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# Compact and Optimal Deep Learning with Recurrent Parameter Generators

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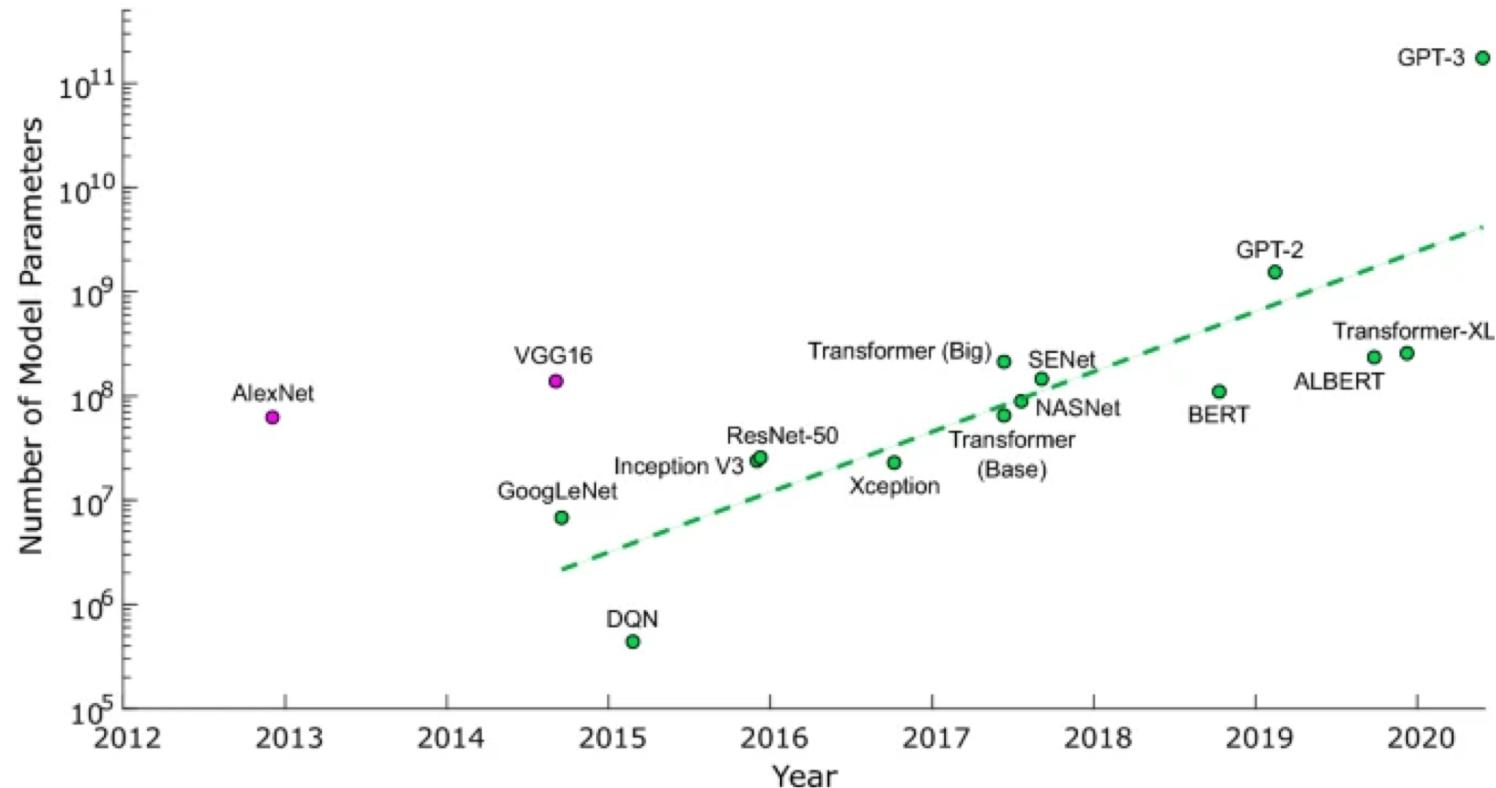
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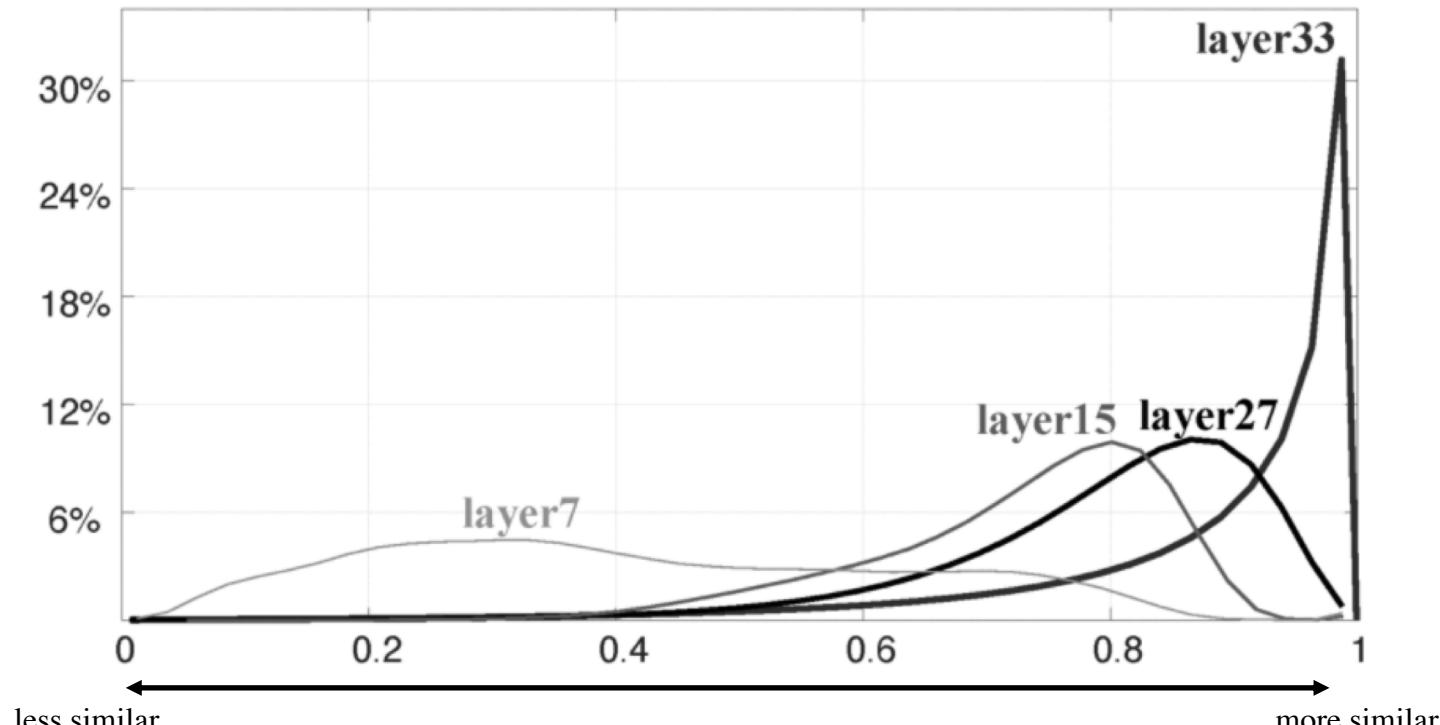
<sup>5</sup>MIT

