

# Module Interface Specification for Lattice Boltzmann Solvers

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# 1 Revision History

Date	Version	Notes
Nov. 25, 2019	1.0	Initial Document

## 2 Symbols, Abbreviations and Acronyms

See CA Documentation for Lattice Boltzmann Solvers ([Michalski, a](#)).

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### 3 Introduction

The following document details the Module Interface Specifications for Lattice Boltzmann Solvers, which provides a library of services based on Lattice Boltzmann Methods (LBM). LBM are a family of fluid dynamics algorithms for simulating single-phase and multiphase fluid flows, often incorporating additional physical complexities ([Chen and Doolen, 1998](#)).

Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found [here](#) ([Michalski, b](#)).

### 4 Notation

[You should describe your notation. You can use what is below as a starting point. —SS]

The structure of the MIS for modules comes from [Hoffman and Strooper \(1999\)](#), with the addition that template modules have been adapted from [Ghezzi et al. \(2003\)](#). The mathematical notation comes from Chapter 3 of [Hoffman and Strooper \(1999\)](#). For instance, the symbol  $:=$  is used for a multiple assignment statement and conditional rules follow the form  $(c_1 \Rightarrow r_1 | c_2 \Rightarrow r_2 | \dots | c_n \Rightarrow r_n)$ .

The following table summarizes the primitive data types used by Lattice Boltzmann Solvers.

Data Type	Notation	Description
character	char	a single symbol or digit
integer	$\mathbb{Z}$	a number without a fractional component in $(-\infty, \infty)$
natural number	$\mathbb{N}$	a number without a fractional component in $[1, \infty)$
real	$\mathbb{R}$	any number in $(-\infty, \infty)$

The specification of Lattice Boltzmann Solvers uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, Lattice Boltzmann Solvers uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.



## 5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding Module	M1: Hardware Hiding Module
Behaviour-Hiding Module	M2: System Control Module
	M3: Input Reading Module
	M4: Input Checking Module
	M5: LBM Control Module
	M6: Streaming Module
	M7: Collision Module
	M8: Problem Module
	M9: Lattice Module
	M10: Boundary Module
Software Decision Module	M11: Output Module

Table 1: Module Hierarchy

## 6 MIS of M1: Hardware Hiding Module

The secrets of this module are the data structure and algorithms used to implement the virtual hardware.

### 6.1 Module

Hardware Hiding

### 6.2 Uses

N/A

### 6.3 Syntax

N/A

#### 6.3.1 Exported Constants

N/A

#### 6.3.2 Exported Access Programs

N/A

### 6.4 Semantics

N/A

#### 6.4.1 State Variables

N/A

#### 6.4.2 Environment Variables

The module has external interaction with the environment when either the Output Module M11 (Section 16) or Input Reading Module M3 (Section 8) require its services for reading inputs or writing outputs.

#### 6.4.3 Assumptions

M11 (Section 16) or M3 (Section 8) have called the modules services.

#### **6.4.4 Access Routine Semantics**

N/A

#### **6.4.5 Local Functions**

N/A

## 7 MIS of M2: System Control Module

The secret of this module is the algorithm to control Lattice Boltzmann Solvers.

### 7.1 Module

System Control

### 7.2 Uses

- Output (Section 16)
- Input Reading (Section 8)
- LBM Control (Section 10)
- Problem Parameter (Section 13)

### 7.3 Syntax

#### 7.3.1 Exported Constants

N/A

#### 7.3.2 Exported Access Programs

N/A

### 7.4 Semantics

#### 7.4.1 State Variables

[Not all modules will have state variables. State variables give the module a memory. —SS]

#### 7.4.2 Environment Variables

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

#### 7.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

#### 7.4.4 Access Routine Semantics

[accessProg —SS]():

- transition: [if appropriate —SS]
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### 7.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

## 8 MIS of M3: Input Reading Module

The secret of this module is the algorithm that gathers the input data.

