

# 1. Study of associated production of vector bosons and b-jets in pp collisions at the LHC <sup>1</sup>

## 1.1 Introduction

The vector boson production in association with one and two b jets at the CERN Large Hadron Collider is important for many different experimental and theoretical reasons. Bottom quarks have a peculiar signature which allows one to easily identify them thanks to a displaced decay vertex. The associated production with vector bosons is an important background to VH production with the Higgs boson decaying to b quarks, and many new physics searches. Theoretically, it offers an interesting testing ground for predictions involving heavy quarks.

There are two possible options for the calculation of processes with b-quarks in the final state at hadron colliders. In the four-flavour scheme (4F) b-quarks are not present in the parton density of the incident protons. They can only be generated in the final state and they are usually massive. In the five-flavour scheme (5F) the b-quark mass is considered small with respect to the scale of the process  $Q$  and powers of logarithms of the type  $\log \frac{Q^2}{m_b^2}$  are resummed into a b parton density function. The b-quark is therefore massless in this approach, though higher order mass effects can be included in the calculation. A critical review of the different flavour number schemes and of the status of theoretical calculations is available in Ref. [1]. The two approaches give identical results to all orders in perturbation theory, but for mass terms which are power suppressed. At finite order, however, they can give very different results. In the 4F scheme the computation is more complicated, but the full kinematics of the heavy quarks is taken into account. Furthermore it can be easily interfaced to parton showers, even at NLO using the MC@NLO [2] or the POWHEG [3] formalisms. On the other hand logarithms in the initial state are not resummed and could lead to large discrepancies in the inclusive quantities like the total cross-section. In the 5F approach, on the opposite, calculations for the inclusive quantities are highly simplified and generally more accurate, but differential distributions and exclusive observables are technically more involved.

The goal of this study is to compare the most recent measurements with the predictions of the state of the art generators using 4F and 5F scheme. The report is organised as follows. In Section 1.2 we provide a short description of the ATLAS and CMS measurements, available in the Rivet framework, for  $V + b + X$  and  $V + b\bar{b} + X$ , where  $V$  is a  $Z$  or a  $W$  boson. In Section 1.3 we describe the generator setups used to obtain the predictions, which are compared to the measurements in Section 1.4 for the  $Z$  and 1.5 for the  $W$ , before conclusions are drawn in Section 1.6.

## 1.2 Rivet Routines

Results in this study were produced using three Rivet routines to compare to published ATLAS and CMS data.

- Measurement of differential production cross-sections for a  $Z$  boson in association with b-jets in proton-proton collisions at  $\sqrt{s} = 7$  TeV with the ATLAS detector [4] (Rivet routine ATLAS\_2014\_I1306294). A pair of opposite sign charge dressed leptons<sup>2</sup> (i.e. electrons or muons) with  $p_T > 20$  GeV and  $|\eta| < 2.5$  are required, with a dilepton mass between 76 and 106 GeV. Anti- $k_t$  0.4 jets are reconstructed from all final state particles, and required to have  $p_T > 20$  GeV,  $|y| < 2.4$  and not overlap with the leptons used to make the  $Z$  candidate ( $\Delta R(jet, l) > 0.5$ ). Jets are labelled as b-jets based on matching with  $\Delta R < 0.3$  to a weakly decaying b-hadron with  $p_T > 5$  GeV.

Distributions include the  $p_T$  and rapidity of b-jets and of the  $Z$ -boson, and for each b-jet, the  $y_{boost}$  of the b-jet and  $Z$ . For events with  $Z p_T > 20$  GeV, the  $\Delta R$ ,  $\Delta\phi$ , and  $\Delta y$  between the  $Z$  and all

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<sup>1</sup>Contributing authors: M. Bell, J. Butterworth, V. Ciulli, G. Hesketh, F. Krauss, G. Luisoni, G. Nail, D. Napoletano, C. Oleari, S. Platzer, C. Reuschle, B. Waugh, ...

<sup>2</sup>Leptons are dressed by adding the four-vectors of all photons within  $\Delta R < 0.1$  to the lepton 4-vector

$b$ -jets are plotted. For events with at least two  $b$ -jets, the  $\Delta R$  and di- $b$ -jet mass for the two leading  $b$ -jets, along with the  $Z$   $p_T$  and rapidity are plotted.

For this study, further distributions were added: the  $p_T$  of all weakly decaying  $b$  hadrons with  $|y| < 2.7$ , and the  $p_T$  of the subset of those that are matched to a jet. For  $b$ -jets, the number of matching  $b$ -hadrons, and the jet  $p_T$  for jets with one or two matching  $b$ -hadrons are plotted, all with and without the 5 GeV requirement on  $b$ -hadron  $p_T$ . Finally the ratio of the number of jets matching one to those matching two  $b$ -hadrons is plotted as a function of jet  $p_T$ . All of these additional distributions are also formed using  $b$ -quarks instead of  $b$ -hadrons.

- Cross-section and angular correlations in  $Z$  boson with  $b$ -hadrons events at  $\sqrt{s} = 7$  TeV [5] (Rivet routine CMS\_2013\_i1256943). A pair of opposite sign charge dressed lepton with  $p_T > 20$  GeV and  $|\eta| < 2.4$  are required, with dilepton mass between 81 and 101 GeV. Exactly two weakly decaying  $b$ -hadrons with  $p_T > 15$  GeV and  $|\eta| < 2$  are then required.

Distributions include the  $Z$   $p_T$ , the  $\Delta R$  and  $\Delta\phi$  between  $b$ -hadrons,  $\Delta R$  between the  $Z$  and closest  $b$ -hadron, and the asymmetry of the  $\Delta R$  between the  $Z$  and closest  $b$ -hadron, and the  $Z$  and the furthest  $b$ -hadron. The angular distributions are repeated with a requirement of  $Z$   $p_T > 50$  GeV.

- Measurement of the cross-section for  $W$  boson production in association with  $b$ -jets in pp collisions at  $\sqrt{s} = 7$  TeV with the ATLAS detector [6] (Rivet routine ATLAS\_2013\_I1219109). A dressed lepton with  $p_T > 25$  GeV and  $|\eta| < 2.5$  and a same-flavour neutrino with  $p_T > 25$  GeV are used to form a  $W$  candidate, which is required to have a transverse mass greater than 60 GeV. Anti- $k_t$  0.4 jets are reconstructed from all final state particles, and required to have  $p_T > 25$  GeV,  $|y| < 2.1$  and not overlap with the charged lepton used to make the  $W$  candidate ( $\Delta R(jet, l) > 0.5$ ). Events with more than two selected jets are vetoed, and the at least one of the selected jets is required to be labelled as  $b$ -jet, based on matching with  $\Delta R < 0.3$  to a weakly decaying  $b$ -hadron with  $p_T > 5$  GeV.

Distributions include the number of  $b$ -jets, and the  $b$ -jet  $p_T$  in events containing exactly one or two selected jets. The same additional distributions for the  $Z$  analysis are also added to this analysis.

### 1.3 Event generators

#### 1.3.1 SHERPA

In this section we present the setups that are used in this study for the SHERPA event generator [7]. In particular we consider three different classes of samples: 4F MC@NLO, 5F MEPS and a 5F MEPS@NLO one.

**4F MC@NLO:** This first set of results is obtained in the four-flavour scheme, and based on the MC@NLO technique [2], as implemented in SHERPA [8]. In a four-flavour scheme calculation,  $b$ -quarks can only be produced as final state massive particles. They are, therefore, completely decoupled from the evolution of the strong coupling,  $\alpha_S$  and that of the PDFs. In this scheme the associated production at tree-level starts from processes such as  $jj \rightarrow b\bar{b}Z$  where  $j$  can be either a light quark or a gluon. No specific cuts are applied on the  $b$ -quarks, their finite mass regulates collinear divergences that would appear in the massless case. In most cases, therefore, a  $b$ -jet actually originates from the parton shower evolution and hadronization of a  $b$ -quark produced by the matrix element.

**5F MEPS:** In a 5F scheme  $b$ -quarks are treated as massless partons. Collinear logs are resummed into a  $b$ -PDF and they can appear as initial state particles as well as final state ones. In order to account for 0 and 1  $b$ -jets bins as well as to cure the collinear singularity that would arise with a massless final state parton, we use multi-jet merging. In SHERPA, the well-established mechanism for combining into one inclusive sample towers of matrix elements with increasing jet multiplicity at tree-level is the CKKW [9]. For this sample we merge together LO samples of  $jj \rightarrow Z$ ,  $jj \rightarrow Z + j$ ,  $jj \rightarrow Z + jj$ ,  $jj \rightarrow Z + jjj$  where now  $j$  can be a light quark, a  $b$ -quark or a gluon, and all these samples are further matched to the SHERPA parton shower CSS [10]. Merging rests on a jet-criterion, applied to the matrix elements. As a result, jets are being produced by the fixed-order

matrix elements and further evolved by the parton shower. As a consequence, the jet criterion separating the two regimes is typically chosen such that the jets produced by the shower are softer than the jets entering the analysis. This is realised here by a cut-off of  $\mu_{\text{jet}} = 10$  GeV.

5F MEPS@NLO: In this scheme we use the extension to next-to leading order matrix elements, in a technique dubbed MEPS@NLO [11]. In particular, we merge  $jj \rightarrow Z$ ,  $jj \rightarrow Z + j$ ,  $jj \rightarrow Z + jj$  calculated with NLO accuracy and we further merge this sample with  $jj \rightarrow Z + jjj$  at the LO. As in the previous case matching criterion has to be chosen, and this is realised by a cut-off of  $\mu_{\text{jet}} = 10$  GeV.

In SHERPA, tree-level cross sections are provided by two matrix element generators, AMEGIC++ [12] and COMIX [13], which also implement the automated infrared subtraction [14] through the Catani–Seymour scheme [15, 16]. For parton showering, the implementation of [10] is employed with the difference that for  $g \rightarrow b\bar{b}$  splittings the invariant mass of the  $b\bar{b}$  pair, instead of their transverse momentum, is being used as scale. NLO matrix elements are instead obtained from OPENLOOPS [17, 18].

