

# Discussion of Analysis of Forensic DNA Mixtures with Artefacts

by Cowell, Graversen, Lauritzen and Mortera

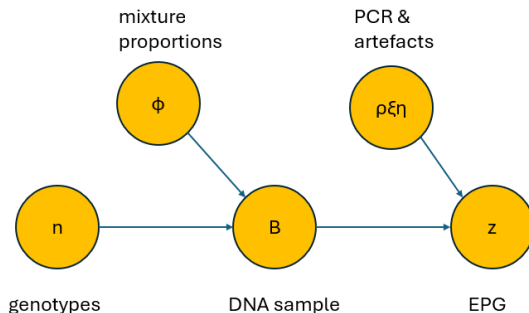
Peter Green

RSS Journal Webinar, August 2025

# CGLM model

CGLM provide a joint probability model connecting

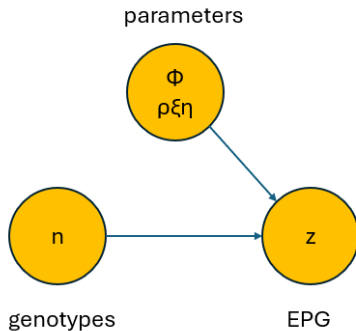
- EPG peak heights  $z$
- genotypes of contributors  $n$
- hypotheses  $\mathcal{H}$  about contributors



# CGLM recap

It is natural to assume

$$p(z, n|\mathcal{H}) = p(n|\mathcal{H}) \times p(z|n)$$



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The key (and innovative!) ingredients

- gamma peak height model for  $p(z|n)$
- captures (most) artefacts
- Bayes net representation for  $p(n|\mathcal{H})$ : continuous-valued  $z$  are fixed, so  $p(n|\mathcal{H}, z)$  is still a BN for  $n$
- 'allele count' representation for  $n$  – Markov serial dependence along allele values
- DNAmixtures R package

# Paternity testing

A common set-up:

- a woman claims that a certain individual (the ‘putative father’) is the father of her child
- mother, child and putative father are genotyped (using STR markers)
- we wish to assess the evidence for paternity

The plaintiff’s hypothesis is  $\mathcal{H}_p$  : the putative father is the true father; the alternative is  $\mathcal{H}_0$  : someone else is the father – to be precise, the father is a randomly chosen person (male) in the population (which population?)

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# Relatedness, relationships and DNA mixtures

... based on joint work with Julia Mortera

In reality, the genotypes of actors (mixture contributors and other typed individuals) are not independent. We distinguish between

- (ambient) **relatedness**: there is always a degree of kinship among individuals in sub-populations: island model,  $\theta$  correction, etc
- (specific, close-family) **relationships**: under some hypothesised scenarios, some actors are close relatives (brothers in crime, paternity cases, etc.)

and in the latter case we may require analysis

- **about** such relationships (e.g. paternity)
- **allowing for** such relationships (e.g. was suspect's brother also at the scene?)



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In the standard case, for  $p(n|\mathcal{H})$  we would assume that the genotypes of the  $k$  contributors are  $k$  independent draws from the ‘gene pool’. Here, we will show how to replace this so that  $p(n|\mathcal{H})$  models the hypothesised relationships (among contributors, or between contributors and typed individuals).

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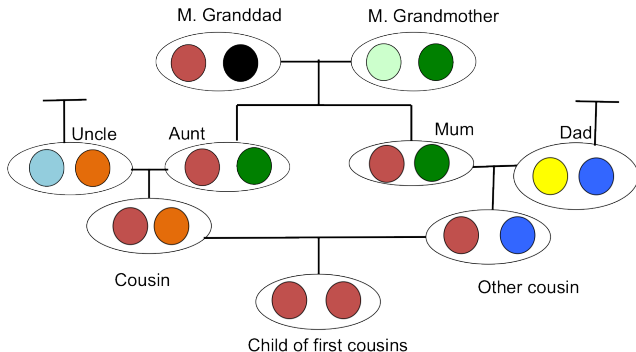
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# Identity by descent



(none of this is specific to CGLM, STR markers, or forensic genetics at all)

# Family relationships $\equiv$ patterns of IBD

## IBD – Identity by descent.

We consider here only autosomal STR markers, one marker (locus) at a time, under Hardy-Weinberg equilibrium.

