### Structures and All That

September 26, 2019

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We can get you prepared for the 31st century
With advanced programming and quad rendering
And Java plus plus plus scripting language
We offer advanced job placement assistance"

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We have taken a weird approach by fixating on data structured in the form of "or" first.

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- Let's say that in Java that you have some person class with a first and last name represented as strings.
- It is easy to define a method that returns the person's full name by concatenating the first and last name.

So, why do we need compound data?

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- We can represent a grid with one number in the same sense that we can simulate a 10x10 2D array with a 100 element array.

## Structs Make Things Easier

Personally, I like doing things the easy way.



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```
def first_name(tup):
   return tup[0]
```

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We can actually define other data structures in terms of things like lists.

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- So Python gives classes (or named tuples) as a way to more easily define such structured data.

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- We will return to discussing lists in more detail later, since they are extremely important.
- But for now, remember that we wanted to avoid the inconveniences given by using other existing data types to represent some piece of compound data!

We said that we didn't want to represent all of our compound data with existing structures like lists are tuples, so let's *finally* talk about structs.

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```
(check-expect (distance-to-0 (point 0 5)) 5)
(check-expect (distance-to-0 (point 7 0)) 7)
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previous version of this function that took in two parameters.
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Testing that function is simple, so let's just move on to talking about structs in general.

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  - One selector per field, which extracts the value of the field from a structure instance; and
  - 3. One structure predicate, which, like ordinary predicates, distinguishes instances from all other kinds of values.

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- The selectors per field are (point-x point-val) and (point-y point-val). The general form of a selector for a specific field is (struct-name-field-name val)
- 3. A predicate for checking types is automatically created, for example: (point? point-val) and in general a predicate struct? is created.

Here are some basic examples of structs:

• (struct movie [title producer year])

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- Sample Problem Develop a structure type definition for a
  program that deals with bouncing balls,. The balls location is
  a single number, namely the distance of pixels from the top.
  Its constant speed is the number of pixels it moves per clock
  tick. Its velocity is the speed plus the direction in which it
  moves.

# Designing Our Ball Struct

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- Now, we can represent a ball as a point (which only has positive components) and a vector (which can have negative components): (struct 2D-ball position vec)

Our 2D Ball struct has nested occurrences of other structs. This is a natural thing, and even recursive descriptions of data are natural, i.e. linked lists and binary trees. But we can also consider using a *flat representation* for our 2D Ball, which doesn't nest structs.

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```
(define-struct point [x y])
; A Point is a structure:
; (point Number Number)
; interpretation a point x pixels from left, y from top
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- Let us consider how to relate a struct description to a diagram that illustrates its "structure".
- (struct centry [name home office cell])

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So, for cell phone entry structs we had three fields that can contain possible values. Consider the following concrete one:

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- This has the following visual representation:

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name phone email "lee@x.me"
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 In a sense, calling (centry-name p1) is unlocking a box in the struct, with a specific key that allows you to retrieve the underlying value. In general we can think of field access as a kind of "unboxing".

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- Using a "key" to unlock the wrong box raises a runtime error (centry-name (point 1 2)) → entry-name:expects a centry, given (point 42 5)

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• Interestingly, we can give 2 interpretations, depending on if the ball is moving vertically (interpretation 1) or horizontally (interpretation 2)

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```
; A Ball-2d is a structure:
; (ball Point Vel)
; interpretation a 2-dimensional position and velocity

(define-struct vel [deltax deltay])
; A Vel is a structure:
; (vel Number Number)
; interpretation (make-vel dx dy) means a velocity of
; dx pixels [per tick] along the horizontal and
; dy pixels [per tick] along the vertical direction
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- The T just communicates that we are defining linked lists that work over any type (parametric polymorphism otherwise known as generics in Java)

## Structs and Program Design

Now we need to consider designing programs using structs. **Sample Problem** Your team is designing an interactive game program that moves a red dot across a image canvas and allows players to use the mouse to reset the dot. Here is how far you got together:

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```
(define MTS (empty-scene 100 100))
(define DOT (circle 3 "solid" "red"))
; A Point represents the state of the world.
: Point -> Point
(define (main p0)
  (big-bang p0
    [on-tick x+]
    [on-mouse reset-dot]
    [to-draw scene+dot]))
```

### Designing scene+dot

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 Testing this is uninteresting, so let's consider if we were asked to define the x+ function, which takes in a Point and returns a new Point with an x-coordinate that is 3 units further to the right of the old point.