### 1.32 HERWIG7

In this section we present the setup for those results obtained with the HERWIG7 event generator [19, 20].

Based on extensions of the previously developed MATCHBOX module [21], HERWIG7 facilitates the automated setup of all ingredients necessary for a full NLO QCD calculation in the subtraction formalism: an implementation of the Catani–Seymour dipole subtraction method [15, 16], as well as interfaces to a list of external matrix-element providers – either at the level of squared matrix elements, based on extensions of the BLHA standard [22, 23, 24], or at the level of color-ordered subamplitudes, where the color bases are provided by an interface to the COLORFULL [25] and CVOLVER [26] libraries.

For this study the relevant tree-level matrix elements are taken from MADGRAPH5\_aMC@NLO [27, 28] (via a matrix-element interface at the level of color-ordered subamplitudes), whereas the relevant tree-level/one-loop interference terms are provided by OPENLOOPS [17, 18] (at the level of squared matrix elements).

Fully automated NLO matching algorithms are available, henceforth referred to as subtractive ( $NLO\oplus$ ) and multiplicative ( $NLO\otimes$ ) matching – based on the MC@NLO [2] and POWHEG [3] formalism respectively – for the systematic and consistent combination of NLO QCD calculations with both shower variants (the angular-ordered *QTilde* shower [29] and the *Dipole* shower [30]) in HERWIG7.

We consider four different classes of samples, for varying combinations of matching and shower algorithms (a selection of plots can be found in sections 1.42 and 1.5):

- 4F, Zbb For this set we consider the subtractive and multiplicative matching together with the *QTilde* shower. The tree-level process of the underlying hard sub-process in this case is  $pp \rightarrow Zb\bar{b} \rightarrow e^+e^-b\bar{b}$ . For this sample the  $b$  quark is considered massive and  $p$  only consist of light quarks or a gluon, not a  $b$  quark.
- 5F, Zbb For this set we consider the subtractive and multiplicative matching together with the *QTilde* and *Dipole* shower. The tree-level process of the underlying hard sub-process in this case is  $pp \rightarrow Zb\bar{b} \rightarrow e^+e^-b\bar{b}$ . For this sample the  $b$  quark is treated as massless, and  $p$  may also include a  $b$  quark. Generator-level cuts on the  $b$  quarks have thus been applied. Only in the shower evolution of the *QTilde* shower is the  $b$  quark assumed massive.
- 5F, Zb For this set we consider the subtractive and multiplicative matching together with the *QTilde* and *Dipole* shower. The tree-level process of the underlying hard sub-process in this case is  $pp \rightarrow Zj_b \rightarrow e^+e^-j_b$ , where  $j_b \ni \{b, \bar{b}\}$ . For this sample the  $b$  quark is treated as massless, and  $p$  may also include a  $b$  quark. Generator-level cuts on the  $b$  quark have thus been applied. Only in the shower evolution of the *QTilde* shower is the  $b$  quark assumed massive. For single  $b$ -quark production only one  $p$  must contribute a  $b$  quark at a time, at the level of the hard sub-process at hand.

4F, Wbb For this set we consider the subtractive and multiplicative matching together with the *QTilde* shower. The tree-level process of the underlying hard sub-process in this case is  $pp' \rightarrow Wb\bar{b} \rightarrow \nu_l b\bar{b}$ , where  $l \in \{e^+, e^-, \mu^+, \mu^-\}$  and  $\nu_l$  the associated (anti-)neutrino. For this sample the  $b$  quark is considered massive and  $p, p'$  only consist of light quarks or a gluon, not a  $b$  quark;  $p'$  simply denotes the contribution of pair-wise different quark flavours in the initial state, as a result from the  $Wdu$  or  $Wsc$  vertex.

In all samples the uncertainty bands are purely from scale variations by simultaneously varying all scales in the hard sub-process and in the shower by factors of two up and down, i.e. factorization and renormalization scale in the hard sub-process, as well as scales related to  $\alpha_s$  variation and PDF reweighting in the shower, as well as the hard shower scale. The central scale choice is always a fixed scale (the  $Z$  mass in associated  $Z$  production; the  $W$  mass in associated  $W$  production).

The PDF sets being used are MMHT2014lo68cl and MMHT2014nlo68cl [31], i.e. the default PDF sets to which the showers are currently tuned. An internal study showed that using different PDF sets (a different  $n_f=5$  PDF set for the 5F runs or  $n_f=4$  PDF sets for the 4F runs) results in only minor differences, within the scale variation uncertainties.

In case the  $b$  quark is assumed massive, its mass is set to the default value in HERWIG7. All other relevant parameters, like  $W$  and  $Z$  mass and width, etc., are set to their respective default values in HERWIG7 as well.

For the 5F, Zbb sample we cut on the final state  $b$  quarks by including them into the jet-defining set of our jet matcher and requiring at least two jets, with a min.  $p^\perp$  of 18 GeV and 15 GeV for the first and second jet respectively. The statistics for this sample are 40k unweighted events so far.

For the 5F, Zb sample we cut on the final state  $b$  quark (similarly to above) by requiring at least one jet, with a min.  $p^\perp$  of 18 GeV for the first jet. The statistics for this sample are 100k unweighted events so far.

For both 5F samples we apply generator level cuts on the invariant mass of the charged-lepton pair, with a min. invariant mass of 60 GeV and a max. invariant mass of 120 GeV.

For the 4F, Zbb sample we apply no cuts on the  $b$  quarks. However, we require the same generator level cuts as for the 5F, Zbb and Zb samples on the invariant mass of the charged-lepton pair again. In addition we cut slightly on the charged leptons, with a min.  $p^\perp$  of 5 GeV and a rapidity range between -4 and 4. The statistics for this sample are 100k unweighted events so far.

For the 4F, Wbb sample we also apply no cuts on the  $b$  quarks. However, we require a slight generator level cut on the transverse mass of the  $W$ , with a min. transverse mass of 20 GeV. We also cut slightly on the charged lepton, with a min.  $p^\perp$  of 5 GeV and a rapidity range between -4 and 4. The statistics for this sample are 100k unweighted events so far.

### 1.33 Powheg

The results obtained with the POWHEG BOX framework are based on the generators presented in ref. [32]. The tree-level amplitudes, which include Born, real, spin- and colour-correlated Born amplitudes, were automatically generated using an interface [33] to MADGRAPH4 [34, 35], whereas the one-loop amplitudes were generated with GOSAM [36, 37] via the Binoth-Les-Houches (BLHA) interface [22, 23], presented for the POWHEG BOX and GOSAM in [38]. The version 2.0 of GOSAM [37] that was run is the 2.0: it uses QGRAF [39], FORM [40] and SPINNEY [41] for the generation of the Feynman diagrams. These diagrams are then computed at running time with NINJA [42, 43], which is a reduction program based on the Laurent expansion of the integrand [44], and using ONELOOP [45] for the evaluation of the scalar one-loop integrals. For unstable phase-space points, the reduction automatically switches to GOLEM [46], that allows to compute the same one-loop amplitude evaluating tensor integrals.

Further details can be found in ref. [32]. Here we briefly summarize the most important features.

1. We have used a mixed renormalization scheme [47], generally known as decoupling scheme, in which the  $n_{\text{f}}$  light flavours are subtracted in the usual  $\overline{\text{MS}}$  scheme, while the heavy-flavour loop is subtracted at zero momentum. In this scheme, the heavy flavour decouples at low energies. To make contact with other results expressed in terms of the  $\overline{\text{MS}}$  strong coupling constant, running with 5 light flavours, and with pdfs with 5 flavours, we have switched our scheme using the procedure discussed in ref. [48].
2. We have generated  $Wb\bar{b}j$  events using the `MinLO` [49] prescription, that attaches a suitable Sudakov form factor to the  $Wb\bar{b}j$  cross section at NLO, and subtracts its expansion (not to have double counting of the Sudakov logarithms), in order to get a finite cross section down to small transverse momentum of the hardest jet. The scales of the primary process (i.e. the process obtained by the attempt to cluster a  $Wb\bar{b}j$  event with a procedure similar to CKKW [9]) have been chosen as follows:
  - (a) if there has been a clusterization, then the scales are set to

$$\mu_{\text{R}} = \mu_{\text{F}} = \mu \equiv \frac{\sqrt{\hat{s}}}{4}, \quad \hat{s} = (p_{\text{W}} + p_{\text{b}} + p_{\bar{\text{b}}})^2, \quad (1)$$

where  $p_{\text{W}}$ ,  $p_{\text{b}}$  and  $p_{\bar{\text{b}}}$  are the momenta of the  $W$ ,  $b$  and  $\bar{b}$  in the primary process

- (b) If the event has not been clustered by the `MinLO` procedure, i.e. if the underlying Born  $Wb\bar{b}j$  process is not clustered by `MinLO`, we take as scale the partonic center-of-mass energy of the event.

The bands in the plots of Figs. 16 and 17 of this section are the envelope of the distributions obtained by varying the renormalization and factorization scales by a factor of 2 around the reference scale  $\mu$  of eq. (1), i.e. by multiplying the factorization and the renormalization scale by the scale factors  $K_{\text{F}}$  and  $K_{\text{R}}$ , respectively, where

$$(K_{\text{R}}, K_{\text{F}}) = (0.5, 0.5), (0.5, 1), (1, 0.5), (1, 1), (2, 1), (1, 2), (2, 2). \quad (2)$$

These variations have been computed using the POWHEG BOX reweighting procedure, that recomputes the weight associated with an event in a fast way.

## 1.4 Z+b(b) production

### 1.4.1 Z+b(b) with SHERPA

Figures 1 and 2 show a selection of the plots comparing Sherpa predictions to data. There is overall a good agreement, but for the normalization. The 5F LO order predictions are generally below the data, though compatible within the large scale uncertainty. For NLO predictions this uncertainty is smaller and some patterns can be observed. Both the 5F and the 4F NLO are in good agreement with distributions for events with two b-tagged jets. But when a single b-jet is tagged, the 5F and 4F results have an opposite behaviour: the 5F is 20% above the data (except for high  $Z$   $p_{\text{T}}$ ), while 4F is 20% below.