Consider a parent and child: the joint distribution of their genotypes can be precisely described thus: the parent's genotype is  $(a, b)$  and the child's is  $(a, c)$ , where  $a, b, c$  are independently drawn from a distribution  $q$  over alleles (the allele frequency distribution for this population and marker). The  $a$  appears in both genotypes: the genes are *identical by descent*.

In the absence of **inbreeding**, any two relatives' genotypes can be written as  $(a, b)$ , and  $(a, b)$ ,  $(a, c)$  or  $(c, d)$  with probabilities  $\kappa_2, \kappa_1, \kappa_0$ , where

$a, b, c, d \stackrel{iid}{\sim} q$ , where  $\kappa_0 + \kappa_1 + \kappa_2 = 1$ .

e.g. for parent & child,  $\kappa_0 = \kappa_2 = 0, \kappa_1 = 1$

for siblings,  $\kappa_0 = \kappa_2 = 0.25, \kappa_1 = 0.5$

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For two individuals, but allowing also for inbreeding, the situation was captured by Jacquard's (1974) condensed coefficients of descent  $\Delta_1, \dots, \Delta_9$ .

The general case of any number of individuals has been formulated and analysed in seminal work by Elizabeth Thompson, using models for the meioses in the pedigree – the random selection of which gene each parent passes to their offspring.

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# IBD pattern distributions

IBD pattern distributions for a Father/Mother/Child triple.

(a) Distinguishing maternal and paternal genes

pr	Fgt		Mgt		Cgt	
0.25	1	2	3	4	1	3
0.25	1	2	3	4	2	3
0.25	1	2	3	4	1	4
0.25	1	2	3	4	2	4

(b) Condensed form  $\equiv$  Not distinguishing maternal and paternal genes

pr	Fgt		Mgt		Cgt	
1	1	3	2	4	1	2

(c) Extending the family to include the paternal grandfather

pr	Fgt		Mgt		Cgt		GFgt	
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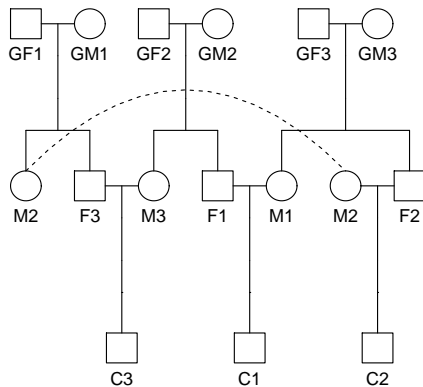
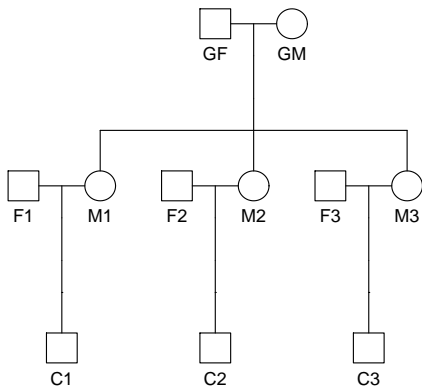
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# Pairwise relationships do not determine joint ones



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IBD pattern distributions for two scenarios of 3 pairwise cousins; (left) star, (right) cyclic arrangements.

pr	C1		C2		C3		pr	C1		C2		C3	
0.3750	1	2	3	4	5	6	0.421875	1	2	3	4	5	6
0.1875	1	2	1	3	4	5	0.140625	1	2	1	3	4	5
0.1875	1	2	3	4	1	5	0.140625	1	2	3	4	1	5
0.1875	1	2	3	4	3	5	0.140625	1	2	3	4	3	5
0.0625	1	2	1	3	1	4	0.046875	1	2	1	3	2	4
							0.046875	1	2	1	3	3	4
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							0.015625	1	2	1	3	2	3

