## Title

aprlb — Estimate the lower bound on the average persuasion rate

# Syntax

aprlb depvar instrvar [covariates] [if] [in] [, model(string)
title(string)]

## **Options**

| option                                 | Description   |
|--|---|
| <pre>model(string) title(string)</pre> | Regression model when <i>covariates</i> are present Title |

# Description

aprlb estimates the lower bound on the average persuasion rate (APR). varlist should include depvar instrvar covariates in order. Here, depvar is binary outcomes (y), instrvar is binary instruments (z), and covariates (x) are optional.

There are two cases: (i) covariates are absent and (ii) covariates are present.

- Without x, the lower bound (theta\_L) on the APR is defined by

theta\_L = 
$$\{\Pr(y=1 | z=1) - \Pr(y=1 | z=0)\}/\{1 - \Pr(y=1 | z=0)\}.$$

The estimate and its standard error are obtained by the following procedure:

- 1. Pr(y=1|z=1) and Pr(y=1|z=0) are estimated by regressing y on z.
- 2. theta L is computed using the estimates obtained above.
- 3. The standard error is computed via STATA command nlcom.
- With x, the lower bound (theta\_L) on the APR is defined by

```
theta_L = E[theta_L(x)],
```

where

```
theta_L(x) = \{\Pr(y=1 | z=1, x) - \Pr(y=1 | z=0, x)\}/\{1 - \Pr(y=1 | z=0, x)\}.
```

The estimate is obtained by the following procedure.

If model("no interaction") is selected (default choice),

1. Pr(y=1|z,x) is estimated by regressing y on z and x.

Alternatively, if model("interaction") is selected,

- 1a. Pr(y=1|z=1,x) is estimated by regressing y on x given z=1. 1b. Pr(y=1|z=0,x) is estimated by regressing y on x given z=0.

Ater step 1, both options are followed by:

- 2. For each x in the estimation sample, theta L(x) is evaluated.
- 3. The estimates of  $theta_L(x)$  are averaged to estimate  $theta_L$ .

When covariates are present, the standard error is missing because an analytic formula for the standard error is complex. Bootstrap inference is implemented when this package's command **persuasio** is called to conduct inference.

#### **Options**

model(string) specifies a regression model of y on z and x.

This option is only relevant when x is present. The default option is "no\_interaction" between z and x. When "interaction" is selected, full interactions between z and x are allowed; this is accomplished by estimating  $\Pr(y=1 | z=1,x)$  and  $\Pr(y=1 | z=0,x)$ , separately.

title(string) specifies a title.

#### Remarks

It is recommended to use this package's command **persuasio** instead of calling **aprlb** directly.

#### Examples

We first call the dataset included in the package.

. use GKB, clear

The first example estimates the lower bound on the APR without covariates.

. aprlb voteddem\_all post

The second example adds a covariate.

. aprlb voteddem\_all post MZwave2

The third example estimates the lower bound by the covariate.

. by MZwave2, sort: aprlb voteddem\_all post

# Stored results

#### Scalars

e(N): sample size

e(lb\_coef): estimate of the lower bound on the average persuasion
rate

 $e(lb\_se)$ : standard error of the lower bound on the average persuasion rate

# Macros

 ${\tt e(outcome):}$  variable name of the binary outcome variable

e(instrument): variable name of the binary instrumental variable

e(covariates): variable name(s) of the covariates if they exist

e(model): regression model specification ("no\_interaction" or "interaction")

## Functions:

e(sample): 1 if the observations are used for estimation, and 0
otherwise.

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GPL-3

### References

Sung Jae Jun and Sokbae Lee (2019), Identifying the Effect of Persuasion, arXiv:1812.02276 [econ.EM]

## Version

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