\* indicates equal contribution

# Exponential Growth in Neural Network Size

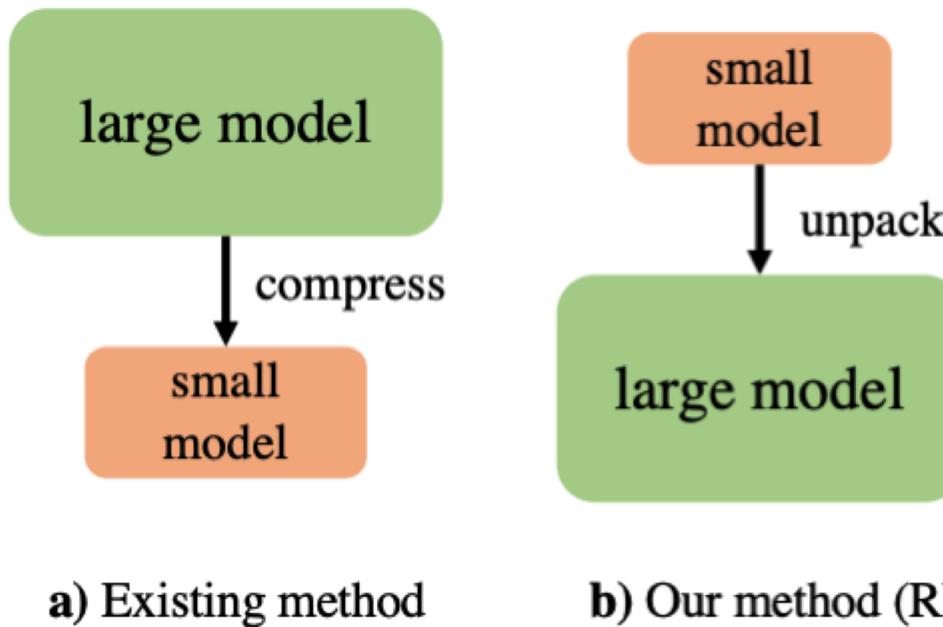


# Neural Nets are Redundant: Filter Similarity Increases with Depth

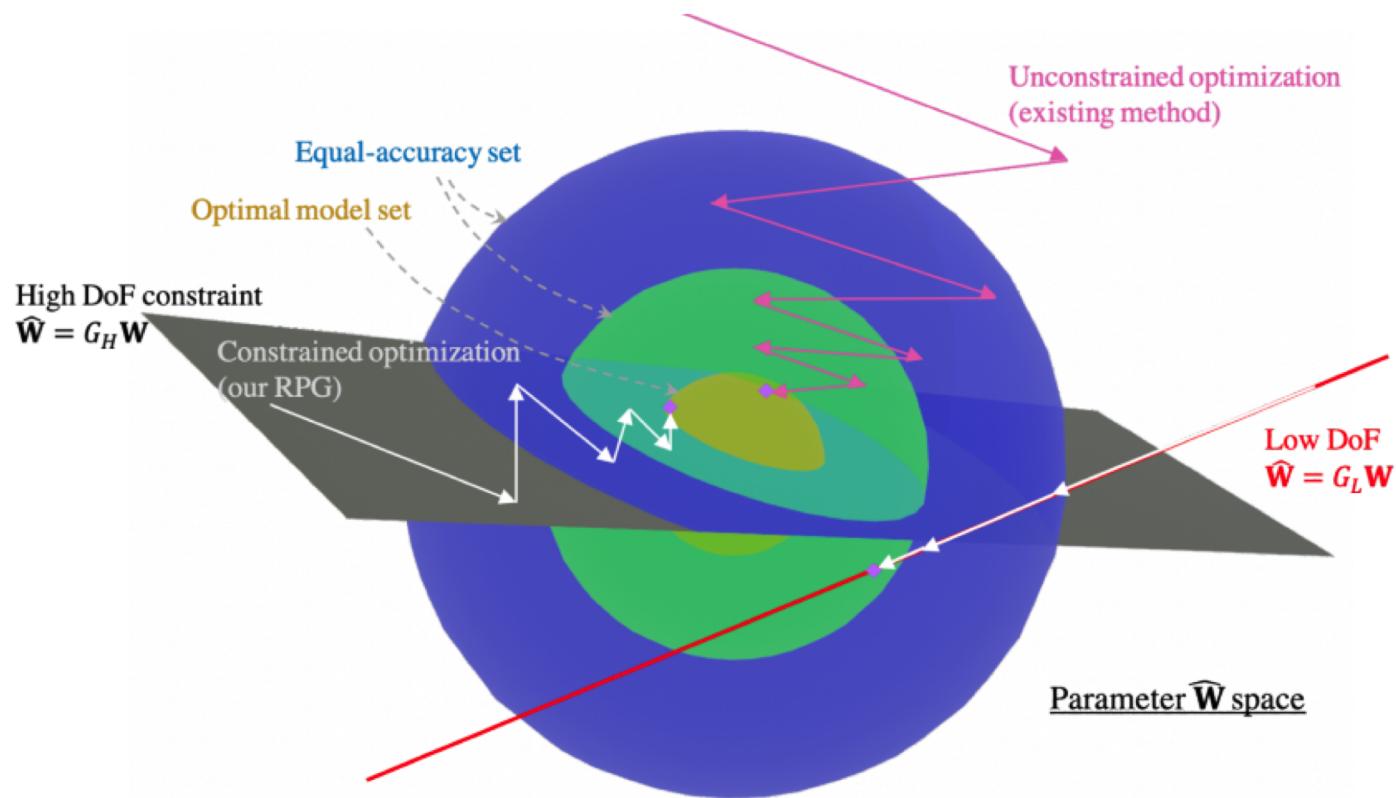


Histogram of Filter Similarity (ResNet34)

