

Lattice Boltzmann Solvers

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1 Revision History

Date	Version	Notes
Oct. 7,2019	1.0	Initial Document
Oct. 20,2019	1.1	First Issues Fixed + 10.4 Added
Nov. 8,2019	2.0	Iteration One Issues Fixed

2 Reference Material

This section records information for easy reference.

2.1 Table of Units

Throughout this document SI (Système International d’Unités) is employed as the unit system. In addition to the basic units, several derived units are used as described below. For each unit, the symbol is given followed by a description of the unit and the SI name.

symbol	unit	SI
m	length	metre
kg	mass	kilogram
s	time	second
F	force	newton
cm	length	centimetre
g	mass	gram
Pa	pressure	pascal

2.2 Table of Symbols

The table that follows summarizes the symbols used in this document along with their units. The choice of symbols was made to be consistent with Lattice Boltzmann Method literature and with existing documentation for Lattice Boltzmann Methods. The symbols are listed in alphabetical order. Boldface represents vector units.

symbol	unit	description
e	$\frac{m}{s}$	velocity
η	$\text{Pa} \cdot s$	viscosity
A	m^2	cross-sectional area
γ	$\frac{1}{s}$	velocity gradient
τ	N/A	relaxation rate
\mathbf{x}	N/A	position vector
l	m	characteristic length of the system
t	s	time
f	N/A	distribution function
Ω	N/A	collision operator
f^{eq}	N/A	equilibrium distribution function

k	N/A	velocity direction
ρ	$\frac{g}{cm^3}$	fluid density
w	N/A	weight coefficient (implementation specific)
\mathbf{u}	N/A	macroscopic velocity of fluid vector
D	N/A	signifies the dimension component of lattice model
Q	N/A	signifies number of velocity directions of lattice model
σ	N/A	variable number of dimensions in the lattice model
κ	N/A	variable number of velocity directions (linkages) of lattice model
\mathbb{R}	N/A	real numbers
\mathbb{N}	N/A	natural numbers
\mathbf{c}_k	N/A	unit vector along the lattice streaming direction
c_s	$\frac{m}{s}$	speed of sound
Re	N/A	Reynolds number
ζ	N/A	Turbulence
?	N/A	Unknown Value

2.3 Abbreviations and Acronyms

symbol	description
1D	1-Dimensional
2D	2-Dimensional
3D	3-Dimensional
A	Assumption
AHP	Analytic Hierarchy Process
CA	Commonality Analysis
DD	Data Definition
GS	Goal Statement
LBM	Lattice Boltzmann Methods
LBS	Lattice Boltzmann Solvers
LC	Likely Change
MG	Module Guide
MIS	Module Interface Specification
MPI	Message Passing Interface
MTBF	Mean Time Between Failures
NFR	Non-Functional Requirement
NNF	Non-Newtonian Fluid
OTS	Off The Shelf (LBM Solutions)
R	Requirement
T	Theoretical Model
VnV	Verification and Validation

Contents

1	Revision History	i
2	Reference Material	ii
2.1	Table of Units	ii
2.2	Table of Symbols	ii
2.3	Abbreviations and Acronyms	iv
3	Introduction	3
3.1	Purpose of Document	3
3.2	Scope of the Family	3
3.3	Characteristics of Intended Reader	4
3.4	Organization of Document	4
4	General System Description	5
4.1	Potential System Contexts	5
4.2	Potential User Characteristics	5
4.3	Potential System Constraints	5
5	Commonalities	6
5.1	Background Overview	6
5.2	Terminology and Definitions	7
5.3	Data Definitions	8
5.4	Goal Statements	10
5.5	Theoretical Models	11
6	Variabilities	14
6.1	Assumptions	14
6.2	Calculation	15
6.3	Output	16
7	Requirements	17
7.1	Family of Functional Requirements	17
7.2	Non-Functional Requirements	18
8	Likely Changes	20
9	Traceability Matrices and Graphs	21
10	Appendix	25
10.1	Symbolic Parameters	25
10.2	Off The Shelf Solutions	25
10.3	Coefficient Weights for Equilibrium Distribution Function	27

