

# Maximum Topological Sort

## Assignment 5

### Data Structures and Algorithms

**Problem Statement:** Given a tree  $G$  with  $N$  nodes and  $N-1$  undirected edges .

Among all nodes, you can pick a node  $u$  and give a direction to each edge in  $G$  in a way that all the nodes in  $G$  are reachable from node  $u$  , to obtain a digraph  $G'$  . It can be proved that the digraph  $G'$  is a DAG . Report the node in  $G$  corresponding to whose pick the digraph  $G'$  obtained has maximum no. of topological sort orderings and also the maximum no. of topological sort orderings modulo  $1e9 + 7$ . If multiple possible such nodes exist report the maximum among them .

#### Input

Each test contain multiple test cases. First line contains  $T$ , the number of test cases.

Each test case begins with  $N$ , the number of nodes in  $G$ .

It is followed by  $N - 1$  lines containing 2 integers  $u, v$ , denoting an undirected edge between  $u$  and  $v$ .

#### Output

Print 2 space separated integers, the node which is the optimal pick and maximum no. of topological sort orderings possible modulo  $1e9 + 7$ .

#### Constraints

$$1 \leq T \leq 10$$

$$1 \leq N \leq 10^6$$

$$1 \leq u, v \leq N$$

It is guaranteed that total no. of nodes across all test cases  $\leq 10^6$ .

**Time Limit:** 4 seconds

**Memory Limit:** 256 MB

#### Sample Test Case

Input	Output
2	2 2
3	3 12
1 2	
2 3	
5	
1 2	
1 3	
3 4	
3 5	

#### Explanation

In the first test case of sample,

orientation *w.r.t* 1 is  $1 \rightarrow 2 \rightarrow 3$ , only 1 topological sort ordering possible.

orientation *w.r.t* 2 is  $1 \leftarrow 2 \rightarrow 3$ , 2 topological sort orderings possible.

orientation *w.r.t* 3 is  $1 \leftarrow 2 \leftarrow 3$ , only 1 topological sort ordering possible.

Hence optimal pick is node 2 and max possible topological sort orderings is 2.