

# **NEMATIC MATERIALS IN CURVES SPACES**

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The Academic Faculty

By

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# NEMATIC MATERIALS IN CURVES SPACES

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A great quote to start the thesis

*George P. Burdell*

A great dedication goes here.

## **ACKNOWLEDGEMENTS**

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# **Appendices**

**APPENDIX A**  
**SOMETHING HERE?**

## **VITA**

Vita may be provided by doctoral students only. The length of the vita is preferably one page. It may include the place of birth and should be written in third person. This vita is similar to the author biography found on book jackets.