10.4 First Stage of Implementation	27
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3 Introduction

This document provides a Commonality Analysis (CA) for a family of Lattice Boltzmann Solvers (LBS), which provide services based on Lattice Boltzmann Methods (LBM). LBM are a family of fluid dynamics algorithms for simulating single-phase and multiphase fluid flows, often incorporating additional physical complexities (Chen and Doolen [9]). They consider the behaviours of a collection of particles as a single unit at the mesoscopic scale. These methods predict the positional probability of a collection of particles moving through a lattice structure. Off the shelf (OTS) Lattice Boltzmann Solvers (LBS) allow for a range of fluid and physical model input parameters, computational parameters, and output parameters as outlined in Section 10.2. The following subsections of this introduction will outline the purpose of this document, a general scope of the family of LBS, the characteristics of the intended reader, and finally an outline of the rest of this document.

3.1 Purpose of Document

The purpose of this document is to provide general information on currently available LBS solutions, including their commonalities and variabilities, as well as a baseline understanding of the model and structure of abstract LBM. The information provided here will be used in the development of the design of a solution providing services of a family of LBS.

3.2 Scope of the Family

The family of LBS will model one or more fluids as they pass through a boundary, modeled by a lattice. Fluids with any properties can be modeled, however only those properties that are accepted as inputs by the LBS will affect the model results. The calculation of the LBM distribution function will use 1D, 2D, and 3D computational models, and will output the data into memory and render it on a screen in up to 3D imaging. The output results can also be rendered to a file.

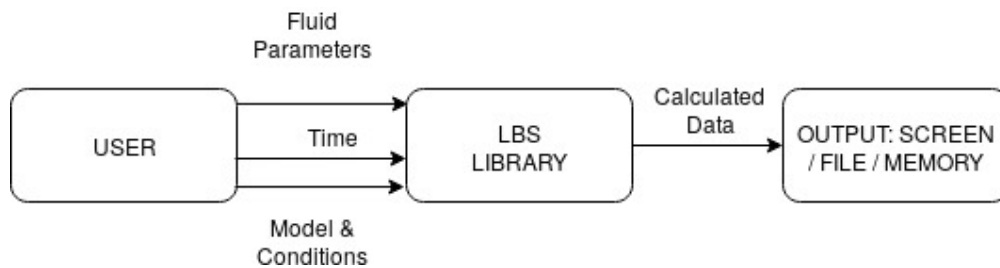


Figure 1: LBS Family Scope

3.3 Characteristics of Intended Reader

The intended reader of this document should have an undergraduate understanding of software requirements specifications and software design principles. Ideally, they will also have at least an undergraduate Level 3 physics understanding, including of lattice structures and fluid dynamics.

3.4 Organization of Document

This document is organized following a template for a CA for scientific computing software proposed by Smith [27]. It follows a standard pattern of presenting a general system description, commonalities, variabilities, and the requirements for a family of LBS. The goal statements of the family of LBS, found in Section 5.4, are refined to the theoretical models in Section 5.5. Variabilities within the family are found in Section 6. Tables of OTS solution commonalities and variabilities are found in Section 10.2.

4 General System Description

This section identifies the interfaces between the system and its environment, describes the potential user characteristics, and lists the potential system constraints.

4.1 Potential System Contexts

- User Responsibilities:
 - The user must provide the system with correctly formatted physical model parameters.
 - The user must select the desired mathematical model for the computation.
 - The user must select the desired format of output for the model.
- Lattice Boltzmann Solvers Responsibilities:
 - Detect data type mismatch, such as a negative number instead of a positive number for a parameter (for example, A cannot accept negative values).
 - Initialize the correct data types and data structures for the model.
 - Perform the calculations to predict the distribution of fluid particles over time.
 - Store the distribution function output data.
 - Store calculated fluid parameters over time.
 - Visually model the results of the distribution function.
 - Store the calculation results in a file and/or in memory.
 - Detect errors during parameter input, model calculation, or model output; store the errors in a file and show the error to the user.
 - Recover from error states, such as those that develop from division by zero or a buffer overflow.

4.2 Potential User Characteristics

The end user of Lattice Boltzmann Solvers should ideally have an understanding of undergraduate Level 1 physics and fluid dynamics. The ideal end user characteristics may differ between the members of the family of solvers. For example, a user of HemeLB, an off the shelf LBM solution for simulating blood flow, would ideally have an understanding of phlebology.

