

Structures and All That

October 1, 2019

“Here at Brymar College
We can get you prepared for the 31st century
With advanced programming and quad rendering
And Java plus plus plus scripting language
We offer advanced job placement assistance”

from Upgrade by Deltron 3030

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- Whereas with “or” we would check which kind of data we would have and then use a computation specific to that data, with products we can directly project out data.
- Let's say that in Java that you have some person class with a first and last name represented as strings.
- It is easy to define a method that returns the person's full name by concatenating the first and last name.

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- We can represent a grid with one number in the same sense that we can simulate a 10x10 2D array with a 100 element array.

Structs Make Things Easier

Personally, I like doing things the easy way.



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def first_name(tup):  
    return tup[0]
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- So Python gives classes (or named tuples) as a way to more easily define such structured data.

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- We will return to discussing lists in more detail later, since they are *extremely* important.
- But for now, remember that we wanted to avoid the inconveniences given by using other existing data types to represent some piece of compound data!

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(check-expect (distance-to-0 (point 0 5)) 5)
(check-expect (distance-to-0 (point 7 0)) 7)

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(define (distance-to-0 ap)
  (sqrt
    (+ (sqr (point-x ap))
        (sqr (point-y ap))))))
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 2. One selector per field, which extracts the value of the field from a structure instance; and
 3. One structure predicate, which, like ordinary predicates, distinguishes instances from all other kinds of values.

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2. The selectors per field are `(point-x point-val)` and `(point-y point-val)`. The general form of a selector for a specific field is `(struct-name-field-name val)`
3. A predicate for checking types is automatically created, for example: `(point? point-val)` and in general a predicate `struct?` is created.

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- **Sample Problem** Develop a structure type definition for a program that deals with bouncing balls,. The balls location is a single number, namely the distance of pixels from the top. Its constant speed is the number of pixels it moves per clock tick. Its velocity is the speed plus the direction in which it moves.

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- Let's first consider defining a 2D vector struct as follows:
(`struct` vector [delta-x delta-y])
- Now, we can represent a ball as a point (which only has positive components) and a vector (which can have negative components): (`struct` 2D-ball position vec)

Other Representations

Our 2D Ball struct has nested occurrences of other structs. This is a natural thing, and even recursive descriptions of data are natural, i.e. linked lists and binary trees. But we can also consider using a *flat representation* for our 2D Ball, which doesn't nest structs.

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- Although valid, I think it's better to keep representations natural and just nest things, barring performance concerns.
- Let's talk about defining data definitions for structs. We must specify the form of the struct and the types of its field and provide an interpretation of what each of the fields represents. Here's how we do this for our point struct:

Other Representations

Our 2D Ball struct has nested occurrences of other structs. This is a natural thing, and even recursive descriptions of data are natural, i.e. linked lists and binary trees. But we can also consider using a *flat representation* for our 2D Ball, which doesn't nest structs.

- (`struct` 2D-ball [x y delta-x delta-y])
- Although valid, I think it's better to keep representations natural and just nest things, barring performance concerns.
- Let's talk about defining data definitions for structs. We must specify the form of the struct and the types of its field and provide an interpretation of what each of the fields represents. Here's how we do this for our point struct:

```
(define-struct point [x y])
; A Point is a structure:
;   (point Number Number)
; interpretation a point x pixels from left, y from top
```



Computing With Structures

As mentioned, we could have use tuples instead of structs to represent compound data, but remembering to access the name field of a person struct is a lot easier than remembering to project out the 7th element in some n-tuple (assuming $n_i=7$).

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- (`struct` centry [name home office cell])

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- Using a “key” to unlock the wrong box raises a runtime error
`(centry-name (point 1 2))` \hookrightarrow **entry-name:expects a centry, given (point 42 5)**

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- **Interpretation** - the action of explaining the meaning of something.
- **Denotation** - the object or concept to which a term refers, or the set of objects of which a predicate is true.

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- My definition - A formal language that has a computable semantics specifying the denotation of a “sentence” written in the language. This denotation can be given by compilation into some other formal language, or by a direct interpretation.