# Modelling and computation in KinMix

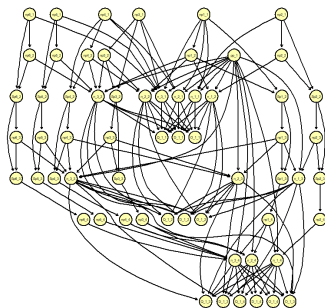
In

$$p(z, n|\mathcal{H}) = p(n|\mathcal{H}) \times p(z|n)$$

we replace the Bayes net representing the standard  $p(n|\mathcal{H})$  by one generated **automatically** from the IBD pattern distribution.

```
> as.IBD('3cousins-star')
```

	pr	a	b	c
0.0625	1	2	1	3
0.1875	1	2	1	3
0.1875	1	2	3	4
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0.3750	1	2	3	4



# Software

Therese Graversen's **R** package **DNAmixtures** performs DNA mixture analysis using the CGLM model.

My **R** package **KinMix** augments **DNAmixtures** to implement the new methods presented here.

**DNAmixtures** and hence **KinMix** requires the commercial software **Hugin** (via the **RHugin** package).

**DNAmixturesLite** and **KinMixLite** are freeware versions of these, and **are available on CRAN** – with slight limits on functionality and problem size, and some loss of efficiency (with Therese Graversen).

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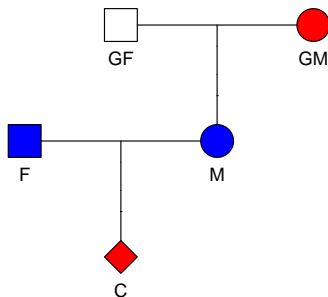
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```
IBD<-as.IBD(matrix(c('M','GM','GF',
  'C','M','F'),2,3,byrow=TRUE),
  targets=c('F','M','C','GM'))
```

```
mix<-KinMix(list(epg),k=2,C=list(0.001),database=db,
  contribs=c('F','M'),typed.gts=list(C=Cgt,GM=GMgt),
  IBD=IBD,targets=c('F','M','C','GM'))
```

# References

Cowell, R. G., Graversen, T., Lauritzen, S., and Mortera, J. (2015). Analysis of DNA mixtures with artefacts. *Journal of the Royal Statistical Society Series C* (with discussion), 64, 1–48 (my discussion p.41).

Green, P. J. and Mortera, J. (2009) Sensitivity of inferences in forensic genetics to assumptions about founding genes. *Annals of Applied Statistics*, 3, 731–763. doi: 10.1214/09-AOAS235.

not mixtures: heterogeneous populations, uncertain allele frequencies, UAF=coancestry

Green, P. J. and Mortera, J. (2017). Paternity testing and other inference about relationships from DNA mixtures. *Forensic Science International: Genetics*, 28, 128–37.

manipulating BNs to express relationships

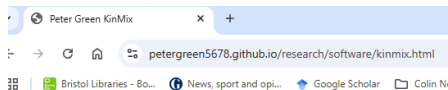
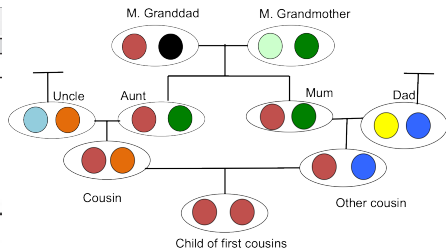
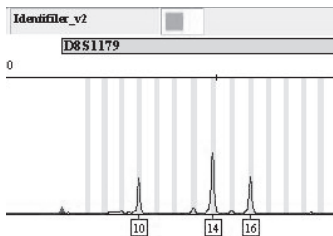
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general IBD patterns, model, algorithm, KinMix package

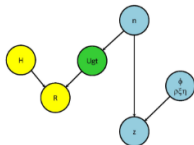
Green, P. J., Mortera, J., and Prieto, L. (2021). Casework applications of probabilistic genotyping methods for DNA mixtures that allow relationships between contributors. *Forensic Science International: Genetics*, 52, 102482.

casework examples

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## KinMix and KinMixLite 2.2.1



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Thanks! Questions?