1 Introduction to Turing Machine Language

In this section, you are given some programs in Turing Machine Language (TML). They will be used to explain the syntax of the programming language and how they can be run on tapes.

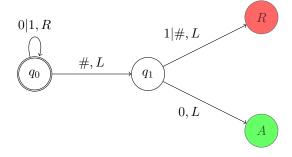
• isDiv2:

```
// checks whether a binary number is divisible by 2
    alphabet = \{0, 1\}
    module isDiv2 {
       while 0, 1 {
5
           move right
6
       } if blank {
7
           move left
           if 0 {
8
9
               accept
10
           } if 1, blank {
11
               reject
12
13
        }
14 }
```

• isDiv2Rec:

```
1 \hspace{0.1in} / / checks whether a binary number is divisible by 2 recursively
    alphabet = {0, 1}
3
    module isDiv2Rec {
4
        if 0, 1 {
5
            move right
 6
            goto isDiv2Rec
 7
        } if blank {
            move left
8
9
            if 0 {
10
                accept
11
            } if 1, blank {
12
                reject
13
14
        }
15
    }
```

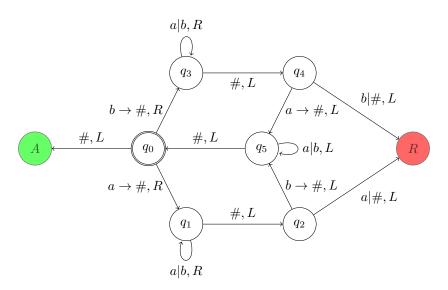
Both isDiv2 and isDiv2Rec correspond to the following Turing Machine (TM):



• palindrome:

```
// checks whether the given string is a palindrome, i.e. the string equals its reverse
    alphabet = {a, b}
 3
    module palindrome {
        if blank {
 4
 5
           accept
 6
        // starts with a => check ends with a
        if a {
 8
 9
           changeto blank
10
           move right
           // move to the end
11
12
           while a, b {
13
               move right
14
           } if blank {
15
               move left
               // cannot end with a b
16
               if b {
17
18
                   reject
19
               } if a, blank {
20
                   changeto blank
21
                   move left
22
                   goto restart
23
               }
24
           }
25
        }
26
        // starts with b => check ends with b \,
27
        if b {
28
           changeto blank
29
           move right
30
           // move to the end
           while a, b {
31
               move right
32
           } if blank {
33
34
               move left
35
               // cannot end with an a
36
               if a {
37
                   reject
38
               } if b, blank {
39
                   changeto blank
40
                   move left
41
                   goto restart
42
               }
           }
43
        }
44
45
    }
46
    // go to the start and restart
47
    module restart {
48
        while a, b {
49
           move left
50
        } if blank {
51
           move right
52
           goto palindrome
53
54 }
```

The program palindrome corresponds to the following TM:



2 Identifying TML Programs

In this section, you are presented with TML programs. You will be given some tape values to run the program in and decode what values the program accepts. You are encouraged to use the website to try and solve this.

1. Consider the following TML Program:

```
alphabet = \{0, 1\}
2
    module mystery {
3
       while 0, 1 {
4
           move right
5
       } if blank {
6
           move left
           if blank, 0 {
               reject
9
           } if 1 {
10
               move left
               if blank, 1 {
11
                   reject
12
13
               } if 0 {
14
                   accept
15
16
17
18 }
```

(a) Does the program accept the values:

i. 2 = 10

Solution:

ii. 1 = 1

Solution:

iii. 4 = 100

Solution:

iv. 5 = 101

Solution:

v. 6 = 110

Solution:

(b) Describe the values this program accepts.

2. Consider the following TML program:

```
alphabet = {a, b}
    module mystery {
3
        if blank {
           accept
 4
5
       } if a {
6
           changeto blank
           move right
8
           while a, b {
9
               move right
10
           } if blank {
11
               move left
12
               if a {
13
                   reject
14
               } if b, blank {
                   changeto blank
15
16
                   move left
17
                   while a, b {
18
                      move left
19
                   } if blank {
20
                      move right
21
                       goto mystery
22
               }
23
24
           }
25
       } if b {
26
           changeto blank
27
           move right
28
           while a, b {
29
               move right
30
           } if blank {
31
               move left
32
               if b {
33
                   reject
34
               } if a, blank {
35
                   changeto blank
                   move left
36
37
                   while a, b {
38
                      move left
39
                   } if blank {
40
                      move right
41
                       goto mystery
42
43
               }
44
           }
45
46
    }
```

(a) Does the program accept the values:

i. ab

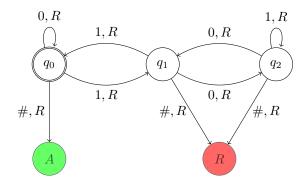
ii.	aab
	Solution:
iii.	abb
	Solution:
iv.	abba
	Solution:
v.	abab
	Solution:
Desc	cribe the values this program accepts.
So	olution:

(b)

3 Identifying TMs

In this section, you are presented with TMs. You will be given some tape values to run the program in and decode what values the program accepts. Since the website can only execute TML programs, you are also given the TML program for the code, but it is not comprehensible like the previous programs; you will likely find it easier to understand the TM than the program (which you should do!).

1. Consider the following TM FSM:



You are given a basic representation of this FSM as code in Teams.

(a) Does the TM accept the values:

i.
$$2 = 10$$

Solution:

ii. 1 = 1

Solution:

iii. 6 = 100

Solution:

iv. 5 = 101

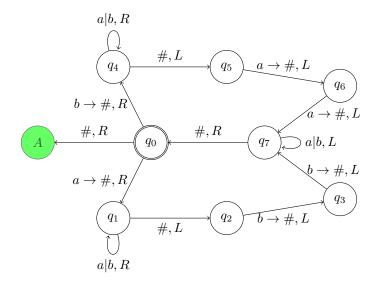
Solution:

v. 8 = 110

Solution:

(b) Describe the values this program accepts.

2. Consider the following TM FSM:



NOTE: The missing transitions go to the reject state, i.e. q_2 , q_3 to a|# and q_5 , q_6 to b|# are rejected. You are given a basic representation of this FSM as code in Teams.

(a) Does this TM accept the values:

i.	ab	

Solution:

ii. abb

Solution:

iii. aabb

Solution:

iv. bbaaaa

Solution:

v. abba

Solution:

vi. abab

Solution:

(b) Describe the values this program accepts.

4 Writing TML Programs

Following a similar syntax to the code given above, write the following programs. You are free to use the website to check the accuracy of the program while writing the programs.

1. divisibility by 4 in binary iteratively [HINT: Go to the end and check for 2 zeros. Allow 0 as well.] Solution:

Solution:			

Solution:			

Solution:			

Solution:			

5 Appendix- Links

Below are the links to the website and the survey:

 \bullet Website: Link to Website

• Survey: Link to Survey