Some Important People



Kurt Gödel



Alan Turing



Alonzo Church

Some Important People



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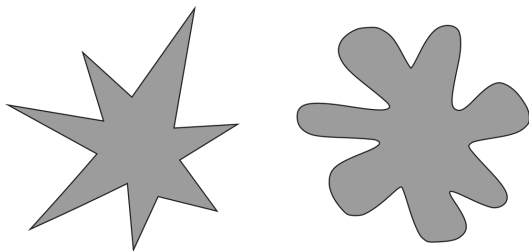


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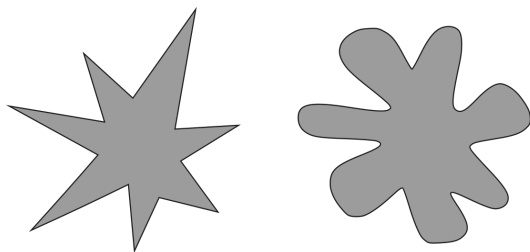
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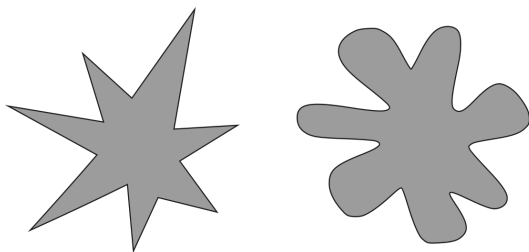
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Natural Interpretations?

Here's a fun little experiment. Look at these two shapes:



- Which of these shapes is named Bouba and which Kiki?
- This is likely due to some physical attributes of sound, but our strong preference for naming the round one Bouba and the sharp one Kiki shows that humans have **innate preferences** about the *naming* and *representation of things*.

Interpreting Structure

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- Interestingly, we can give 2 interpretations, depending on if the ball is moving vertically (interpretation 1) or horizontally (interpretation 2)

Interpreting Structure (cont.)

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- Consider the ball that can move in two dimensions.
- Since the ball relies on a vector struct, it is important to make sure that the vector also has an interpretation.

```
; A Ball-2d is a structure:  
;   (ball Point Vel)  
; interpretation a 2-dimensional position and velocity
```

```
(define-struct vel [deltax deltay])  
; A Vel is a structure:  
;   (vel Number Number)  
; interpretation (make-vel dx dy) means a velocity of  
; dx pixels [per tick] along the horizontal and  
; dy pixels [per tick] along the vertical direction
```

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- The T just communicates that we are defining linked lists that work over any type (*parametric polymorphism* otherwise known as *generics* in Java)

Structs and Program Design

Now we need to consider designing programs using structs.

Sample Problem Your team is designing an interactive game program that moves a red dot across a image canvas and allows players to use the mouse to reset the dot. Here is how far you got together:

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Sample Problem Your team is designing an interactive game program that moves a red dot across a image canvas and allows players to use the mouse to reset the dot. Here is how far you got together:

```
(define MTS (empty-scene 100 100))  
(define DOT (circle 3 "solid" "red"))
```

; A Point represents the state of the world.

; Point -> Point

```
(define (main p0)  
  (big-bang p0  
    [on-tick x+]  
    [on-mouse reset-dot]  
    [to-draw scene+dot]))
```

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(check-expect (scene+dot (point 10 20))
               (place-image DOT 10 20 MTS))
(check-expect (scene+dot (point 88 73))
               (place-image DOT 88 73 MTS))
```

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-
- Testing this is uninteresting, so let's consider if we were asked to define the x+ function, which takes in a Point and returns a new Point with an x-coordinate that is 3 units further to the right of the old point.

Designing `x+`

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- When carrying out step 2, recall that x+ handles clock ticks:

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```

- To take inventory we project out the x and y fields from our point, as usual:

```
(define (x+ p) (... (point-x p) ... (point-y p) ...))
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Designing $x+$ (cont.)

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(define (x+ p)  
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- If we had more fields than y, we simply are projecting out the old field as an argument when creating the new struct value.
- This adds a lot of boilerplate code...

Struct Boilerplate

We might want to define a function, `point-set-x` which takes in a point and a value and produces a new point where the x-coordinate is the given value and the y-coordinate is taken from the old point.

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- `point-set-x` is known as a *functional setter*, similar to a more traditional setter in languages like Java.
- However, defining an update operation on a complicated structure can get very complicated, and we can get around this using *lenses* (we may discuss this later in the course).

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```
(check-expect
  (reset-dot (point 10 20) 29 31 "button-down")
  (point 29 31))
(check-expect
  (reset-dot (point 10 20) 29 31 "button-up")
  (point 10 20))
```

-

Events Creating Structs (cont.)

From here, writing the skeleton and finishing coding are easy.

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- The Skeleton:

- For real this time:

```
(define (reset-dot p x y me)
  (cond
    [(mouse=? "button-down" me) (... p ... x y ...)]
    [else (... p ... x y ...)]))
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- The takeaway here is that our skeletons can end up being more complicated than the actual final version.
- This is especially true when we consider skeletoning out code for which a parameter is a struct.

