

# ECE 434 Biophotonics Project

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A Project Report on optical trapping  
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April 8, 2024

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## Theory

### The Ray Optics Model

TODO

### The Electric Dipole Model

$$\mathbf{F} = (\mathbf{p} \cdot \nabla) \mathbf{E} + \frac{d\mathbf{p}}{dt} \times \mathbf{B}$$

$$\mathbf{F} = \alpha \left[ (\mathbf{E} \cdot \nabla) \mathbf{E} + \frac{d\mathbf{E}}{dt} \times \mathbf{B} \right]$$

$$\mathbf{F} = \alpha \left[ \frac{1}{2} \nabla E^2 + \frac{d}{dt} (\mathbf{E} \times \mathbf{B}) \right]$$

$$\mathbf{F} = \frac{1}{2} \alpha \nabla E^2$$

$$\mathbf{F}_{\text{scat}}(\mathbf{r}) = \frac{k^4 \alpha^2}{6\pi c n^3 \varepsilon_0^2} \mathbf{I}(\mathbf{r}) \hat{z} = \frac{8\pi n_0 k^4 a^6}{3c} \left( \frac{m^2 - 1}{m^2 + 2} \right)^2 \mathbf{I}(\mathbf{r}) \hat{z}$$

### Harmonic Potential Approximation

$$\nabla \mathbf{E}_{\text{AC Stark}} = \frac{3\pi c^2 \Gamma \mu}{2\omega_0^3 \delta} \mathbf{I}(\mathbf{r}, \mathbf{z})$$

$$I(r, z) = I_0 \left( \frac{\omega_0}{\omega(z)} \right)^2 e^{-\frac{2r^2}{\omega^2(z)}}$$

$$\omega(z) = \omega_0 \sqrt{1 + \left( \frac{z}{Z_R} \right)^2}$$

$$Z_R = \frac{\pi \omega_0^2}{\lambda}$$

$$P_0 = \frac{1}{2} \pi I_0 \omega_0^2$$

$$\left. \frac{1}{2!} \frac{\partial^2 I}{\partial z^2} \right|_{r,z=0} z^2 = \frac{2P_0 \lambda^2}{\pi^3 \omega_0^6} z^2 = \frac{1}{2} m \omega_z^2 z^2$$

$$\left. \frac{1}{2!} \frac{\partial^2 I}{\partial r^2} \right|_{r,z=0} r^2 = \frac{4P_0}{\pi \omega_0^4} r^2 = \frac{1}{2} m \omega_r^2 r^2$$

$$\omega_r = \sqrt{\frac{8P_0}{\pi m \omega_0^4}}$$

$$\omega_z = \sqrt{\frac{4P_0 \lambda^2}{m \pi^3 \omega_0^6}}$$

$$\frac{\omega_r}{\omega_z} = \sqrt{2} \frac{\omega_0 \pi}{\lambda}$$

Want to go over time dependent perturbation theory

Then add sinusoidal perturbations

Then derive Einstein's A and B coeffs

Ultimately get Fermi's golden rule and lasers

## Applications

## References