4.3 Potential System Constraints

The parallel nature of LBS prefers operating and hardware systems that can handle concurrency and large amounts of data. Modern operating systems and computer hardware platforms are suggested. Memory should be scaled to the requirements of the desired LBS library, and decomposition technique.

5 Commonalities

5.1 Background Overview

As LBS model fluid dynamics within a boundary using a predefined lattice structure, the methods rely on a two step calculation process. The first process is streaming, where the particles move along the lattice via links. The second process is collision, where energy and momentum is transferred among particles that collide [6]. There are many standardized lattice models - individual solvers within the family might only use a subset of them. The LBM uses the initial parameters of the fluid to find the probability of where along the lattice linkages a group of particles are most likely to travel. It then moves the particles into the next node, and transfers the energy and momentum if a collision occurs. Then the process repeats for the duration of the modeling instance.

5.2 Terminology and Definitions

This subsection provides a list of terms that are used in the subsequent sections and their meaning, with the purpose of reducing ambiguity and making it easier to correctly understand the requirements:

- **Correctness:** The degree to which a system or component is free from faults in its specification, design, and implementation (IEEE Std 610.12-1990 [14]).
- **Maintainability:** The ease with which a software system or component can be modified to correct faults, improve performance or other attributes, or adapt to a changed environment (IEEE Std 610.12-1990 [14]).
- **Performance:** The degree to which a system or component accomplishes its designated functions within given constraints, such as speed, accuracy, or memory usage (IEEE Std 610.12-1990 [14]).
- **Portability:** The ease with which a system or component can be transferred from one hardware or software environment to another (IEEE Std 610.12-1990 [14]).
- **Reliability:** The ability of a system or component to perform its required functions under stated conditions for a specified period of time (IEEE Std 610.12-1990 [14]).
- **Reusability:** The degree to which a software module or other work product can be used in more than one computer program or software system (IEEE Std 610.12-1990 [14]).
- **Robustness:** The degree to which a system or component can function correctly in the presence of invalid inputs or stressful environmental conditions (IEEE Std 610.12-1990 [14]).
- **Scalability:** The ability of the system to cope with increasing numbers of users without reducing overall QoS that is delivered to any user (Sommerville [28]).
- **Understandability:** The ease of understanding the software system (Uchida and Shima [29]).
- **Usability:** The ease with which a user can learn to operate, prepare inputs for, and interpret outputs of a system or component (IEEE Std 610.12-1990 [14]).
- **Velocity Directions (Q):** The number of links connecting to each lattice node in the chosen model from neighbouring nodes. All nodes in a chosen lattice model will have the same number of links. A single link will connect between two adjacent nodes.
- **D#Q# Convention:** This signifies the dimension (D) and velocity direction (Q) components of a lattice model. For example, D2Q9 signifies a 2D lattice model with 9 velocity directions out of each node.

5.3 Data Definitions

This section collects and defines all the data needed to build the instance models. The dimension of each quantity is also given.

Number	DD1
Label	Velocity
Symbol	v
SI Units	$\frac{m}{s}$
Equation	$v = \frac{dr}{dt}$
Description	Velocity is the distance that an object moves relative to time. r is the distance (m) in change for our change in time t of units (s).
Sources	Mohamad [20]
Ref. By	T1 T3 T4

Number	DD2
Label	Viscosity
Symbol	η
SI Units	$Pa \cdot s$
Equation	$\eta = \frac{F/A}{\gamma}$
Description	Viscosity is the measure of resistance to deformation. F is the applied force (N), A is the cross-sectional area (m^2), and γ is the velocity gradient.
Sources	vis [3]
Ref. By	T4 DD3 A1

Number	DD3
Label	Relaxation Rate Towards Equilibrium
Symbol	τ
SI Units	NA
Equation	$\tau = \frac{12\eta\Delta t}{\Delta \mathbf{x}^2} + \frac{1}{2}$
Description	The relaxation rate defines how quickly the particles recover to equilibrium state. Adjusting this method in the implementation allows for the simulation of complex physical phenomena, specifically concerning the fluid media. η is the viscosity of the fluid, t is the time interval (s), and \mathbf{x} is the position vector.
Sources	Bolton [8]
Ref. By	T1 A1 A5