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(check-expect (x+ (point 0 0)) (point 3 0))
(check-expect (x+ (point 10 10)) (point 13 10))
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```

 To take inventory we project out the x and y fields from our point, as usual:

```
(define (x+p) (... (point-x p) ... (point-y p) ...)
```

```
(define (x+ p)
  (point (+ (point-x p) 3) (point-y p)))
```

To finish coding, we need to first add 3 to the x-coordinate and then pack the result back into a new point structure.

```
(define (x+ p)
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• This is a perfect example of the *essence* of functional programming. We are creating a *new* point whose x-coordinate is based on the old one, instead of modifying the original point to store a new x-coordinate.

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- If we had more fields than y, we simply are projecting out the old field as an argument when creating the new struct value.
- This adds a lot of boilerplate code...

We might want to define a function, point-set-x which takes in a point and a value and produces a new point where the x-coordinate is the given value and the y-coordinate is taken from the old point.

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- point-set-x is known as a *functional setter*, similar to a more traditional setter in languages like Java.
- However, defining an update operation on a complicated structure can get very complicated, and we can get around this uses *lenses* (we may discuss this later in the course).

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```
(check-expect
  (reset-dot (point 10 20) 29 31 "button-down")
  (point 29 31))
(check-expect
  (reset-dot (point 10 20) 29 31 "button-up")
  (point 10 20))
```

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- For real this time:

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(define (reset-dot p x y me)
  (cond
    [(mouse=? "button-down" me) (... p ... x y ...)]
    [else (... p ... x y ...)]))
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Finally, though the skeleton looks complicated the final version of the function is relatively simple.

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- The takeaway here is that our skeletons can end up being more complicated than the actual final version.
- This is especially true when we consider skeletoning out code for which a parameter is a struct.

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 For some of the classes you see in Java, skeletoning out code in such a manner is infeasible...

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 If a function deals with nested structures, develop one function per level of nesting.

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```
(define (complex-skeleton ball)
  (... (point-x (ball-position ball)) ...
     ... (vec-delta-y (ball-vector ball)) ...))
```

 Of course, things are easier if we picked the write functions to add in our skeleton, but this keeps the structure of the skeleton much simpler.

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- Of course, things are easier if we picked the write functions to add in our skeleton, but this keeps the structure of the skeleton much simpler.
- We will return to this point later in the course.

Signatures can tell us a lot about a function. I'll put some signatures up, and what kind of functions could we write for these signatures?

Number Number → Number

- Number Number → Number
- Point Vec → Point

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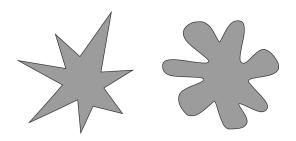
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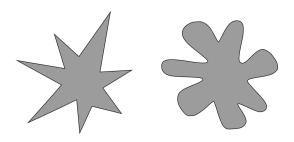
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- The idea that a function signature can tell you about the behavior of the function is an extremely powerful idea.

Here's a fun little experiment. Look at these two shapes:

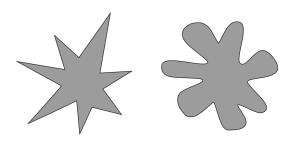


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- Which of these shapes is named Bouba and which Kiki?
- This is likely due to some physical attributes of sound, but our strong preference for naming the round one Bouba and the sharp one Kiki shows that humans have innate preferences about the naming and representation of things.

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; "hello",
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- For example, look at this data definition:

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• If this is the domain of some function, we restricted ourselves to needing to handle three values.

With itemizations we specified subsets of the existing data universe.

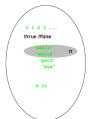


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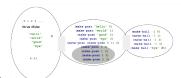


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Notice that we specify our point struct as containing two numbers.

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- Without that, it is up to us programmers to validate that points are only constructed with valid arguments.
- This might mean creating a function
   (define (make-point x y) ...) that checks that both x
   and y actually receive integers before calling the point
   constructor. More on this later.

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- For intervals, use the end points (if they are included) and at least one interior point.
- For itemizations, deal with each part separately
- For data definitions for structures, follow the natural language description; that is, use the constructor and pick an example from the data collection named for each field.