It is nevertheless remarkable that the ratio of 4F NLO predictions to data is flat for all the observables. This is particularly interesting, since it is more efficient to generate a sample of  $Z + b\bar{b}$  events with the 4F scheme than with the 5F. The reason why an overall normalization factor is needed could lie in the large logarithms, that in the 5F scheme are resummed in the  $b$  parton distribution function. However they might not affect the shape of the distributions. To check this hypothesis the 4F NLO predictions have been rescaled to the best available inclusive cross-sections *FIXME:UNCERTAINTY BAND/REFERENCES*. A selection of the plots is shown in Figure 3. The results are very encouraging but further studies are needed to understand if this approach fails for other observables, e.g. those related to the presence of additional light-quark jets.

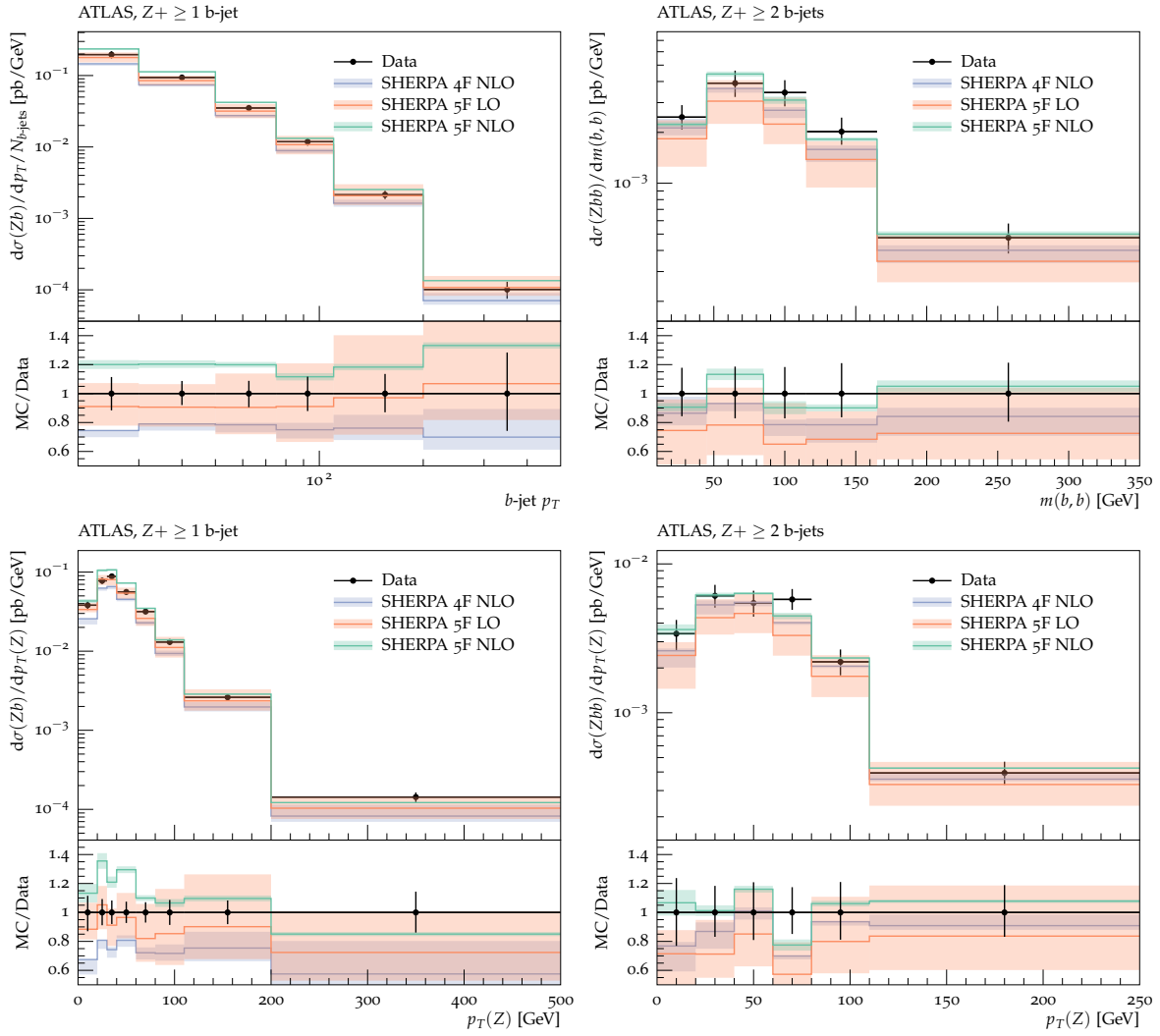


Fig. 1: A selection of the plots comparing Sherpa predictions to ATLAS results.

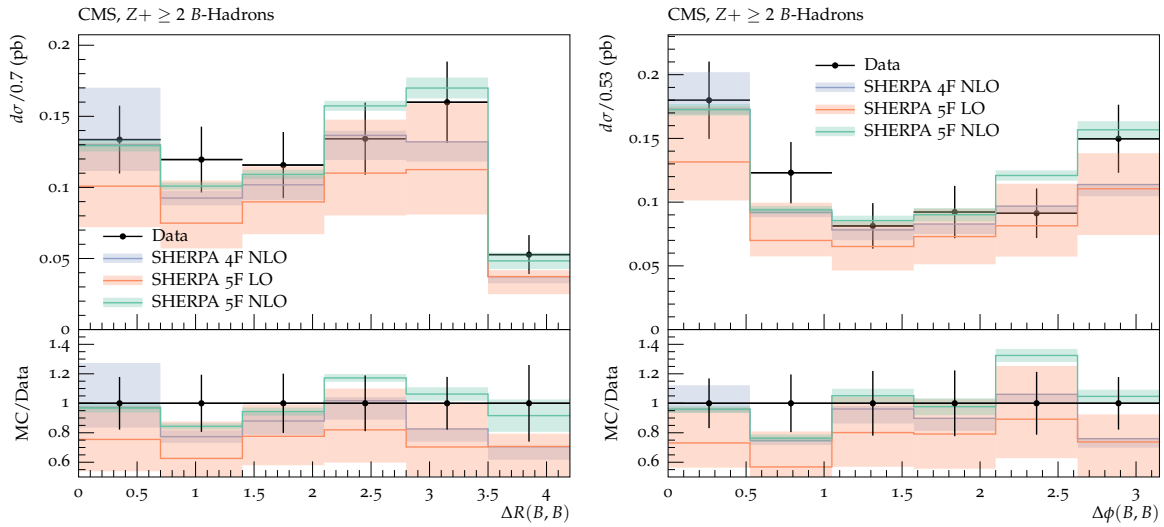


Fig. 2: A selection of the plots comparing Sherpa predictions to CMS results.

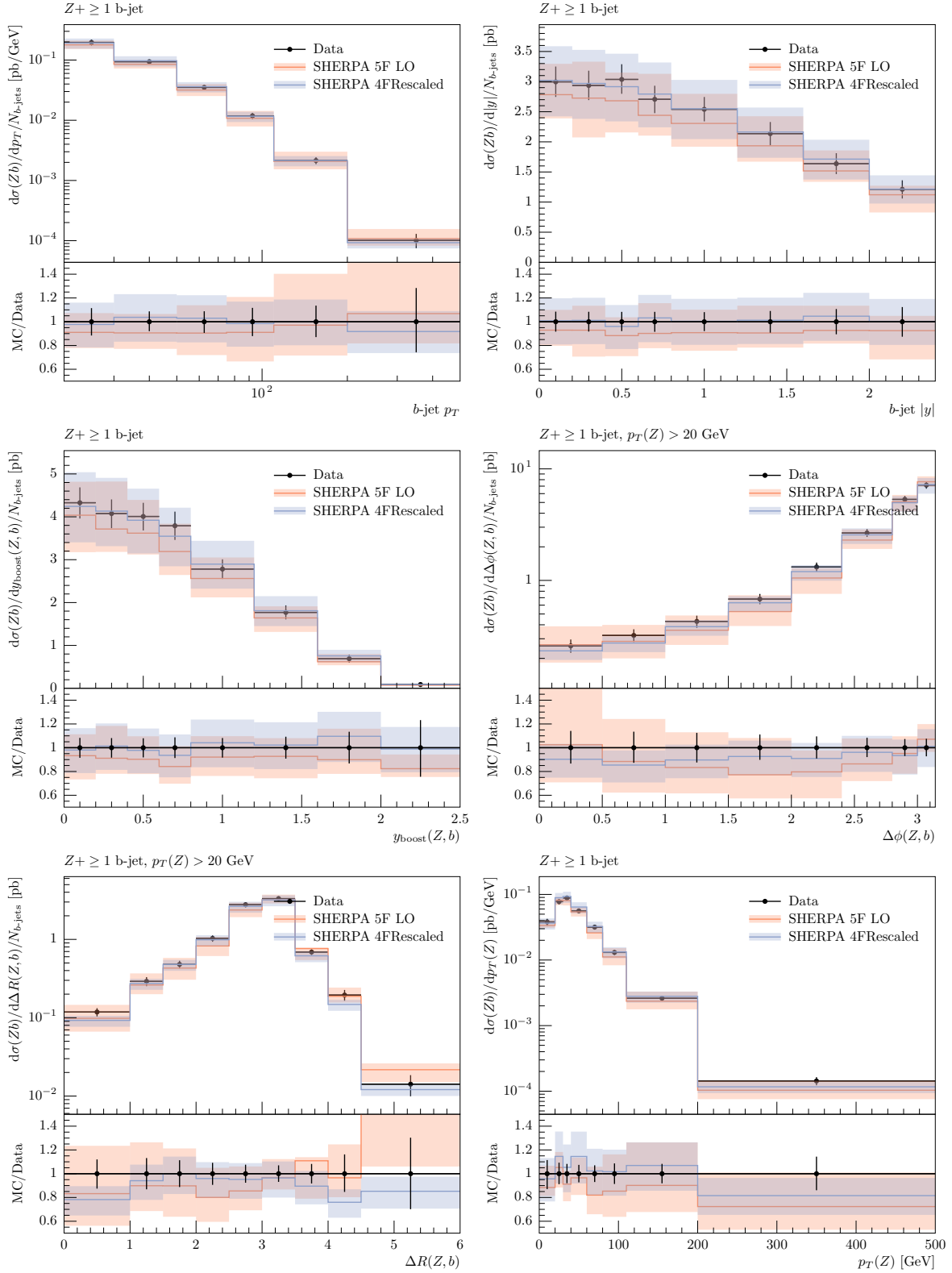


Fig. 3: *FIXME:REMOVE ONE PLOT OR ADD Z PT?* A selection of the plots comparing rescaled Sherpa 4F NLO predictions to ATLAS results.