Number	DD4
Label	Velocity Gradient
Symbol	γ
SI Units	$\frac{1}{s}$
Equation	$\gamma = \frac{de}{dz}$
Description	Velocity gradient is the difference in velocity between adjacent fluids. de represents the difference in velocities of the fluids and dz is the distance of the two velocities.
Sources	vis [3]
Ref. By	DD2 A1

Number	DD5
Label	Fluid Density
Symbol	ρ
SI Units	$\frac{g}{cm^3}$
Equation	$\rho = \frac{g}{cm^3}$
Description	Density is the ratio of mass to volume of a material. g is the mass and cm^3 is the volume.
Sources	den [1]
Ref. By	T3 T4 A1

5.4 Goal Statements

Given the lattice model, boundary conditions, simulation time, fluid characteristics, and forces, the goal statements are:

G1 - Location: Predict the location of all fluid particles in the lattice over time.

G2 - Velocity: Predict the velocity of all fluid particles within the lattice over time.

G3 - Fluid Pressure: Predict the pressure of all fluid particles within the lattice over time.

5.5 Theoretical Models

This section focuses on the general equations and laws that Lattice Boltzmann Solvers are based on.

Number	T1
Label	Boltzmann Transport Equation
Equation	$f(\mathbf{x} + \mathbf{e}dt, \mathbf{e} + \frac{\mathbf{F}}{kg}dt, t + dt)d\mathbf{x}d\mathbf{e} - f(\mathbf{x}, \mathbf{e}, t)d\mathbf{x}d\mathbf{e} = \Omega(f)d\mathbf{x}d\mathbf{e}$
Description	<p>This equation determines the statistical description of a group of particles. The left part of the equation, $f(\mathbf{x} + \mathbf{e}dt, \mathbf{e} + \frac{\mathbf{F}}{kg}dt, t + dt)d\mathbf{x}d\mathbf{e}$, represents the distribution function result after an external force \mathbf{F} is applied. The middle function, $f(\mathbf{x}, \mathbf{e}, t)d\mathbf{x}d\mathbf{e}$, represents the distribution function result before the external force is applied. The distribution function f represents the probability that a set of particles will be at a specific location of the lattice at a specified time. The right hand side of the equation represents the collision operator, Ω.</p> <p>The variable \mathbf{x} represents the vector of the particles within the lattice, \mathbf{e} is velocity $\frac{\text{m}}{\text{s}}$, t is time (s), \mathbf{F} is force (N), kg is mass. This equation can be further developed for specific instances.</p>
Source	Bolton [8] Mohamad [20]
Ref. By	A5

Number	T2
Label	Bhatnagar-Gross-Krook Collision Operator
Equation	$\Omega = \frac{\Delta t}{\tau}(f^{eq}(r, t) - f(r, t))$
Description	The above equation is a mathematical operator that preserves continuity for a discretized model. τ is the relaxation rate towards equilibrium and should be in the range of 0.5 - 2.0. It is related to viscosity as outlined in DD. f^{eq} is the equilibrium particle probability distribution function. f is the particle probability distribution function. This equation can be further developed for specific instances. Several fluids in the instance model can be modeled by this equation.
Source	Bolton [8] Mohamad [20]
Ref. By	T1 A1 A5

Number	T3
Label	Equilibrium Distribution Function
Equation	$f_k^{eq} = pw_k[1 + \frac{2\mathbf{c}_k\mathbf{u}-\mathbf{u}\mathbf{u}}{2c_s^2} + \frac{(\mathbf{c}_k\mathbf{u})^2}{2c_s^4}] + O(u^2)$
Description	The above equation captures the probability distribution of the particles. Adjusting this method in the implementation allows for the simulation of complex physical phenomena, including geometry of the boundary. ρ is the fluid density ($\frac{g}{cm^3}$). w is the weighting coefficient for the lattice model as the fluid flows through a lattice structure. The weighting coefficients are standard. k is the discretized velocity direction, referring to the directions of the chosen lattice model. \mathbf{c}_k is the unit vector along the lattice streaming direction. \mathbf{u} is the macroscopic velocity of the fluid, which is a vector field of velocity at a specific position and time. c_s is the speed of sound, a constant. This equation can be further developed for specific instances.
Source	Bolton [8] Mohamad [20]
Ref. By	T2 A1 A2 A3 A4 A5

