

Math 135, Calculus 1, Fall 2020

Weekly Quiz 11-18

Show all work: clearly indicate your answer and the reasoning used to arrive at the answer. Unsupported answers may not receive full credit.

Problem 1. Consider the function $f(x) = 6x - x^2$.

(a) Use calculus to find the critical point(s) of $f(x)$.

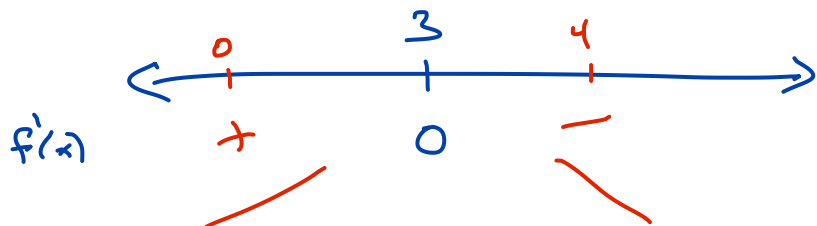
$$\begin{aligned} f'(x) &= 6 - 2x \stackrel{!}{=} 0 \\ 2x &= 6 \\ \boxed{x &= 3} \end{aligned}$$

(b) Use calculus to compute the absolute maximum and minimum values of $f(x)$ on $[0, 5]$.

EVT: CPs & Endpoints

$$\begin{aligned} f(3) &= 6(3) - (3)^2 = 18 - 9 = \boxed{9} \text{ Absolute max value} \\ f(0) &= 6(0) - (0)^2 = \boxed{0} \text{ Absolute min value} \\ f(5) &= 6(5) - (5)^2 = 30 - 25 = 5 \end{aligned}$$

(c) Use calculus to find the intervals where $f(x)$ is increasing or decreasing.



$$f'(0) = 6 - 2(0) > 0$$

$$f'(4) = 6 - 2(4) < 0$$

Increasing on $(-\infty, 3)$
Decreasing on $(3, \infty)$