

## Title

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**aprlb** — Estimate the lower bound on the average persuasion rate

## Syntax

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```
aprlb depvar instrvar [covariates] [if] [in] [, model(string)  
title(string)]
```

## Options

<i>option</i>	<i>Description</i>
<b>model</b> ( <i>string</i> )	Regression model when <i>covariates</i> are present
<b>title</b> ( <i>string</i> )	Title

## Description

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**aprlb** estimates the lower bound on the average persuasion rate (APR). *varlist* should include *depvar instrvar covariates* in order. Here, *depvar* is binary outcomes (*y*), *instrvar* is binary instruments (*z*), and *covariates* (*x*) are optional.

There are two cases: (i) *covariates* are absent and (ii) *covariates* are present.

- Without *x*, the lower bound (**theta\_L**) on the APR is defined by

$$\mathbf{theta\_L} = \{\Pr(y=1|z=1) - \Pr(y=1|z=0)\} / \{1 - \Pr(y=1|z=0)\}.$$

The estimate and its standard error are obtained by the following procedure:

1.  $\Pr(y=1|z=1)$  and  $\Pr(y=1|z=0)$  are estimated by regressing *y* on *z*.
2. **theta\_L** is computed using the estimates obtained above.
3. The standard error is computed via STATA command **nlcom**.

- With *x*, the lower bound (**theta\_L**) on the APR is defined by

$$\mathbf{theta\_L} = E[\mathbf{theta\_L\_num}(x)]/E[\mathbf{theta\_L\_den}(x)],$$

where

$$\mathbf{theta\_L\_num}(x) = \Pr(y=1|z=1,x) - \Pr(y=1|z=0,x)$$

and

$$\mathbf{theta\_L\_den}(x) = 1 - \Pr(y=1|z=0,x).$$

The estimate is obtained by the following procedure.

If **model**("no\_interaction") is selected (default choice),

1.  $\Pr(y=1|z,x)$  is estimated by regressing  $y$  on  $z$  and  $x$ .

Alternatively, if **model**("interaction") is selected,

1a.  $\Pr(y=1|z=1,x)$  is estimated by regressing  $y$  on  $x$  given  $z = 1$ .

1b.  $\Pr(y=1|z=0,x)$  is estimated by regressing  $y$  on  $x$  given  $z = 0$ .

Ater step 1, both options are followed by:

2. For each  $x$  in the estimation sample, **theta\_L\_num**( $x$ ) and **theta\_L\_den**( $x$ ) are evaluated.

3. The estimates of **theta\_L\_num**( $x$ ) and **theta\_L\_den**( $x$ ) are averaged to estimate **theta\_L**.

When *covariates* are present, the standard error is missing because an analytic formula for the standard error is complex. Bootstrap inference is implemented when this package's command **persuasio** is called to conduct inference.

## **Options**

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**model**(*string*) specifies a regression model of  $y$  on  $z$  and  $x$ .

This option is only relevant when  $x$  is present. The default option is "no\_interaction" between  $z$  and  $x$ . When "interaction" is selected, full interactions between  $z$  and  $x$  are allowed; this is accomplished by estimating  $\Pr(y=1|z=1,x)$  and  $\Pr(y=1|z=0,x)$ , separately.

**title**(*string*) specifies a title.

## **Remarks**

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It is recommended to use this package's command **persuasio** instead of calling **aprlb** directly.

## **Examples**

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We first call the dataset included in the package.

```
. use GKB_persuasio, clear
```

The first example estimates the lower bound on the APR without covariates.

```
. aprlb voteddem_all post
```

The second example adds a covariate.

```
. aprlb voteddem_all post MZwave2
```

The third example estimates the lower bound by the covariate.

```
. by MZwave2, sort: aprlb voteddem_all post
```

## **Stored results**

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### **Scalars**

**e(N)**: sample size

**e(lb\_coef)**: estimate of the lower bound on the average persuasion rate

**e(lb\_se)**: standard error of the lower bound on the average persuasion rate

### **Macros**

**e(outcome)**: variable name of the binary outcome variable

**e(instrument)**: variable name of the binary instrumental variable

**e(covariates):** variable name(s) of the covariates if they exist

**e(model):** regression model specification ("no\_interaction" or "interaction")

**Functions:**

**e(sample):** 1 if the observations are used for estimation, and 0 otherwise.

**Authors**

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Sung Jae Jun, Penn State University, <sjun@psu.edu>

Sokbae Lee, Columbia University, <sl3841@columbia.edu>

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**References**

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Sung Jae Jun and Sokbae Lee (2022), Identifying the Effect of Persuasion, [arXiv:1812.02276](https://arxiv.org/abs/1812.02276) [econ.EM].

**Version**

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