Number	T4
Label	Reynolds Number
Equation	$Re = \frac{\rho l v}{\eta}$
Description	The ratio of inertial resistance to viscous resistance for a flowing fluid. ρ is the density of the fluid, v is the velocity, l is the characteristic length of the system, and η is the viscosity
Sources	see [2]
Ref. By	

6 Variabilities

6.1 Assumptions

- A1: One or more fluids with distinct properties can be simultaneously released into the boundary. The fluid parameters are defined in DD2 and DD5. They are used in DD3, and in DD4.
- A2: The dimensions of boundary conditions, including flow obstacles, may vary.
- A3: The fluid flows through space via a lattice structure, moving between lattice nodes via linkages (Q).
- A4: Weight coefficients are standard for each lattice model. See the Table 11. [I like this variability. It isn't really connected to the rest of the document, since it doesn't tell me where weight coefficients are used, but it does tell me of the discrete set of choices that people use for the values. We can make it a bit better when we add a data definition for the discretization. (I'll be discussing this discretization DD separately.) —SS]
- A5: The user will select the desired model prior to running the simulation. The position vector of DD3 is influenced by this.

Goal	Model	A1	A2	A3	A4	A5
G1	T1					✓
G1	T2	✓				✓
G1	T3	✓	✓	✓	✓	✓
G1	T4	✓	✓	✓	✓	✓
G2	T1					✓
G2	T2	✓				✓
G2	T3	✓	✓	✓	✓	✓
G2	T4	✓	✓	✓	✓	✓
G3	T1					✓
G3	T2	✓				✓
G3	T3	✓				✓
G3	T4			✓	✓	✓

Table 1: Assumption Relationship to Goals and Models

6.2 Calculation

Variability	Parameter of Variation	Binding Time
destination for output	Set of {file, screen, memory}	compile
boundary parameters	Set of {deflective, non deflective}	compile
dimension	Set of {1D, 2D, 3D}	compile
# of velocity directions	Set of {2, 3, 5, 9, 13, 15, 19, 27}	compile

Table 2: Input Variabilities

Variability	Parameter of Variation	Binding Time
computational model (see Section 4.3)	D1Q2, D1Q3, D1Q5, D2Q9, D2Q13, D2Q15, D3Q15, D3Q15i, D3Q19, D3Q19+, D3Q27	compile
decomposition technique (see Section 4.3)	Set of {ParMETIS library, PT_Scotch library, block-wide decompo- sition, domain decomposition, spinoidal decomposition}	compile
coefficient weights	Set of $\{0 < \mathbb{R} < 1\}; \sum \mathbb{R} = 1$	compile
input check	boolean (false if input satisfies in- put assumptions)	compile
encoding of output	Set of {binary, text}	compile
exception check	boolean (false if no exception con- dition raised)	compile

Table 3: Calculation Variabilities

6.3 Output

Variability	Parameter of Variation	Binding Time
graphical model	Set of $\{2D, 3D\}; \sum \mathbb{R} = 1$	compile
fluid characteristics	$\{\text{wall pressure, flow velocity,}$ Set of fluid location, pressure gradient $\}$	run

Table 4: Output Variabilities

7 Requirements

This section provides the functional requirements, the business tasks that the software is expected to complete, and the nonfunctional requirements, the qualities that the software is expected to exhibit.

7.1 Family of Functional Requirements

- R1: The system shall read a set of input fluid parameters, listed in Table 2. These parameters will be used in calculations for T1, T2, and T3.
- R2: The system shall allow the user to select from a set of model and velocity direction parameters, listed in Table 2, as per A5. These models will be reflected in the calculations of T1.
- R3: The system shall verify that the inputs fall within the allowable parameters of variation, see Table 2.
- R4: The system shall instantiate required data types and structures for the selected model.
- R5: The system shall import the relevant coefficient weights for the selected model, as per A4. The weighting values can be found in Table 11. These models will be reflected in the calculations of T1.
- R6: The system shall calculate and store the predicted fluid parameters, iterating through streaming and collision processes over the desired model time.
- R7: The system shall output the results of the calculations in a manner consistent with the decisions made regarding variabilities.

