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## Problem 1

Consider an  $r$ -dimensional column vector  $x$  whose entries are random real numbers between  $-5$  and  $5$ . For an integer  $r$  between  $15$  and  $25$  (inclusive), (a) compute  $\|x\|_{\infty}$  using a user-defined function `norminf` (b) compute  $\|x\|_1$  using a user-defined function `norm1` (c) compute  $\|x\|_2$  using a user-defined function `norm2` (d) compute  $\|x\|_p$  for  $p = 3$  using a user-defined function `normp`

```
fprintf('Problem 1\n')
r = 14 + randi(11);

x = randi([-5,5], r, 1);

% (a)
xinf = Norminf(x)

% (b)
xlnorm = Norm1(x)

% (c)
x2norm = Norm2(x)

% (d)
x3norm = Pnorm(x,3)
```

*Problem 1*

## Problem 2

Redo Problem 1 (for the same vector  $x$ ) using the built-in function `norm`.

```
fprintf('Problem 2\n')
% (a)
xinf2 = norm(x, Inf)
% (b)
xlnorm2 = norm(x,1)
% (c)
x2norm2 = norm(x,2)
```

---

```
% (d)
x3norm3 = norm(x,3)
```

*Problem 2*

```
xinf2 =
```

```
5
```

```
x1norm2 =
```

```
59
```

```
x2norm2 =
```

```
14.1774
```

```
x3norm3 =
```

```
9.1057
```

## Problem 3

The following linear systems  $Ax = b$  have  $x$  as the actual solution and  $x_{\text{tilde}}$  as an approximate solution. Compute  $|x - x_{\text{tilde}}|_{\infty}$  and  $|Ax_{\text{tilde}} - b|_{\infty}$ .

```
fprintf('Problem 3\n')
% (a)
x = [1/7, -1/6]';
xtilde = [0.142, -0.166]';

diff1 = norm(x-xtilde, Inf)

A = [1/2, 1/3;
     1/3, 1/4];

b = [1/63, 1/168]';

diff2 = norm(A*xtilde - b, Inf)

% (b)
x = [1.827586, 0.6551724, 1.965517]';
xtilde = [1.8, 0.64, 1.9]';

diff1 = norm(x-xtilde, Inf)

A = [0.04, 0.01, -0.01;
     0.2 , 0.5 , -0.2 ;
     1   , 2   , 4   ];
```

---

```
b = [0.06, 0.3, 11]';

diff2 = norm(A*xtilde - b, Inf)

Problem 3

diff1 =

    8.5714e-04

diff2 =

    2.0635e-04

diff1 =

    0.0655

diff2 =

    0.3200
```

## Problem 4

Find the eigenvalues and corresponding eigenvectors for

```
A = [1 ,0;
     0, 2];

%(a) by hand
%      det(A-lam*I) = 0
% => (1-lam)(2-lam) = 0
% => lam in {1,2}
% => If lam = 1 then eigVec1 = [1,0]'
%      If lam = 2 then eigVec2 = [0,1]'

[V, D] = eig(A)

V =

    1    0
    0    1

D =

    1    0
    0    2
```

---

## Problem 5

Repeat Problem 4 for

```
A = [ 0, 1;
      1, 0];
```

```
%(a) by hand
%      det(A-lam*I) = 0
% => (0-lam)(0-lam)-1*1 = 0
% =>      lam^2 - 1^2 = 0
% =>      (lam-1)(lam+1) = 0
% => lam in {-1,+1}
% => If lam = -1 then
%      (A-lam*I)x = 0
%      => [ 1 1 | 0
%           1 1 | 0 ]
%      => [ 1 1 | 0
%           0 0 | 0 ]
%      => [ x1, x2 ]' = [ -p, p ]' where p in R. If p = 1 then
%      => [ x1, x2 ]' = [ -1, 1 ]'
%      If lam = 1 then
%      (A-lam*I)x = 0
%      => [ -1 1 | 0
%           1 -1 | 0 ]
%      => [ -1 1 | 0
%           -1 1 | 0 ]
%      => [ 1 -1 | 0
%           0 0 | 0 ]
%      => [ x1, x2 ]' = [ p, p ]' where p in R. If p = 1 then
%      => [ x1, x2 ]' = [ 1, 1 ]'

[V, D] = eig(A)

% The entries in V are scalar multiples of the eigenvectors I chose.
```

V =

```
-0.7071    0.7071
 0.7071    0.7071
```

D =

```
-1    0
 0    1
```

## Infinity norm

```
function norminf = Norminf(x)
norminf = max( abs(x) );
```

---

```
end
```

```
xinf =
```

```
5
```

## 1-norm

```
function norm1 = Norm1(x)
norm1 = sum( abs(x) );
end
```

```
x1norm =
```

```
59
```

## 2-norm

```
function norm2 = Norm2(x)
norm2 = ( sum( (abs(x)).^2 ) ) ^ (1/2);
end
```

```
x2norm =
```

```
14.1774
```

## p-norm

```
function pnorm = Pnorm(x,p)
pnorm = ( sum( (abs(x)).^p ) ) ^ (1/p);
end
```

```
x3norm =
```

```
9.1057
```

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