### 1.42 $Z+b(b)$ with HERWIG7

A selection of results is shown in figures 4, 5, 6 and 7 for the 5F, Zbb setup, in figures 8, 9, 10 and 11 for the 5F, Zb setup, and in figures 12, 13, 14 and 15 for the 4F, Zbb setup. Regarding the process setups for the 5F, Zb and Zbb samples, as well as for the 4F, Zbb sample we refer to section 1.32.

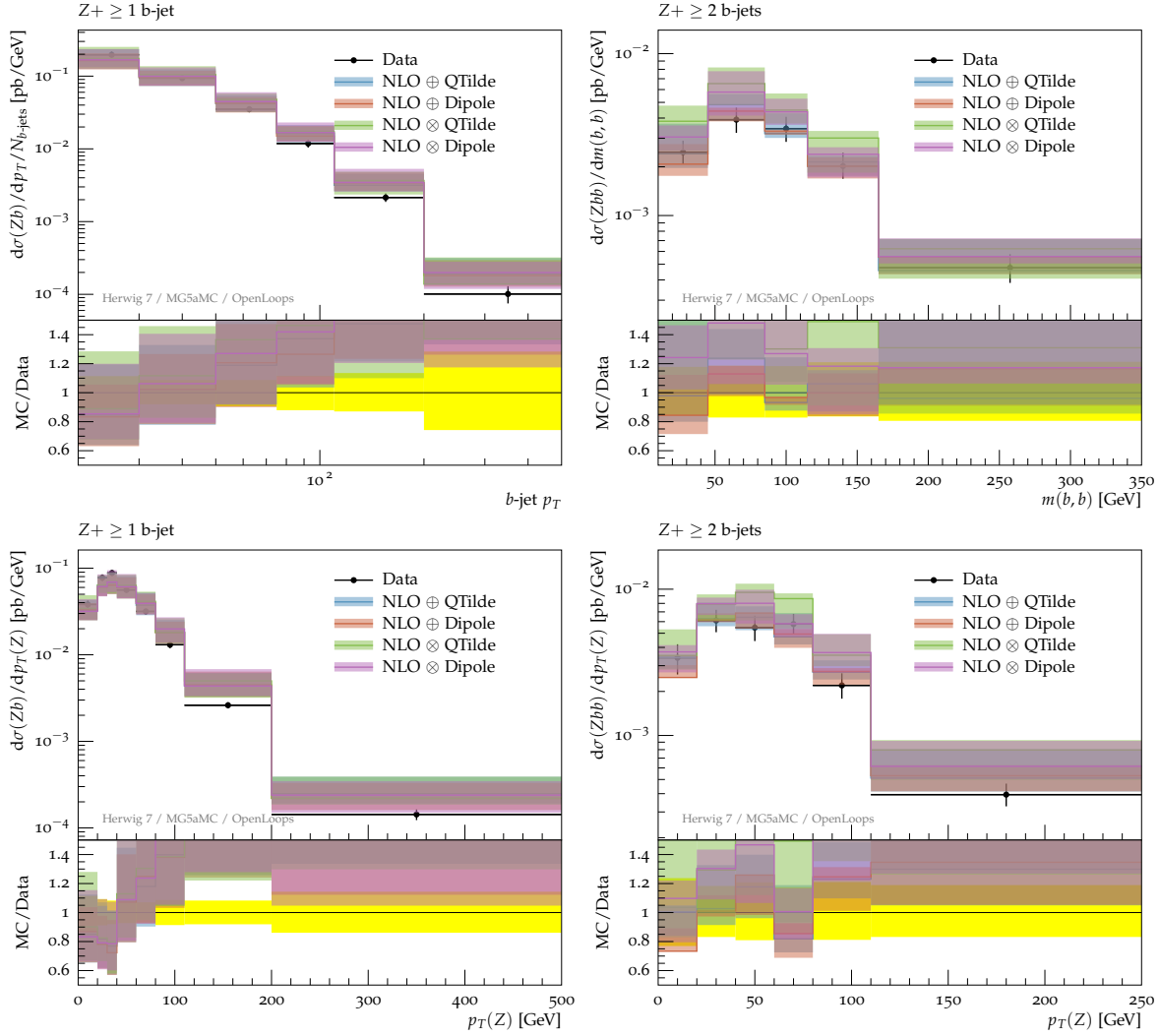


Fig. 4: A selection of the plots comparing HERWIG7 5F, Zbb predictions to ATLAS results.

## 1.5 W+b production

Results for the 4F, Wbb setup (as described in section 1.33 and 1.32) are shown in figures 16 and 17.

## 1.6 Conclusions



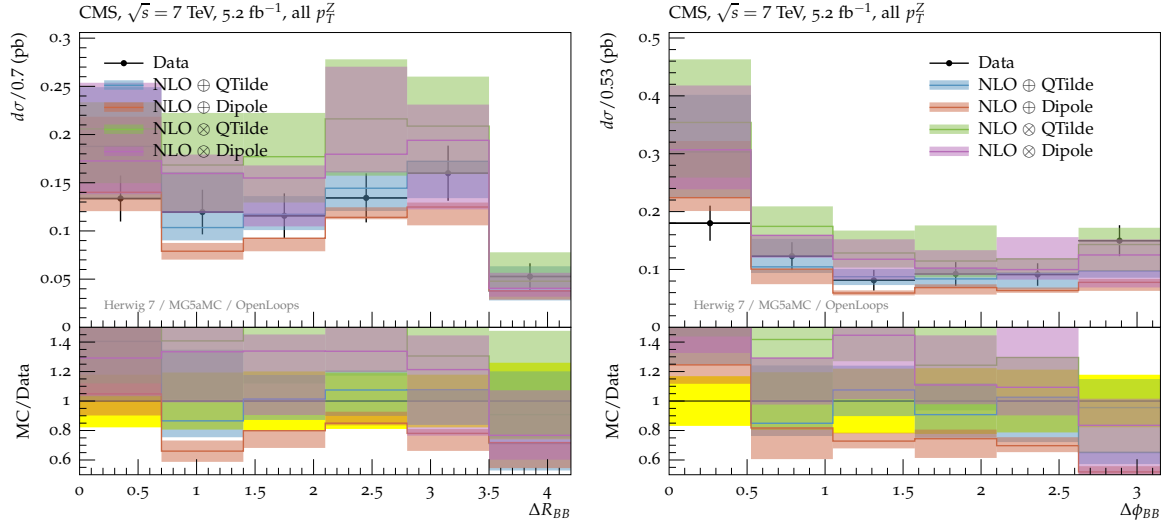


Fig. 5: A selection of the plots comparing HERWIG7 5F, Zbb predictions to CMS results.