### 8.1 Module

Input Reading

### 8.2 Uses

- Input Checking
- Hardware Hiding

### 8.3 Syntax

#### 8.3.1 Exported Constants

*LIBRARY\_IN*: string  
*DIMENSIONS\_IN*:  $\mathbb{N}$   
*VEL\_DIR\_IN*:  $\mathbb{N}$   
*INPUTS*: array of strings,  $\mathbb{R}$ ,  $\mathbb{N}$

#### 8.3.2 Exported Access Programs

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inputArray	string	array of strings, $\mathbb{R}$ , $\mathbb{N}$	-
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### 8.4 Semantics

#### 8.4.1 State Variables

Input\_Location: string

#### 8.4.2 Environment Variables

N/A

#### 8.4.3 Assumptions

The System Control Module M2 (Section 7) has called the inputArray function of this module.

#### 8.4.4 Access Routine Semantics

[accessProg —SS]():

- transition: [if appropriate —SS]
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### 8.4.5 Local Functions

Name	In	Out	Exceptions
open	string	object	NOT_FOUND
readline	object	-	ERR_READ NO_LINES

## 9 MIS of M4: Input Checking Module

This secret of this module is the algorithm that checks if input values fall within allowable parameters.

### 9.1 Module

Input Checking

### 9.2 Uses

N/A

### 9.3 Syntax

#### 9.3.1 Exported Constants

N/A

#### 9.3.2 Exported Access Programs

Name	In	Out	Exceptions
verifyInputs	string array	boolean	OUT_OF_BOUNDS UNKN_PARM

### 9.4 Semantics

#### 9.4.1 State Variables

*LIBRARIES*: set of strings: {pyLBM}

*DIMENSIONS*: set of  $\mathbb{N}$ : {2}

*VEL\_DIRS*: set of  $\mathbb{N}$ : {9}

*REYNOLDS\_MIN*:  $\mathbb{R}$ : {0.001}

*REYNOLDS\_MAX*:  $\mathbb{R}$ : {5000}

*DENSITY\_MIN*:  $\mathbb{R}$ : {0.0708}

*DENSITY\_MIN*:  $\mathbb{R}$ : {13.6}

*BULK\_VIS\_MIN*:  $\mathbb{R}$ : {0.0001}

*BULK\_VIS\_MIN*:  $\mathbb{R}$ : {20000}

*SHEAR\_VIS\_MIN*:  $\mathbb{R}$ : {0.001}

*SHEAR\_VIS\_MIN*:  $\mathbb{R}$ : {20000}

*TIME\_MIN*:  $\mathbb{N}$ : {1}

*LIBRARY\_IN*: string

*DIMENSIONS\_IN*:  $\mathbb{N}$

*VEL\_DIR\_IN*:  $\mathbb{N}$



$Re: \mathbb{R}$   
 $\rho: \mathbb{R}$   
 $\eta_b: \mathbb{R}$   
 $\eta_s: \mathbb{R}$   
 $t: \mathbb{N}$   
 $a: \mathbb{R}$   
 $c_s: \mathbb{R}$   
 $e: \mathbb{R}$   
 $F: \mathbb{R}$   
 $kg: \mathbb{R}$   
 $A: \mathbb{R}$   
 $u: \mathbb{R}$

### 9.4.2 Environment Variables

N/A

### 9.4.3 Assumptions

The Input Reading Module M3 (Section 8) has called the `verifyInputs` function of this module.

### 9.4.4 Access Routine Semantics

`[accessProg —SS]()`:

- transition: `[if appropriate —SS]`
- output: `[if appropriate —SS]`
- exception: `[if appropriate —SS]`

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

### 9.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

## 10 MIS of M5: LBM Control Module

The secret of this module is the algorithm which controls the LBM library.

