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CSE 3666
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Homework 5

1)

1) a) $0x45652000$
 $0100\ 0101\ 0110\ 0101\ 0010\ 0000\ 0000\ 0000$
 $198-127=11$
normalized representation: $1.1100101001 \cdot 2^{11}$
number in decimal: $111001010010_2 = 3666$
significand in decimal: 0.7900390625

b) $0x00070000$
 $0000\ 0000\ 0000\ 0111\ 0000\ 0000\ 0000\ 0000$
 $0-127=-127$
normalized representation: $0.000111 \cdot 2^{-127} = 1.11 \cdot 2^{-131}$
number in decimal: $1.75 \cdot 2^{-131}$
significand in decimal: 0.0546875

2)

a) $-15.82 \cdot 2^{-10}$

$= 01111.1101000111101011000 \cdot 2^{-10}$

$= 1.111101000111101011000 \cdot 2^{-7}$

$-7 + 127 = 120$

sign exponent fraction

1 0111000 111101000111101011000

single-precision: $0 \times \text{BC7D1EB8}$

b) -831.9

$= 110011111.11100110011010$

$= 1.1001111111100110011010 \cdot 2^9$

$9 + 127 = 136$

sign exponent fraction

1 10001000 1001111111100110011010

single-precision: $0 \times \text{C44FF99A}$

3)

3) Largest odd integer 16777215

in decimal: 16777215

in hex: 0x4B7FFFFF

We set the sign bit to 0 for positive numbers and maximize the significand by setting all bits to 1 to ensure it is odd. Then we determine the exponent that places the binary point right of the significand maximizing the integer value which is 23 thus our normalized representation is: $1.111111111111111111111111 \cdot 2^{23}$

Therefore:

sign	exponent	fraction
0	10010110	111111111111111111111111

4)

```
67 dot_product:
68     # TODO
69     # use one of the fcvf instructions to convert
70     # integer 0 to SF 0
71     fcvf.s.w ft0, t0      # ft0 = 0.0
72     fcvf.s.w fs0, t0     # fs0 = 0.0
73 loop:
74     bge     t0, a2, f_exit # if(i >= n) goto f_exit
75
76     slli    t1, t0, 2      # t1 = i * 4
77     add     t2, t1, a0     # t2 = x[i]
78     add     t3, t1, a1     # t3 = y[i]
79
80     flw     ft1, 0(t2)     # load value at x[i] to ft1
81     flw     ft2, 0(t3)     # load value at y[i] to ft2
82
83     fmul.s  ft3, ft1, ft2
84     fadd.s  fs0, fs0, ft3  # sum += x[i] * y[i]
85
86     addi    t0, t0, 1      # i += 1
87     beq     x0, x0, loop   # goto loop
88 f_exit:
89     fadd.s  fa0, ft0, fs0  # set return value to fs0
90     jalr    x0, ra, 0      # return
91
```

5)

$$a) (1 \cdot 0.1) + (2 \cdot 0.2) + (3 \cdot 0.5) + (3 \cdot 0.2) = 2.6$$

$$b) (1 \cdot 0.1) + (1 \cdot 0.2) + (4 \cdot 0.5) + (5 \cdot 0.2) = 3.3$$

$$c) CPU_{Time_1} = \frac{CPI_1}{ClockRate_1} = \frac{2.6}{2} = 1.3$$

$$CPU_{Time_2} = \frac{CPI_2}{ClockRate_2} = \frac{3.3}{3} = 1.1$$

$$n = \frac{CPU_{Time_1}}{CPU_{Time_2}} = \frac{1.3}{1.1} = 1.18 \text{ (P2 is 1.18 times faster than P1)}$$

$$d) (1 \cdot 0.417) + (1 \cdot 0.166) + (4 \cdot 0.417) = 2.25$$

$$e) Speedup = \frac{CPI_{before}}{CPI_{after}} = \frac{3.3}{2.25} = 1.47$$

6)

$$b) a) \text{ Speedup} = \frac{1}{0.8 + \frac{0.2}{100}} = 1.25$$

$$b) \text{ Speedup} = \frac{1}{0.65 + \frac{0.2}{10} + \frac{0.15}{6}} = 1.44$$

$$c) \text{ Speedup} = \frac{1}{0.45 + \frac{0.2}{100} + \frac{0.2}{10} + \frac{0.15}{6}} = 2.012$$

$$d) \text{ Best Speedup} = \frac{0.497}{0.45} = 1.1044$$