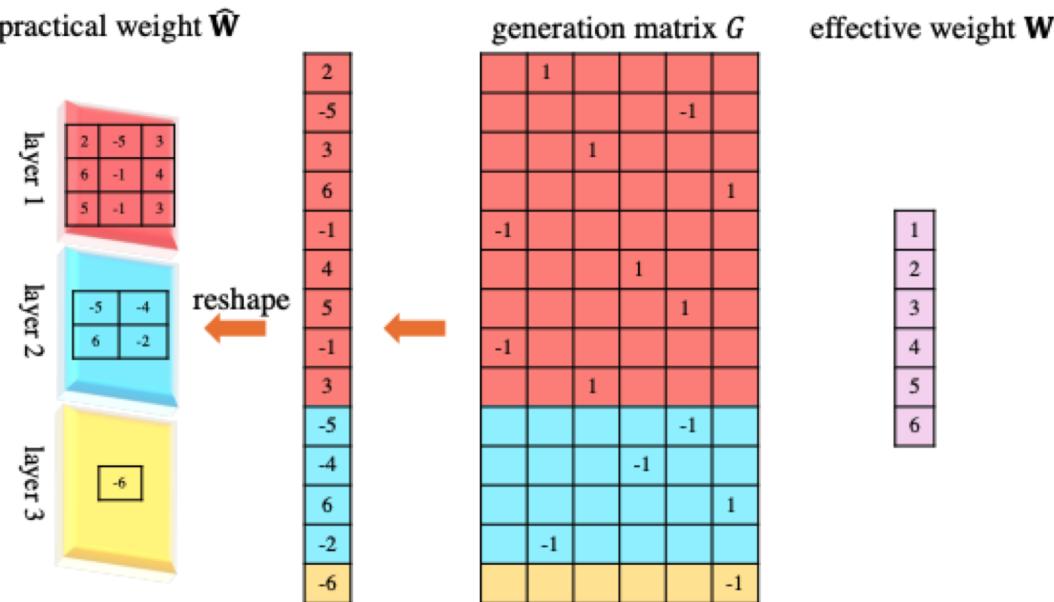
# New Paradigm for Compact and Optimal Deep Learning



# Linearly Constrained Neural Optimization



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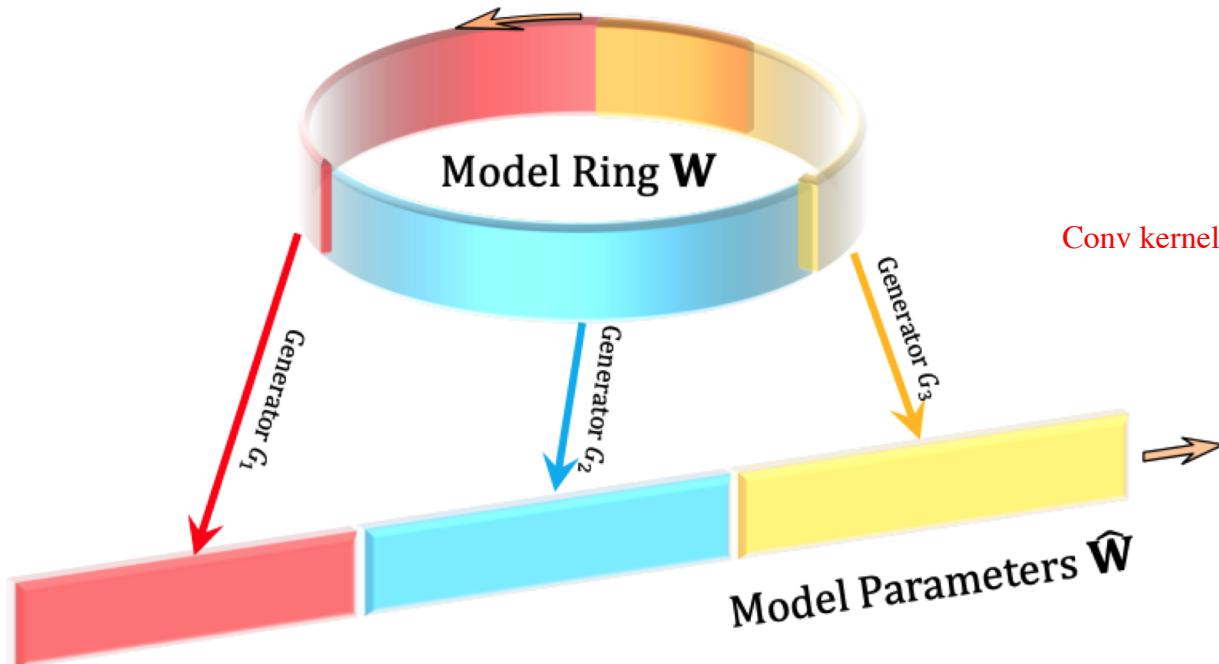