### 10.1 Module

LBM Control

### 10.2 Uses

- Streaming
- Collision

### 10.3 Syntax

#### 10.3.1 Exported Constants

#### 10.3.2 Exported Access Programs

Name	In	Out	Exceptions
vortVal	array of strings, $\mathbb{R}$ , $\mathbb{N}$	array of $\mathbb{R}$	-

### 10.4 Semantics

#### 10.4.1 State Variables

array of vorticity vector values

#### 10.4.2 Environment Variables

N/A

#### 10.4.3 Assumptions

The System Control Module M2 (Section 7) has called the vortVal function of this module.

#### 10.4.4 Access Routine Semantics

[[accessProg](#) —SS]():

- transition: [[if appropriate](#) —SS]
- output: [[if appropriate](#) —SS]
- exception: [[if appropriate](#) —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### **10.4.5 Local Functions**

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

## 11 MIS of M6: Streaming Module

The secret of this module is the algorithm to calculate the streaming pf particles.

### 11.1 Module

Streaming

### 11.2 Uses

N/A

### 11.3 Syntax

#### 11.3.1 Exported Constants

N/A

#### 11.3.2 Exported Access Programs

Name	In	Out	Exceptions
bgkCollision	array of strings, $\mathbb{R}$ , $\mathbb{N}$	$\mathbb{R}$	NAN_ERROR

### 11.4 Semantics

#### 11.4.1 State Variables

N/A

#### 11.4.2 Environment Variables

N/A

#### 11.4.3 Assumptions

The LBM Control Module M5 (Section 10) has called the bgkCollision function of this module.

#### 11.4.4 Access Routine Semantics

[accessProg —SS]():

- transition: [if appropriate —SS]
- output: [if appropriate —SS]

- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### 11.4.5 Local Functions

Name	In	Out	Exceptions
relatUpdate	array of strings, $\mathbb{R}$ , $\mathbb{N}$	$\mathbb{R}$	NAN_ERROR
equilDistrib	array of strings, $\mathbb{R}$ , $\mathbb{N}$	$\mathbb{R}$	NAN_ERROR
relaxRate	$\mathbb{R}$ , $\mathbb{N}$	$\mathbb{R}$	NAN_ERROR

## 12 MIS of M7: Collision Module

The secret of this module is the algorithm to calculate the collision of particles.

### 12.1 Module

Collision

### 12.2 Uses

N/A

### 12.3 Syntax

#### 12.3.1 Exported Constants

N/A

#### 12.3.2 Exported Access Programs

Name	In	Out	Exceptions
streamingFunc	array of strings, $\mathbb{R}$ , $\mathbb{N}$	$\mathbb{R}$	NAN_ERROR

### 12.4 Semantics

#### 12.4.1 State Variables

N/A

#### 12.4.2 Environment Variables

N/A

#### 12.4.3 Assumptions

The LBM Control Module M5 (Section 10) has called the streamingFunc function of this module.

#### 12.4.4 Access Routine Semantics

[accessProg —SS]():

- transition: [if appropriate —SS]
- output: [if appropriate —SS]

- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### 12.4.5 Local Functions

Name	In	Out	Exceptions
prbDnsFunc	array of $\mathbb{R}$ , $\mathbb{N}$	$\mathbb{R}$	NAN_ERROR

## 13 MIS of M8: Problem Module

The secret of this module is the structure of the LBM input parameters.

### 13.1 Module

Problem Parameter

### 13.2 Uses

- Lattice
- Boundary

### 13.3 Syntax

#### 13.3.1 Exported Constants

N/A

#### 13.3.2 Exported Access Programs

Name	In	Out	Exceptions
formatInput	array of $\mathbb{R}$ , $\mathbb{N}$	array of $\mathbb{R}$ , $\mathbb{N}$	-

### 13.4 Semantics

#### 13.4.1 State Variables

N/A

#### 13.4.2 Environment Variables

N/A

#### 13.4.3 Assumptions

The System Control Module M2 (Section 7) has called the formatInput function of this module.