7.2 Non-Functional Requirements

The following are non-functional requirements (NFRs), and their metrics, for a family of LBS. They are defined in Section 5.2:

1. Correctness: The allowable error of the output results, per module, will be less than the average error taken from the results of a sample of OTS solutions.
2. Maintainability: The system shall be documented with a Commonality Analysis (CA), Verification and Validation (VnV) plan, MG (Module Guide), MIS (Module Interface Specification), and User Guide.
3. Performance: The system shall be able to run modules faster than the pseudo-oracle pyLBM.
4. Portability: The system shall be able to run on macOS, Windows, and Linux operating systems.
5. Reliability: The mean time between failures (MTBF) will be longer than the average MTBF of a sample of the OTS solutions.
6. Reusability: Individual modules of the system can be removed and reused in other systems.
7. Robustness: The system shall behave reasonably in circumstances that were not anticipated in the requirements specification [12].
8. Scalability: The system must be able to support additional computational models.
9. Understandability: New users must easily understand which LBM models are available in ProgName.
10. Usability: Users will find the system easy to use.

The NFRs have been compared using a pairwise technique based on the Analytic Hierarchy Process (AHP), a decision making method. Each NFR has been compared to every other individual NFR and a professional judgment has been made by the author of this document as to which NFR of the pair has been prioritized in the OTS LBM solutions found in Section 10.2. The judgment is based on a test of the OTS solutions and a review of their documentation.

The results of the comparison are listed in Table 5 below. The comparison took into account the available documentation of current off the shelf LBS solutions, listed in Table 8, Table 9, and Table 10.

NFR/ NFR	1	2	3	4	5	6	7	8	9	10	Σ
1	-	1	1	1	1	1	1	1	1	1	9
2	0	-	0	1	0	1	1	1	0	0	4
3	0	1	-	1	0	1	0	1	1	1	6
4	0	0	0	-	0	0	0	0	0	0	0
5	0	1	1	1	-	1	1	1	1	1	8
6	0	0	0	1	0	-	0	0	0	0	1
7	0	0	1	1	0	1	-	1	1	0	5
8	0	0	0	1	0	1	0	-	0	0	2
9	0	1	0	1	0	1	0	1	-	0	4
10	0	1	0	1	0	1	1	1	1	-	6

Table 5: Pairwise Comparison of NFR

The following is a list of NFR by importance as found in the Table 5 pairwise comparison:

1. Correctness
2. Reliability
3. Performance and Usability
4. Robustness
5. Maintainability and Understandability
6. Scalability
7. Reusability
8. Portability

8 Likely Changes

- LC1: A family of LBS solvers will have 2D and 3D output. 1D output is not a common variability. See Table 8. The solvers follow the assumptions of A3, A4, A5.
- LC2: Wall pressure is not an output variability that is often needed. This may be removed from a family of LBS. See Table 10. The solvers follow the assumptions of A2, A3, A5.
- LC3: Spinoidal decomposition is most common among LBS family members and should be the standard for a library implementation. See Table 9.
- LC4: MPI is the standard parallel interface for LBS and should be the standard for a library implementation. See Table 9.
- LC5: LBS generally read input parameters from a file and this should be the standard for a library implementation. See Table 8.

9 Traceability Matrices and Graphs

	T1	T2	T3	T4	DD1	DD2	DD3	DD4	DD5
T1		✓			✓		✓		
T2	✓		✓						
T3			✓		✓				✓
T4					✓	✓			✓
DD1	✓		✓	✓					
DD2				✓			✓	✓	
DD3	✓					✓			
DD4						✓			
DD5			✓	✓					

Table 6: Traceability Matrix Showing the Connections Between Items of Different Sections

	A1	A2	A3	A4	A5
T1					✓
T2	✓			✓	✓
T3	✓	✓	✓	✓	✓
T4					
DD1					
DD2	✓				
DD3	✓				✓
DD4	✓				
DD5	✓				
LC1			✓	✓	✓
LC2		✓	✓		✓
LC3					
LC4					
LC5					

Table 7: Traceability Matrix Showing the Connections Between Assumptions and Other Items

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10 Appendix

10.1 Symbolic Parameters

MIN_INSTANCES: 2

10.2 Off The Shelf Solutions

The following tables list some off the shelf Lattice Boltzmann Solvers, along with input parameters, computational parameters, and output parameters.

