

# Math 342W Lecture 20

## Information on Models (Types)

Response Space	Model Type	$\hat{y}$ returns	$\mathcal{A}$	Estimates
$y \in \mathbb{R}$	Regression	$\hat{y} \in \mathbb{R}$	OLS	$y$
$y = \{c_1, c_2, \dots, c_k\}$	Classification	$\hat{y} \in \{c_1, \dots, c_k\}$	kNN	$y$
$y = \{0, 1\}$	Binary Classification	$\hat{y} \in \{0, 1\}$	SVM	$y$
$y = (0, 1)$	Proportion	$\hat{y} \in (0, 1)$	Beta Regression	$y$
$y = \mathbb{R}_{\geq 0}$	Survival	$\hat{y} \in \mathbb{R}_{\geq 0}$	Weibull Regression	$y$
$y = \{0, 1, 2, \dots\}$	Count	$\hat{y} \in \{0, 1, 2, \dots\}$	Poisson Regression	$y$
$y = \{0, 1\}$	Probability Estimation Model	$\hat{p} \in [0, 1]$	Logistic Regression	$P(Y=1) = \hat{p}$
$y = \{c_1, \dots, c_k\}$	" "	$\hat{p} \in [0, 1]^k$	Multi-Logit Regression	$\begin{bmatrix} P(Y=c_1) \\ \vdots \\ P(Y=c_k) \end{bmatrix}$
$y = \{c_1, \dots, c_k\}$	" "	" "	Proportional Odds Model	" "

ordinal

These are some of the types of models in existence, but some of the more frequently used types.

## Asymmetric Cost Modeling

Traditional Misclassification Error =  $\frac{1}{n} \sum_{i=1}^n \mathbb{I}_{\hat{y}_i \neq y_i} \Rightarrow e_i = y_i - \hat{y}_i$

$\underbrace{\qquad\qquad\qquad}_{C_i \neq 0}$

	$\hat{y}$	0	1	
$y$	0	0	-1	False Positive
	1	+1	0	False Negative

$$\text{Misclassification Error} = \frac{\sum_i (FP + FN)}{n}$$

Another Objective Function  $\Rightarrow$  Total Cost =  $C_{FP} \cdot FP + C_{FN} \cdot FN$

$\hookrightarrow$  Average Cost = Total Cost /  $n$

$\mathcal{R}$ : Minimize Total Cost  $\Rightarrow$  Asymmetric Cost Model ( $C_{FP} \neq C_{FN}$ )

$$y \in \{0, 1\} \Leftrightarrow Y \sim \text{Bern}(t(\vec{z})) \Rightarrow Y \sim \text{Bern}(f_{pr}(\vec{x}) + (t(\vec{z}) - f_{pr}(\vec{x})))$$

$$y = t(\vec{z}) \xrightarrow{y \in \{0, 1\}} \Rightarrow Y \sim \text{Bern}(f_{pr}(\vec{x}))$$

$$= f(\vec{x}) + s \xrightarrow{s \in \{-1, 0, 1\}} \Rightarrow Y \sim \text{Bern}(h_{pr}^*(\vec{x}) + (f_{pr}(\vec{x}) - h_{pr}^*(\vec{x})) + (t(\vec{z}) - f_{pr}(\vec{x})))$$

$$= h^*(\vec{x}) + e \Rightarrow Y \sim \text{Bern}(g_{pr}(\vec{x}) + \dots)$$

$$= g(\vec{x}) + e \xrightarrow{e \in \{-1, 0, 1\}} \Rightarrow Y \sim \text{Bern}(g_{pr}(\vec{x})) \Rightarrow \hat{p} = g_{pr}(\vec{x}), \text{estimating } P(Y=1|\vec{x})$$

$\uparrow$   
Shows "e"

$$f_{pr}(\vec{x}) : \mathcal{R}^D \rightarrow (0, 1)$$

$$h_{pr}^*(\vec{x}) : \mathcal{R}^D \rightarrow (0, 1)$$

$$g_{pr}^*(\vec{x}) : \mathcal{R}^D \rightarrow (0, 1)$$