#### 13.4.4 Access Routine Semantics

[accessProg —SS]():

- transition: [if appropriate —SS]



- output: [if appropriate —SS]
- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### **13.4.5 Local Functions**

N/A

## 14 MIS of M9: Lattice Module

The secret of this module is the structure of the lattice model.

### 14.1 Module

Lattice

### 14.2 Uses

N/A

### 14.3 Syntax

#### 14.3.1 Exported Constants

N/A

#### 14.3.2 Exported Access Programs

Name	In	Out	Exceptions
setLattice	array of $\mathbb{R}$	array of $\mathbb{N}$	No_LATTICE

### 14.4 Semantics

#### 14.4.1 State Variables

Array of tuples  $\langle \mathbb{R} \rangle \langle \mathbb{R} \rangle \langle \mathbb{R}, \mathbb{N}_0 \dots \mathbb{R}_n \rangle$

#### 14.4.2 Environment Variables

N/A

#### 14.4.3 Assumptions

The Problem Module M8 (Section 13) has called the setLattice function of this module.

#### 14.4.4 Access Routine Semantics

$[\text{accessProg} \text{---SS}]()$ :

- transition:  $[\text{if appropriate} \text{---SS}]$
- output:  $[\text{if appropriate} \text{---SS}]$
- exception:  $[\text{if appropriate} \text{---SS}]$

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### **14.4.5 Local Functions**

N/A

## 15 MIS of M10: Boundary Module

The secret of this module is the structure of the model boundary.

### 15.1 Module

Boundary

### 15.2 Uses

N/A

### 15.3 Syntax

#### 15.3.1 Exported Constants

N/A

#### 15.3.2 Exported Access Programs

Name	In	Out	Exceptions
boundFunc	array of $\mathbb{R}$	array of $\mathbb{R}$	-

### 15.4 Semantics

#### 15.4.1 State Variables

N/A

#### 15.4.2 Environment Variables

N/A

#### 15.4.3 Assumptions

The Problem Module M8 (Section 13) has called the boundFunc function of this module.

#### 15.4.4 Access Routine Semantics

[accessProg —SS]():

- transition: [if appropriate —SS]
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### **15.4.5 Local Functions**

N/A

## 16 MIS of M11: Output Module

The algorithm to convert the LBM output into an image.

### 16.1 Module

Output

### 16.2 Uses

- System Control Module

### 16.3 Syntax

#### 16.3.1 Exported Constants

N/A

#### 16.3.2 Exported Access Programs

Name	In	Out	Exceptions
imageFunc	array of $\mathbb{R}$	image format	-

### 16.4 Semantics

#### 16.4.1 State Variables

N/A

#### 16.4.2 Environment Variables

N/A

#### 16.4.3 Assumptions

The System Control Module M2 (Section 13) has called the imageFunc function of this module.

#### 16.4.4 Access Routine Semantics

[accessProg —SS]():

- transition: [if appropriate —SS]
- output: [if appropriate —SS]

- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### **16.4.5 Local Functions**

N/A

## References

- Shiyi Chen and Gary D Doolen. Lattice Boltzmann method for fluid flows. *Annual review of fluid mechanics*, 30(1):329–364, 1998.
- Carlo Ghezzi, Mehdi Jazayeri, and Dino Mandrioli. *Fundamentals of Software Engineering*. Prentice Hall, Upper Saddle River, NJ, USA, 2nd edition, 2003.
- Daniel Hoffman and Paul Strooper. Software Design, Automated Testing, and Maintenance—A Practical Approach. 1999.
- Peter Michalski. Lattice Boltzmann Solvers - CA, a. URL <https://github.com/peter-michalski/LatticeBoltzmannSolvers/blob/master/docs/SRS/CA.pdf>.
- Peter Michalski. Lattice Boltzmann Solvers, b. URL <https://github.com/peter-michalski/LatticeBoltzmannSolvers>.



## 17 Appendix

[Extra information if required —SS]