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- We would have to write a field access for both of the underlying point structure's fields, along with field accesses for the underlying vector structure's fields.
- It would look like the following:

```
(define (complex-skeleton ball)
  (... (point-x (ball-position ball)) ...
        (... (point-y (ball-position ball)) ...
              (... (vec-delta-x (ball-vector ball)) ...
                    (... (vec-delta-y (ball-vector ball)) ...)))
```

Complex Skeletons

Consider a skeleton for a function whose input is a ball moving two dimensionally.

- We would have to write a field access for both of the underlying point structure's fields, along with field accesses for the underlying vector structure's fields.
- It would look like the following:

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(define (complex-skeleton ball)
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```

- For some of the classes you see in Java, skeletoning out code in such a manner is infeasible...

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- Of course, things are easier if we picked the write functions to add in our skeleton, but this keeps the structure of the skeleton much simpler.
- We will return to this point later in the course.

A Digression About Signatures

Signatures can tell us a lot about a function. I'll put some signatures up, and what kind of functions could we write for these signatures?

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- The idea that a function signature can tell you about the behavior of the function is an extremely powerful idea.

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;   "hello",  
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- If this is the domain of some function, we restricted ourselves to needing to handle three values.

Expanding the Universe

With itemizations we specified subsets of the existing data universe.



Expanding the Universe

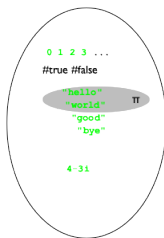
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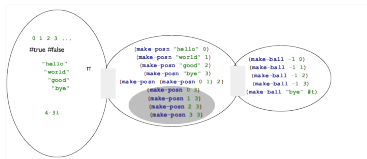
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- Without that, it is up to us programmers to validate that points are only constructed with valid arguments.
- This might mean creating a function
`(define (make-point x y) ...)` that checks that both `x` and `y` actually receive integers before calling the point constructor. More on this later.

Respect Interpretations (cont.)

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- For intervals, use the end points (if they are included) and at least one interior point.
- For itemizations, deal with each part separately
- For data definitions for structures, follow the natural language description; that is, use the constructor and pick an example from the data collection named for each field.

Back to the Drawing Board

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- **Sample Problem** Design a function that computes the distance of objects in a 3-dimensional space to the origin.
- The first step to our design process has a bigger change than was typical for previous revisions to our design process.

Step 1 and Structs

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- (1) When a problem calls for the representation of pieces of information that belong together or describe a natural whole, you need a structure type definition. It requires as many fields as there are relevant properties. An instance of this structure type corresponds to the whole, and the values in the fields correspond to its attributes.

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- (1) A data definition for a structure type introduces a name for the collection of instances that are legitimate. Furthermore, it must describe which kind of data goes with which field. Use only names of built-in data collections or previously defined data definitions.
- (1) In the end, we (and others) must be able to use the data definition to create sample structure instances. Otherwise, something is wrong with our data definition. To ensure that we can create instances, our data definitions should come with data examples.

Add Steps 2 and 3

Here's how we apply our step 1 changes to our sample problem:

```
(define-struct r3 [x y z])  
; An R3 is a structure:  
;   (make-r3 Number Number Number)  
  
(define ex1 (make-r3 1 2 13))  
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- (3) Your functional examples should use the examples generated by step (1):

```
(check/expect (r3-distance ex1) (sqrt 174))
(check/expect (r3-distance ex2) (sqrt 10))
```

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- (5) Use the selector expressions from the template when you define the function. Delete unneeded selections.
- (6) As usual, except that your tests are based on examples from step (1) and other examples.

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- Our state becomes (`struct` space-game [ufo tank])
- Let's come up with a data interpretation. Let's assume the ufo descends 2-dimensionally with random jumps to the left or right.

Space Game State

The state for our space game is relatively straightforward:

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; A SpaceGame is a structure:  
;   (make-space-game Posn Number).  
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; describes a configuration where the UFO is  
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- Also think about how we would randomly add enemies to a scene in a Geometry Wars style game.
- Continue to think about other kinds of games and what kind of state we need

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- Here is a start to our data interpretation:

```
(define-struct editor [pre post])  
; An Editor is a structure:  
;   (make-editor String String)  
; interpretation (make-editor s t) describes an editor  
; whose visible text is (string-append s t) with  
; the cursor displayed between s and t
```