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1 from falkner_skan import falkner_skan
2 import numpy as np
3 import sympy as sp
4 import matplotlib.pyplot as plt
5
6 ### Define constants
7 m = 0.0733844181517584 # Exponent of the edge velocity ("a")
8 Vinf = 7 # Velocity at the trailing edge
9 nu = 1.45e-5 # kinematic viscosity
10 c = 0.08 # chord, in meters
11 x = sp.symbols("x") # x as a symbolic variable
12
13 ### Get the nondimensional solution
14 eta, f0, f1, f2 = falkner_skan(m=m) # each returned value is a
    ndarray
15
16 ### Dimensionalize the solution
17 ue = Vinf * (x / c) ** m
18 y = eta / (
19     sp.sqrt(
20         ((m + 1) / 2) * (ue / (nu * x))
21     )
22 )
23 u = f1 * ue
24
25 ### Get parameters of interest
26 Re_local = ue * x / nu
27 dFS = sp.sqrt(nu * x / ue)
28
29 theta_over_dFS = np.trapz(
30     f1 * (1 - f1),
31     dx=eta[1]
32 ) * np.sqrt(2 / (m + 1))
33 dstar_over_dFS = np.trapz(
34     (1 - f1),
35     dx=eta[1]
36 ) * np.sqrt(2 / (m + 1))
37 H = dstar_over_dFS / theta_over_dFS
38
39 dudy_wall = u[1] / y[1] # approximately
40 Cf = nu * dudy_wall / (0.5 * ue ** 2)
41
42 ### Plot parameters of interest
43 plt.ion()
44

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45 # Generate discrete values of parameters
46 x_over_c = np.linspace(1 / 100, 1, 100)
47 theta_d = sp.lambdify(x, theta_over_dFS * dFS, "numpy")(
    x_over_c * c)
48 H_d = sp.lambdify(x, H, "numpy")(x_over_c * c)
49 Cf_d = sp.lambdify(x, Cf, "numpy")(x_over_c * c)
50
51 # Plot it
52 fig, ax = plt.subplots()
53
54 plt.subplot(311)
55 plt.plot(x_over_c, theta_d)
56 plt.title(r"$\theta$ Distribution")
57 plt.xlabel(r"$x/c$")
58 plt.ylabel(r"$\theta$ (unitless)")
59 plt.grid(True)
60
61 plt.subplot(312)
62 plt.plot(x_over_c, np.tile(H_d, len(x_over_c)))
63 plt.title(r"$H$ Distribution")
64 plt.xlabel(r"$x/c$")
65 plt.ylabel(r"$H$ (unitless)")
66 plt.grid(True)
67
68 plt.subplot(313)
69 plt.plot(x_over_c, Cf_d)
70 plt.title(r"$C_f$ Distribution")
71 plt.xlabel(r"$x/c$")
72 plt.ylabel(r"$C_f$ (unitless)")
73 plt.grid(True)
74
```