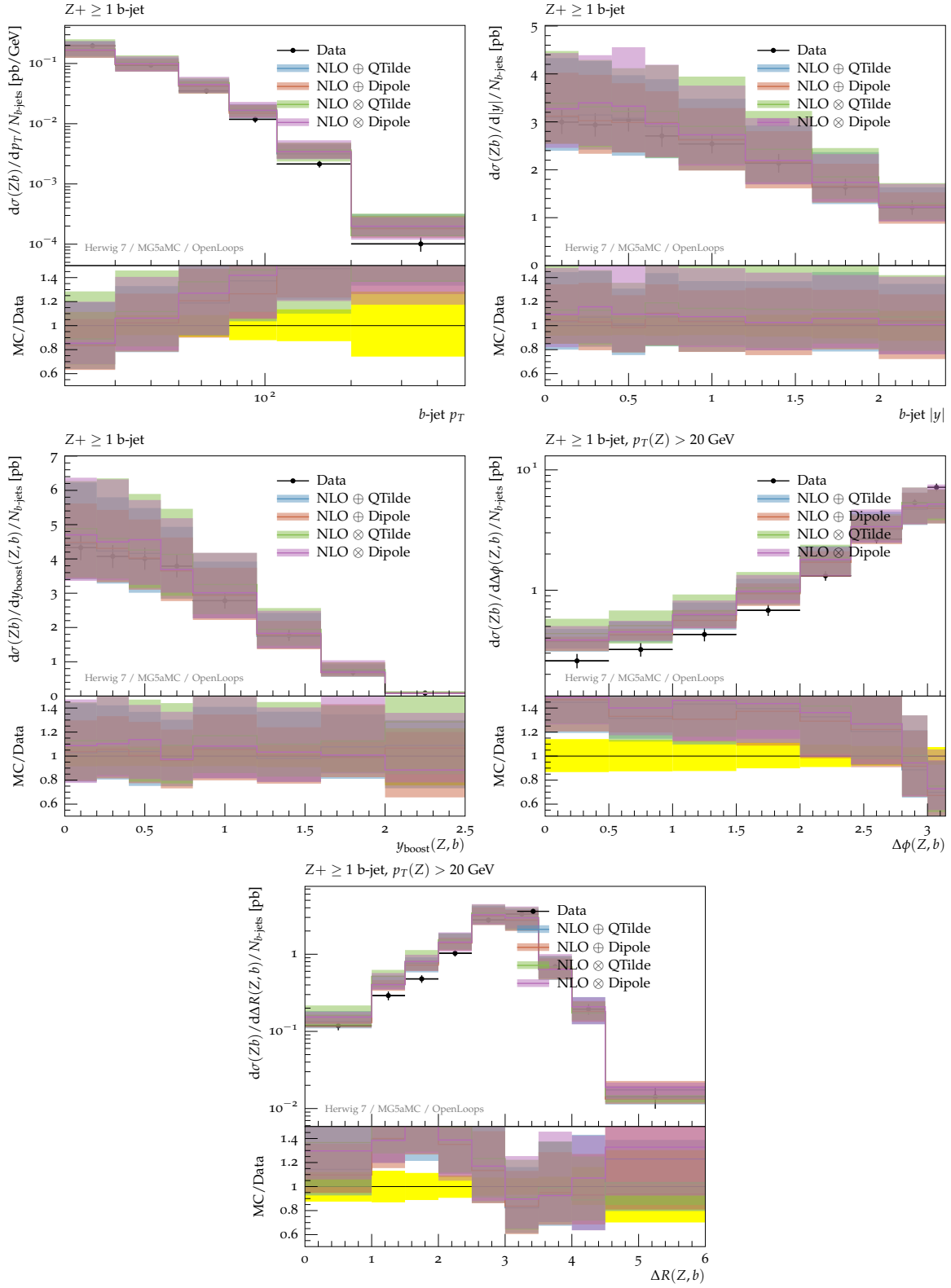


Fig. 6: A selection of the plots comparing HERWIG7 5F,  $Zb\bar{b}$  predictions to ATLAS results; in comparison to figure 3.

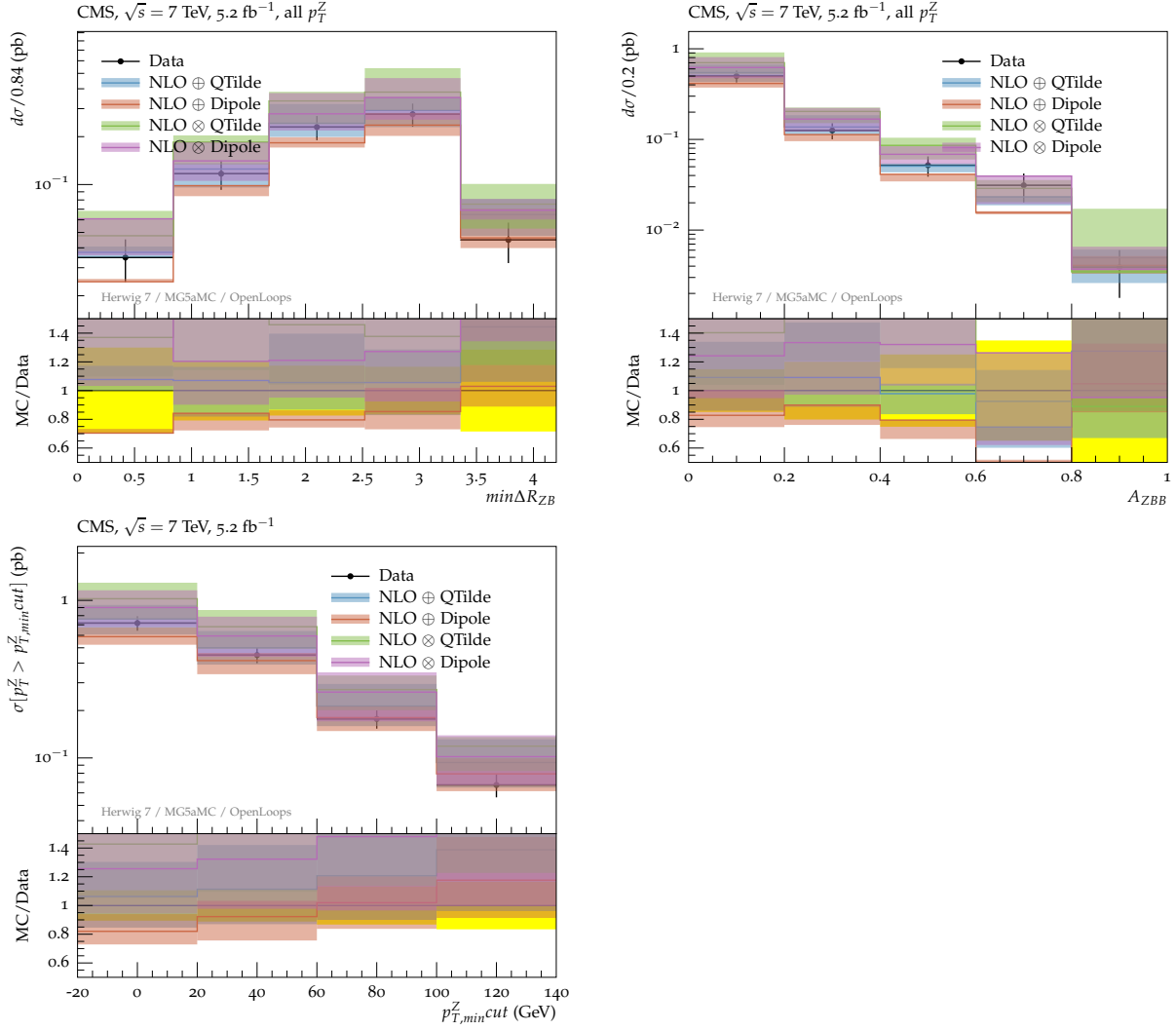


Fig. 7: A selection of the plots comparing HERWIG7 5F, Zbb predictions to CMS results.

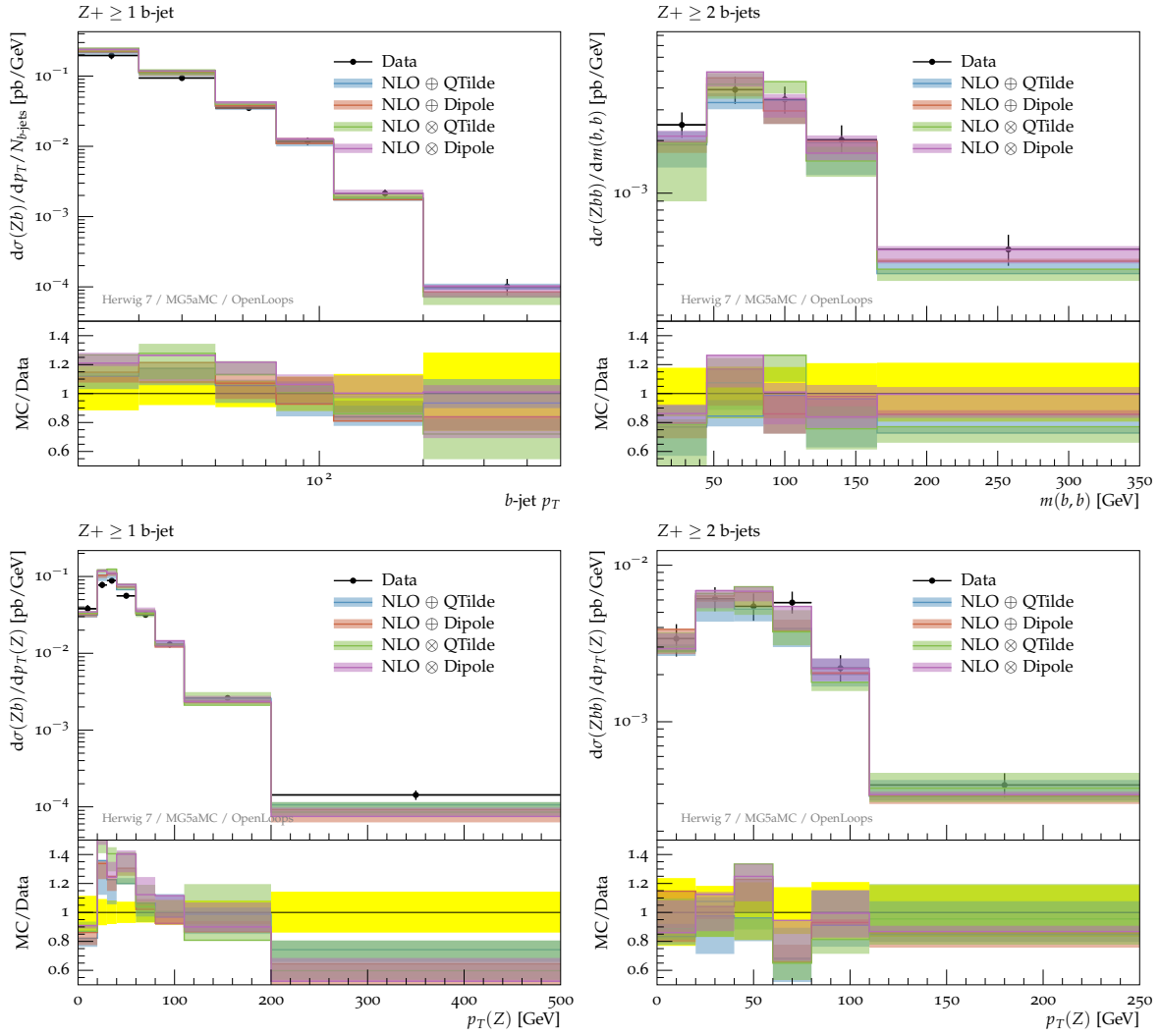


Fig. 8: A selection of the plots comparing HERWIG7 5F, Zb predictions to ATLAS results.

