2 W2 + s^2 \left(\frac{W1}{C} + W2 \right) + s \left(W1^2 + \frac{W1 W2}{C} \right)}$$

$$\text{In}[8]:= s = P \frac{z - 1}{z + 1}$$

$$\text{Out}[8]= \frac{P (-1 + z)}{1 + z}$$

$$\text{In}[9]:= \text{sdomain}$$

$$\text{Out}[9]= \frac{A W1^2 W2 + B W1^2 W2 + \frac{A P^2 W2 (-1+z)^2}{(1+z)^2} + \frac{A P W1 W2 (-1+z)}{C (1+z)}}{W1^2 W2 + \frac{P^3 (-1+z)^3}{(1+z)^3} + \frac{P^2 \left(\frac{W1}{C} + W2 \right) (-1+z)^2}{(1+z)^2} + \frac{P \left(W1^2 + \frac{W1 W2}{C} \right) (-1+z)}{1+z}}$$

$$\text{In}[10]:= \text{Together}[\text{ExpandAll}[\%]]$$

$$\text{Out}[10]= (A C P^2 W2 - A P W1 W2 + A C W1^2 W2 + B C W1^2 W2 - A C P^2 W2 z - A P W1 W2 z + 3 A C W1^2 W2 z + 3 B C W1^2 W2 z - A C P^2 W2 z^2 + A P W1 W2 z^2 + 3 A C W1^2 W2 z^2 + 3 B C W1^2 W2 z^2 + A C P^2 W2 z^3 + A P W1 W2 z^3 + A C W1^2 W2 z^3 + B C W1^2 W2 z^3) / ((-P + W2 + P z + W2 z) (C P^2 - P W1 + C W1^2 - 2 C P^2 z + 2 C W1^2 z + C P^2 z^2 + P W1 z^2 + C W1^2 z^2))$$

$$\text{In}[11]:= \text{Collect}[\text{Numerator}[\%10], z]$$

$$\text{Out}[11]= A C P^2 W2 - A P W1 W2 + A C W1^2 W2 + B C W1^2 W2 + (-A C P^2 W2 - A P W1 W2 + 3 A C W1^2 W2 + 3 B C W1^2 W2) z + (-A C P^2 W2 + A P W1 W2 + 3 A C W1^2 W2 + 3 B C W1^2 W2) z^2 + (A C P^2 W2 + A P W1 W2 + A C W1^2 W2 + B C W1^2 W2) z^3$$

In[12]:= **Collect**[**Denominator**[%10], z]

Out[12]=
$$\begin{aligned} & -C P^3 + P^2 W1 - C P W1^2 + C P^2 W2 - P W1 W2 + C W1^2 W2 + \\ & (3 C P^3 - P^2 W1 - C P W1^2 - C P^2 W2 - P W1 W2 + 3 C W1^2 W2) z + \\ & (-3 C P^3 - P^2 W1 + C P W1^2 - C P^2 W2 + P W1 W2 + 3 C W1^2 W2) z^2 + \\ & (C P^3 + P^2 W1 + C P W1^2 + C P^2 W2 + P W1 W2 + C W1^2 W2) z^3 \end{aligned}$$

In[13]:= **Collect**[%11 / (C P³ + P² W1 + C P W1² + C P² W2 + P W1 W2 + C W1² W2), z]

Out[13]=
$$\begin{aligned} & \frac{A C P^2 W2 - A P W1 W2 + A C W1^2 W2 + B C W1^2 W2}{C P^3 + P^2 W1 + C P W1^2 + C P^2 W2 + P W1 W2 + C W1^2 W2} + \\ & \frac{(-A C P^2 W2 - A P W1 W2 + 3 A C W1^2 W2 + 3 B C W1^2 W2) z}{C P^3 + P^2 W1 + C P W1^2 + C P^2 W2 + P W1 W2 + C W1^2 W2} + \\ & \frac{(-A C P^2 W2 + A P W1 W2 + 3 A C W1^2 W2 + 3 B C W1^2 W2) z^2}{C P^3 + P^2 W1 + C P W1^2 + C P^2 W2 + P W1 W2 + C W1^2 W2} + \\ & \frac{(A C P^2 W2 + A P W1 W2 + A C W1^2 W2 + B C W1^2 W2) z^3}{C P^3 + P^2 W1 + C P W1^2 + C P^2 W2 + P W1 W2 + C W1^2 W2} \end{aligned}$$

In[14]:= **Collect**[%12 / (C P³ + P² W1 + C P W1² + C P² W2 + P W1 W2 + C W1² W2), z]

Out[14]=
$$\begin{aligned} & \frac{-C P^3 + P^2 W1 - C P W1^2 + C P^2 W2 - P W1 W2 + C W1^2 W2}{C P^3 + P^2 W1 + C P W1^2 + C P^2 W2 + P W1 W2 + C W1^2 W2} + \\ & \frac{(3 C P^3 - P^2 W1 - C P W1^2 - C P^2 W2 - P W1 W2 + 3 C W1^2 W2) z}{C P^3 + P^2 W1 + C P W1^2 + C P^2 W2 + P W1 W2 + C W1^2 W2} + \\ & \frac{(-3 C P^3 - P^2 W1 + C P W1^2 - C P^2 W2 + P W1 W2 + 3 C W1^2 W2) z^2}{C P^3 + P^2 W1 + C P W1^2 + C P^2 W2 + P W1 W2 + C W1^2 W2} + z^3 \end{aligned}$$