solver	e	ρ	model	velocity directions	time	η	input method	NNF	ζ
hemeLB[19]	≥ 0	≥ 0	3D	15	≥ 0	≥ 0	prompt	Yes[21]	?
MUPHY[7]	≥ 0	≥ 0	3D	19	≥ 0	≥ 0	file	?	?
waLBerla[25]	≥ 0	≥ 0	2D/3D	19	≥ 0	≥ 0	file	Yes[10]	?
DL_Meso[26]	≥ 0	≥ 0	2D/3D	9,15,19,27	≥ 0	≥ 0	file	Yes	?
LB3D[24]	≥ 0	≥ 0	3D	19	≥ 0	≥ 0	file	Yes[23]	?
Sailfish[15]	≥ 0	≥ 0	2D/3D	9,13,15, 19,27	≥ 0	?	?	?	?
MP-LABS[11]	≥ 0	≥ 0	2D/3D	9,19	≥ 0	?	file	?	?
LBSim[5]	≥ 0	?	2D/3D	6,19	≥ 0	?	?	?	Yes[4]
pyLBM[13]	≥ 0	≥ 0	1D,2D,3D	2,3,5,9, 13,15,19	≥ 0	≥ 0	file	?	Yes

Table 8: OTS LBS Inputs

solver	computational model	decomposition technique	parallel interface
hemeLB[19]	D3Q15i	ParMETIS library	MPI
MUPHY[7]	D3Q19+	PT_Scotch library	MPI
waLBerla[25]	D2Q9, D3Q19	block-wide decomposition	MPI
DL_Meso[26]	D2Q9, D3Q15, D3Q19, D3Q27	domain decomposition	MPI
LB3D[24]	D3Q19	spinodal decomposition	MPI
Sailfish[15]	D2Q9, D3Q13, D3Q15, D3Q19, D3Q27	spinoidal decomposition	MPI, CUDA
MP-LABS[11]	D2Q9, D3Q19	?	MPI
LBSim[5]	D2Q6, D3Q19	spinoidal decomposition	
pyLBM[13]	D1Q2, D1Q3, D1Q5, D2Q9, D2Q13, D2Q15, D3Q15, D3Q19	?	MPI

Table 9: OTS LBS Computational Parameters

solver	wall pressure	flow velocity	graphical model
hemeLB[19]	≥ 0	≥ 0	2D/3D
MUPHY[7]	?	?	2D/3D
waLBerla[25]	?	≥ 0	2D/3D
DL_Meso[26]	?	≥ 0	2D/3D
LB3D[24]	?	≥ 0	2D/3D
Sailfish[15]	?	≥ 0	2D
MP-LABS[11]	?	≥ 0	2D/3D
LBSim[5]	?	?	2D/3D
pyLBM[13]	?	?	2D/3D

Table 10: OTS LBS Output Parameters

10.3 Coefficient Weights for Equilibrium Distribution Function

lattice model	coefficient weights (w_i)
D1Q2[]	?
D1Q3[16]	4/6, i = 0; 1/6, i=1,2
D1Q5[17]	1/2,i = 0; 1/6, i = 1,2; 1/12, i = 3,4
D2Q9[22]	4/9,i = 0; 1/9, i = 1,2,3,4; 1/36, i = 5,6,7,8
D2Q13[18]	3/8,i = 0; 1/12, i = 1,2,3,4; 1/16, i = 5,6,7,8; 1/96, i = 9-12
D2Q15[]	?
D3Q15[22]	2/9, i = 0; 1/9, i = 1,2,...,6; 1/72, i = 7,8,...,14
D3Q19[22]	2/9, i = 0; 1/18, i = 1,2,...,6; 1/36, i = 7,8,...,18
D3Q27[22]	8/27, i = 0; 2/27, i = 1,2,...,6; 1/54, i = 7,8,...,18; 1/216. i = 19,20,...,26

Table 11: Lattice Model Coefficient Weights

10.4 First Stage of Implementation

The first stage of implementation will focus on a library of services using the OTS family member pyLBM.

variability	value	binding time
Computational Model	D2Q9	compile
Re	0.0001 - 50000	run
ρ	0.0708 - 13.6	run
Bulk viscosity	0.0001 - 20000	run
Shear viscosity	0.001 - 20000	run
t	$\mathbb{N} > 0$	run
Pressure gradient	\mathbb{R}	run

Table 12: First Stage Implementation Values