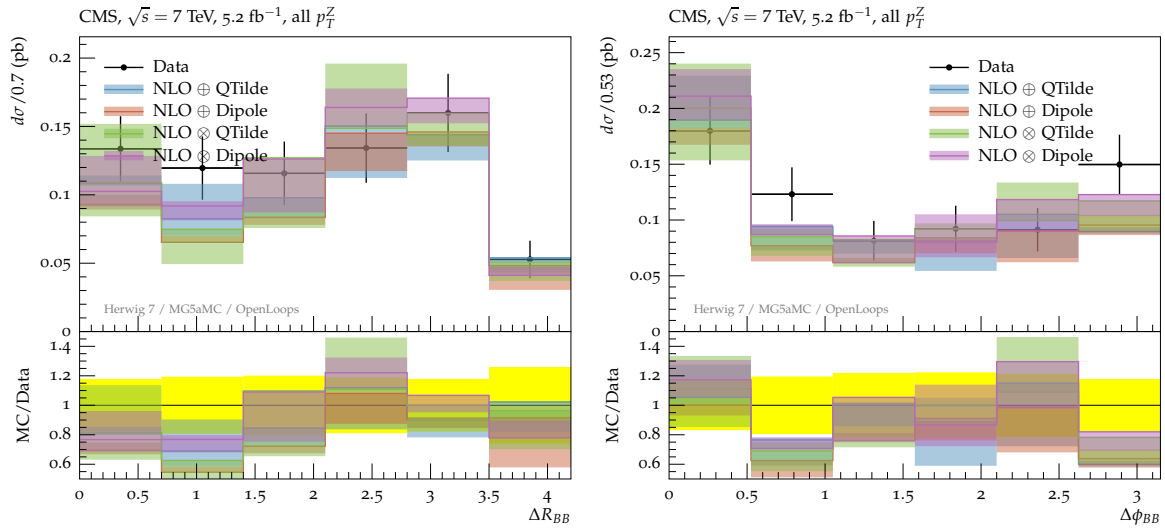


Fig. 9: A selection of the plots comparing HERWIG7 5F, Zb predictions to CMS results.

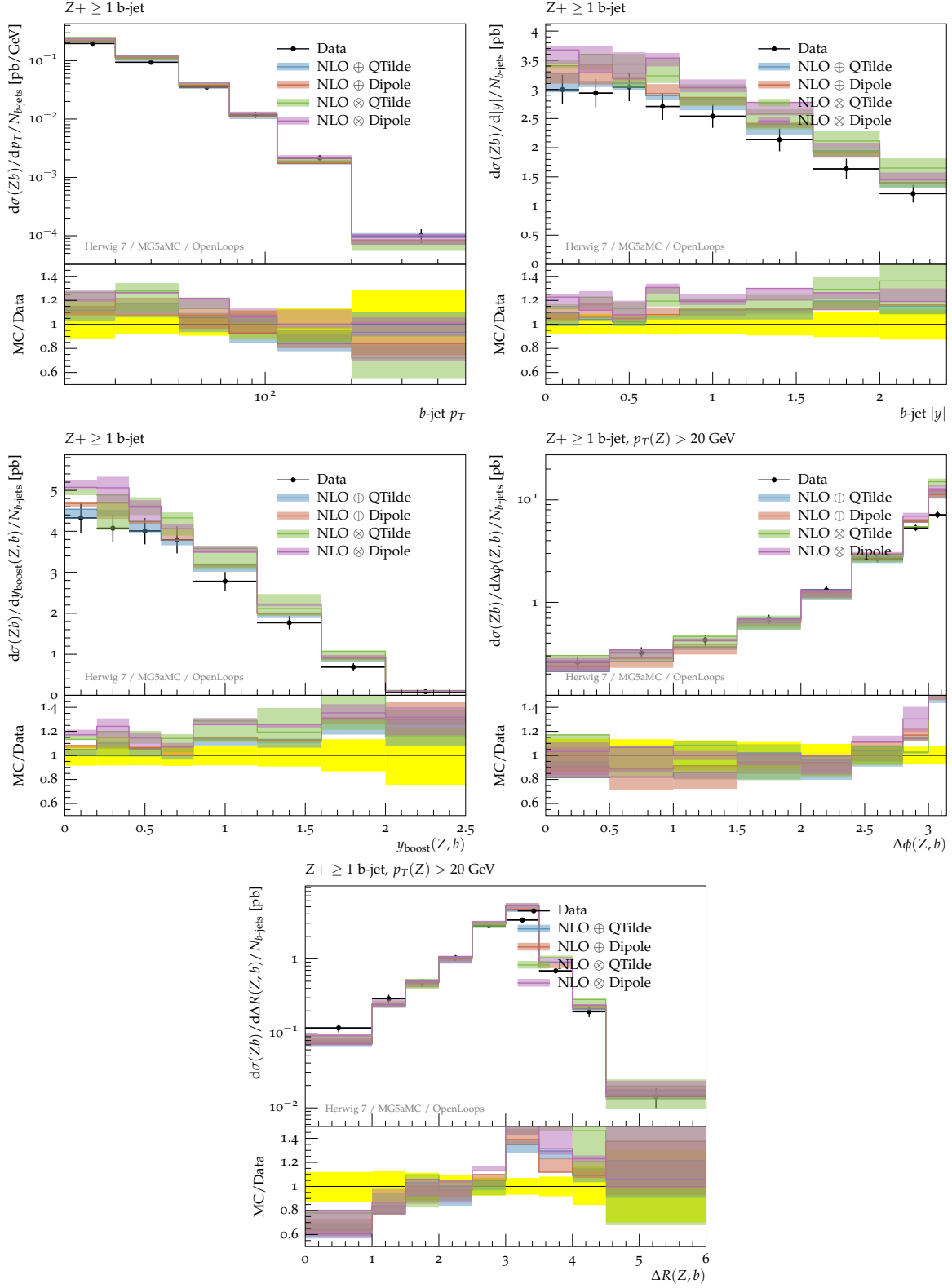


Fig. 10: A selection of the plots comparing HERWIG7 5F, Zb predictions to ATLAS results; in comparison to figure 3.

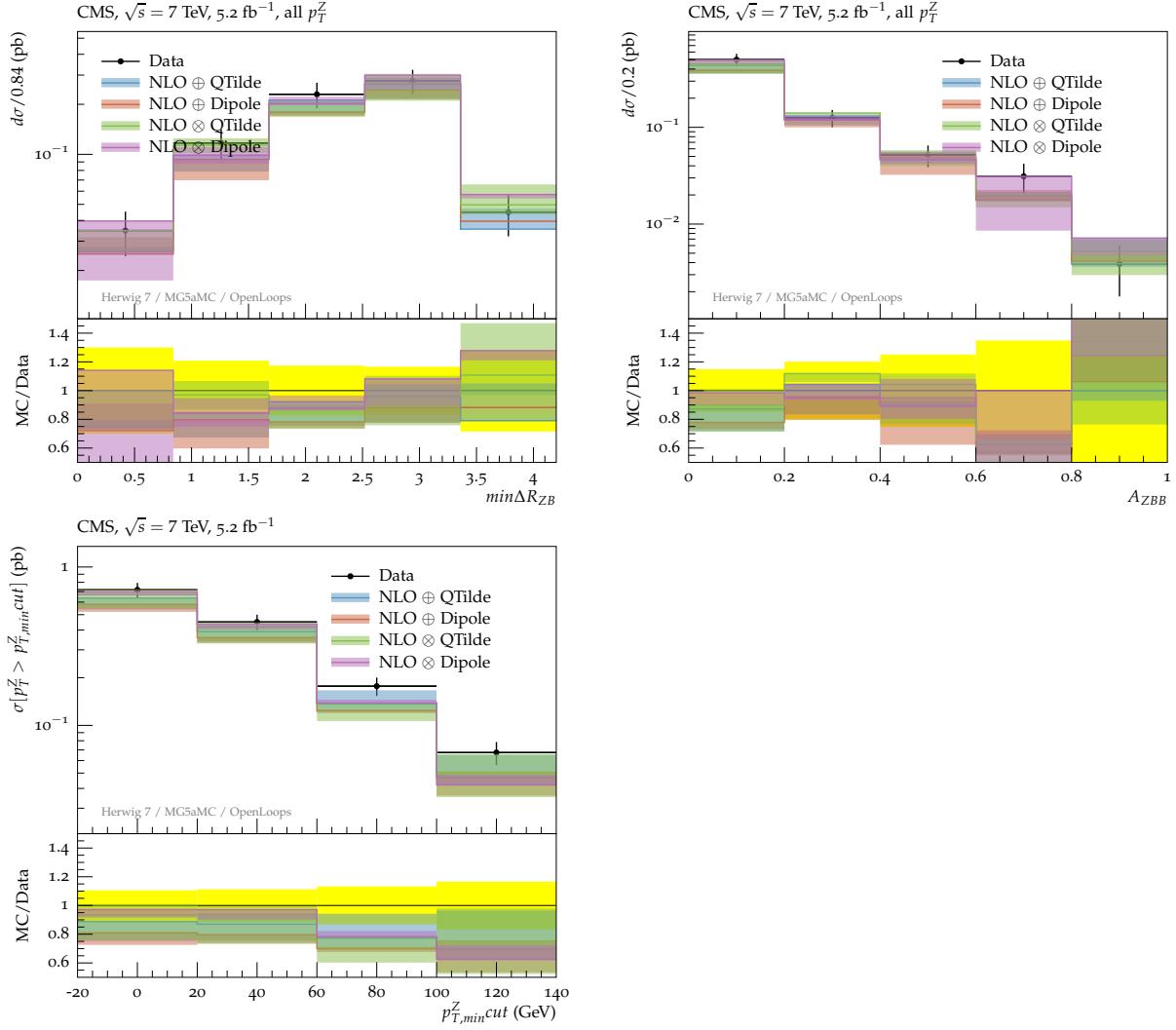


Fig. 11: A selection of the plots comparing HERWIG7 5F, Zb predictions to CMS results.

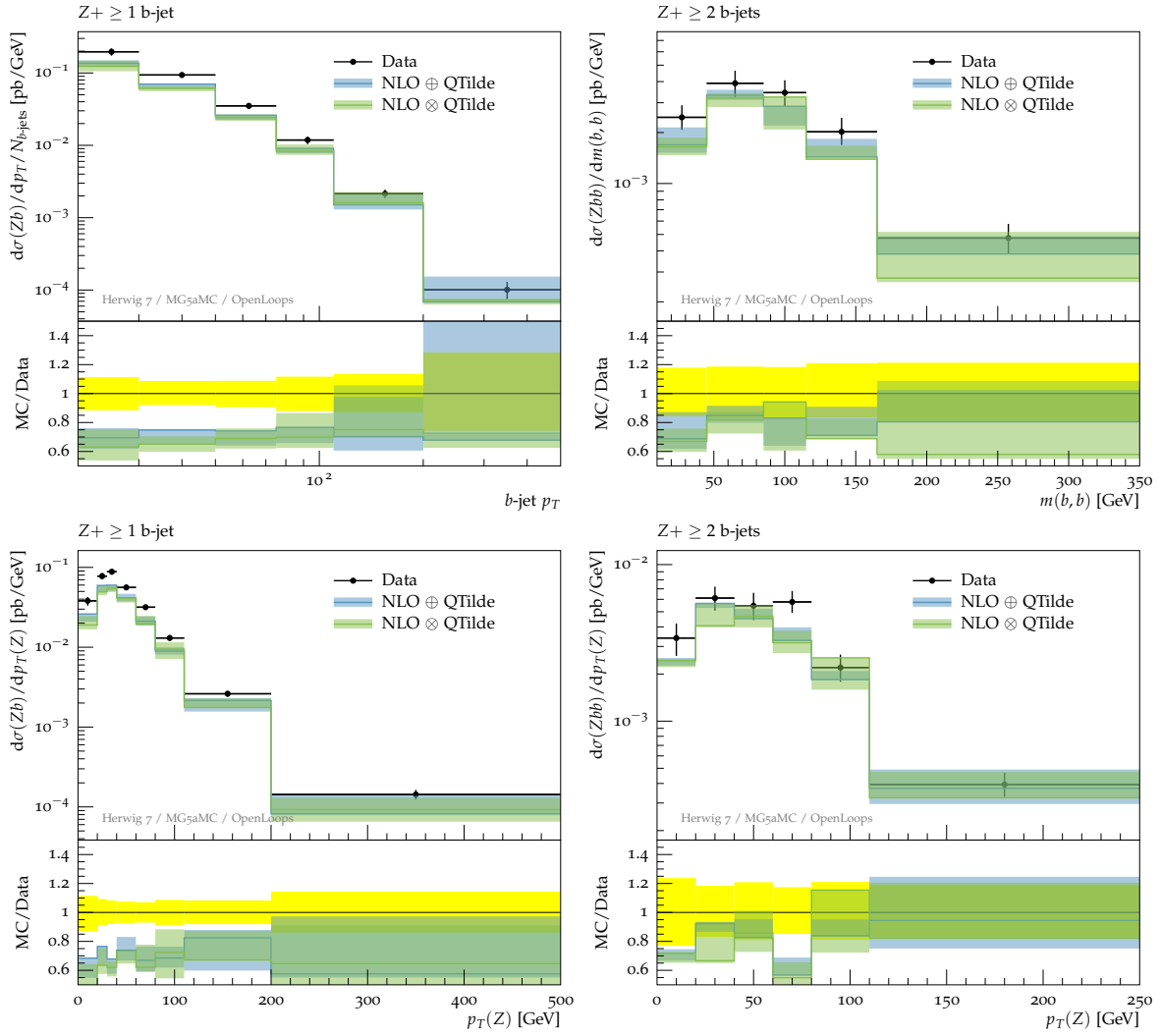


Fig. 12: A selection of the plots comparing HERWIG7 4F, Zbb predictions to ATLAS results.

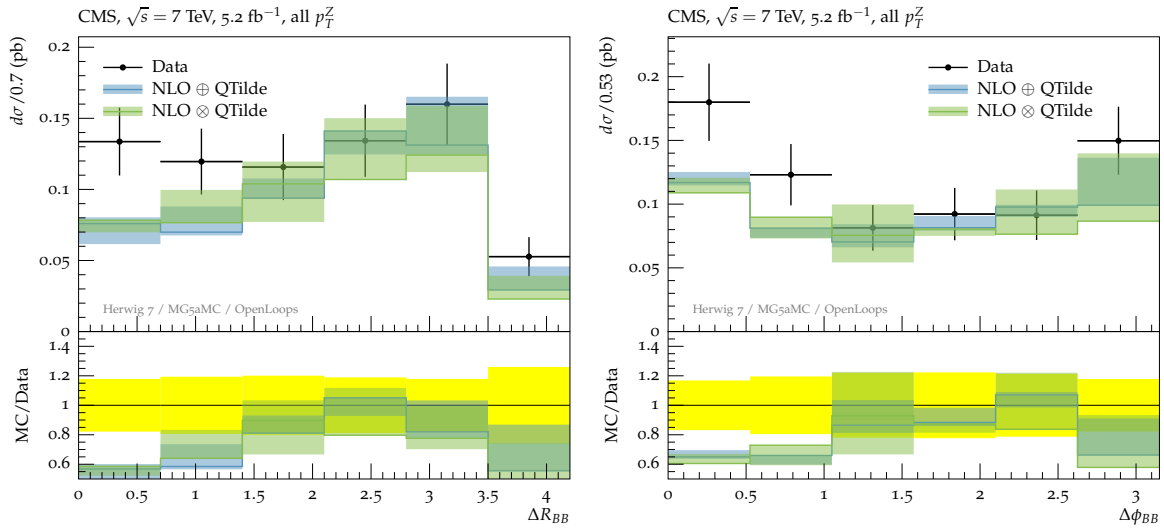


Fig. 13: A selection of the plots comparing HERWIG7 4F, Zbb predictions to CMS results.

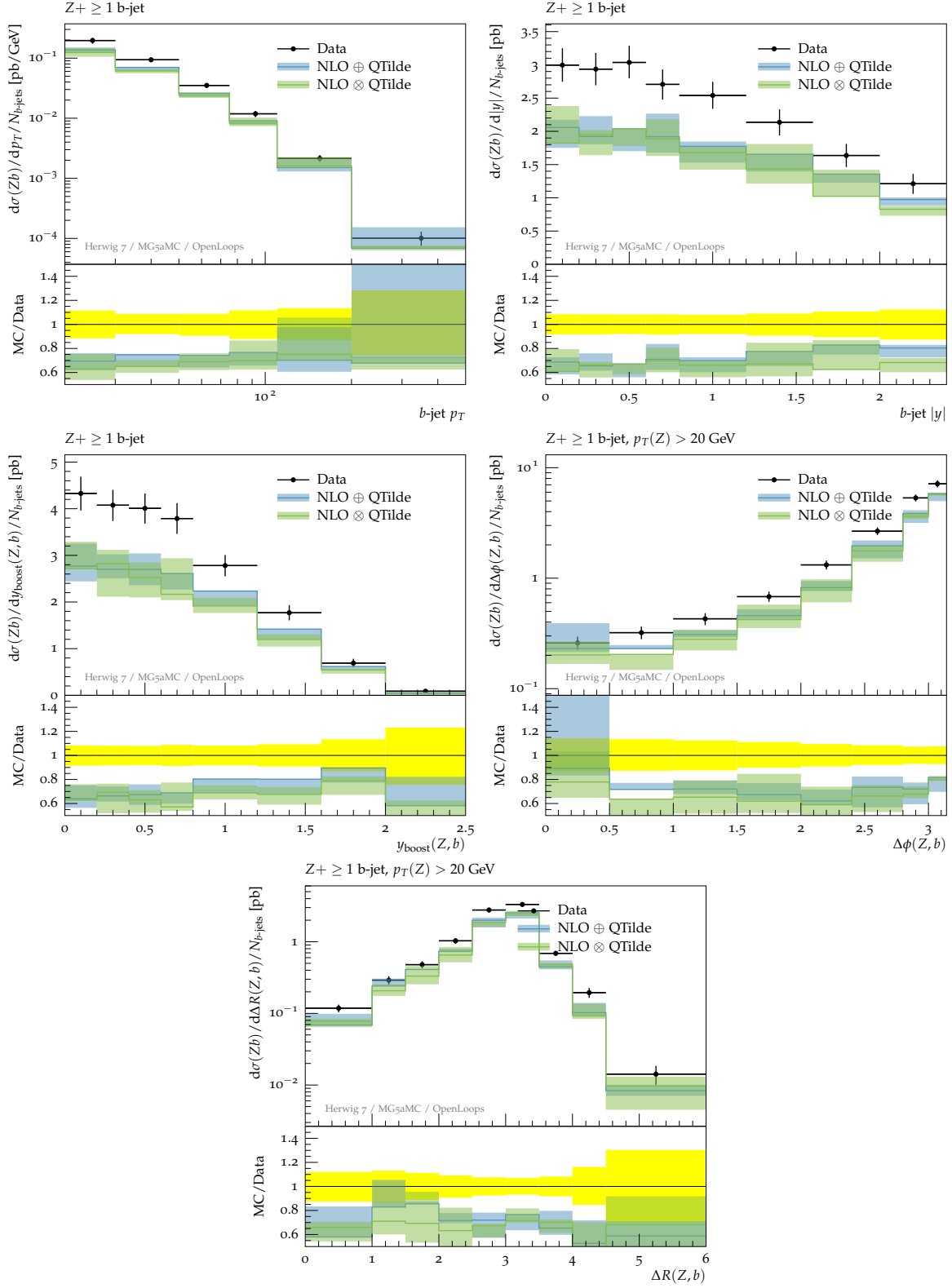


Fig. 14: A selection of the plots comparing HERWIG7 4F, Zbb predictions to ATLAS results; in comparison to figure 3.



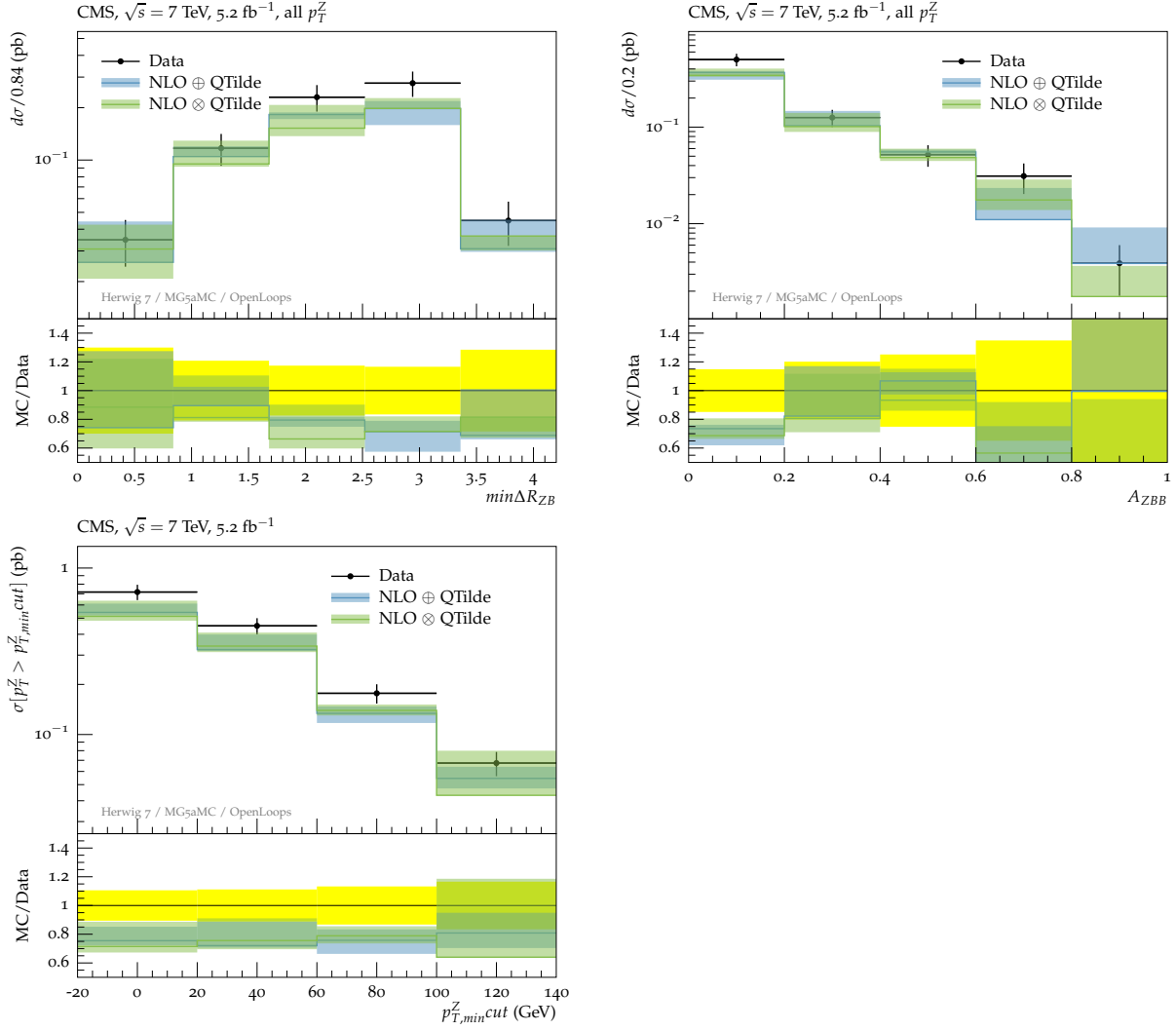


Fig. 15: A selection of the plots comparing HERWIG7 4F, Zbb predictions to CMS results.

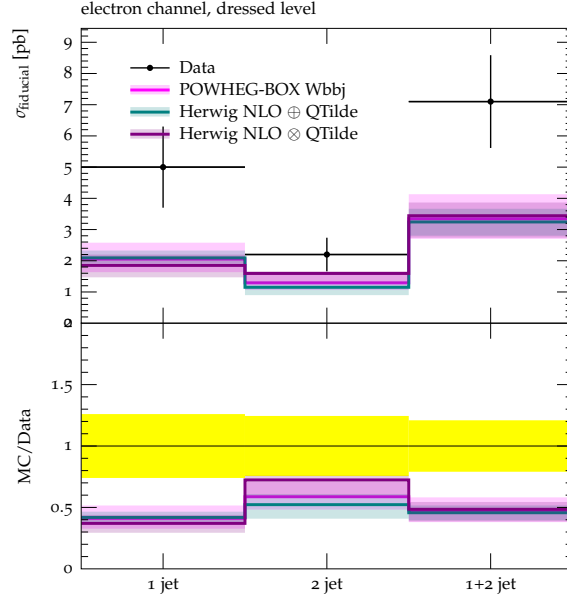


Fig. 16: ATLAS measured cross sections for  $Wb$  production with only a  $b$ -tagged jet (“1 jet”), one  $b$ -tagged and at least an additional jet (“2 jet”), or both (“1+2 jet”) . The theoretical results are at the full shower+hadron level. No DPI corrections are included.

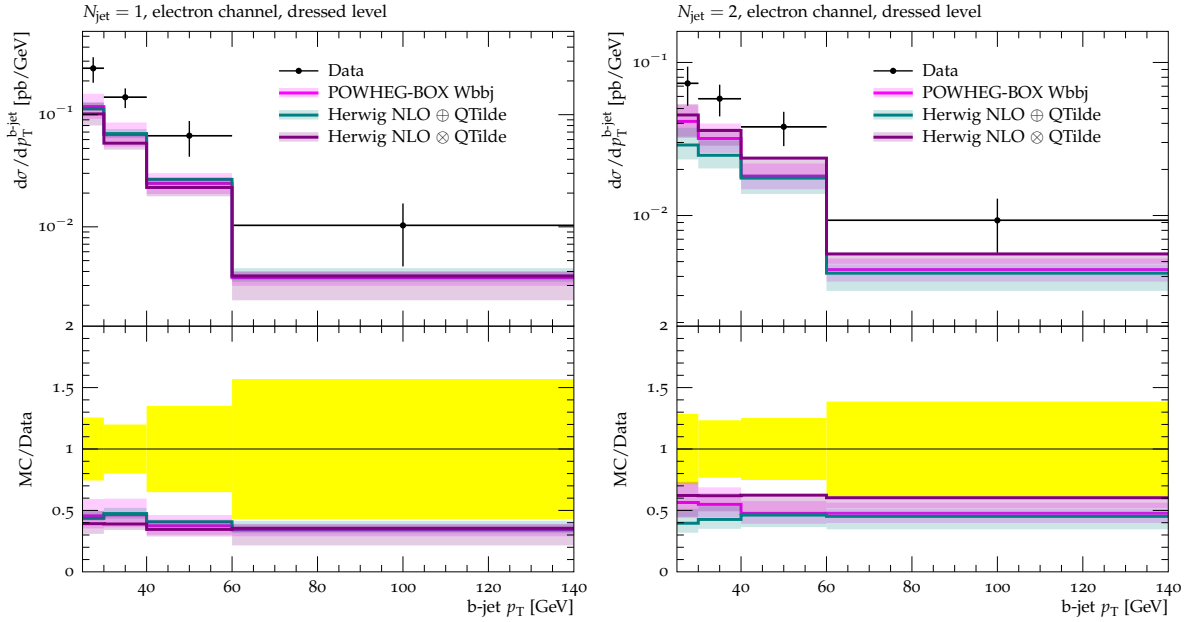


Fig. 17: ATLAS measured differential  $p_T$  distribution of the  $b$ -tagged jet in  $W + b$  events with a single jet (left) or with at least one additional jet (right). The theoretical results are at the shower+hadron level. No DPI corrections are included.

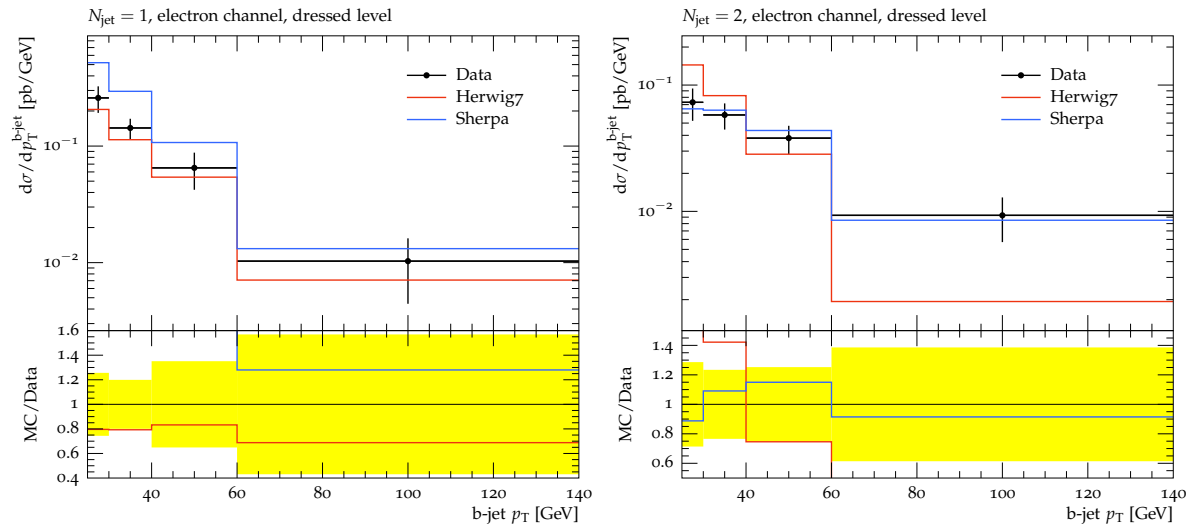


Fig. 18: Differential  $p_T$  distribution of the b-jet in  $W + b$  events with a single jet (left) or with two jets (right). Superimposed are shown the predictions from Sherpa  $W + b\bar{b}j$ . *FIXME: SHERPA IS LO/NLO? REMOVE HERWIG FROM THESE PLOTS? ADD ALSO RATE PLOT HERE OR REMOVE EVERYWHERE?*

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