Networks are optimized with a linear constraint  $\hat{\mathbf{W}} = \mathbf{G}\mathbf{W}$

The constrained (practical) parameter  $\hat{\mathbf{W}}$  of each network layer was generated by the generating matrix  $\mathbf{G}$  from the free (effective) parameter  $\mathbf{W}$ , which is directly optimized.

$\hat{\mathbf{W}}$  is unpacked large model parameter while the size of  $\mathbf{W}$  is the model DoF (degree of freedom).

# Recurrent Parameter Generator (Special Case)



Model parameters is a combination of conv kernels:

$$\widehat{\mathbf{W}} = [\mathbf{K}_1, \mathbf{K}_2, \dots, \mathbf{K}_L]$$

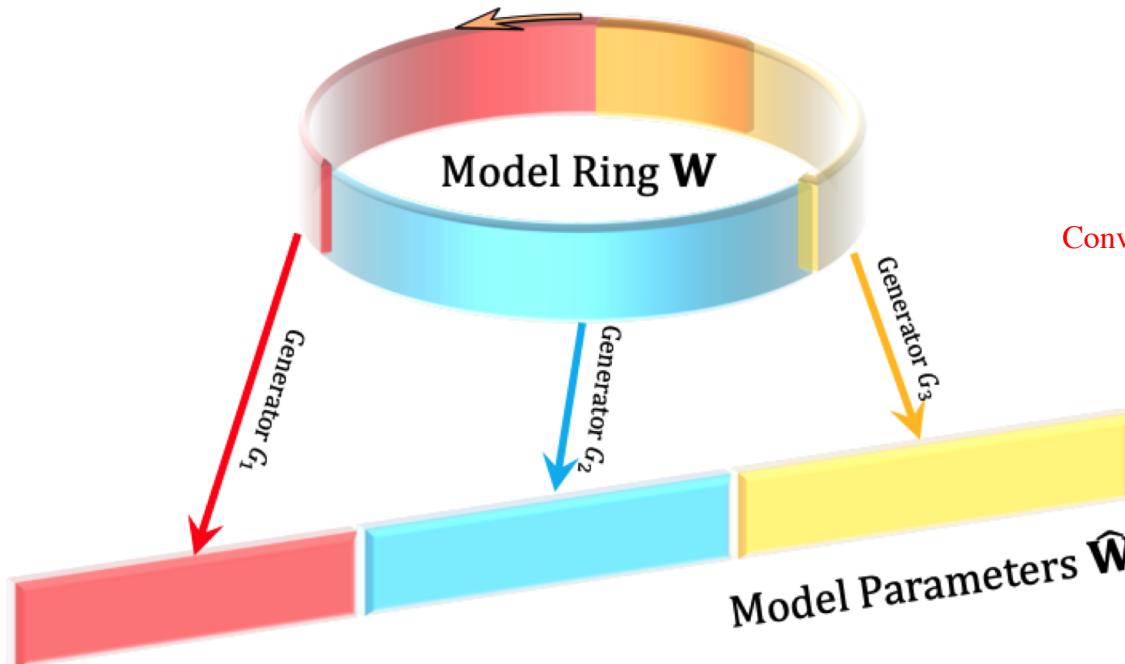
Generating matrix

$$\mathbf{K}_i = \mathbf{G}_i \cdot \mathbf{W}, i \in \{1, \dots, L\}$$

Conv kernel at layer  $i$

(shared) Model ring

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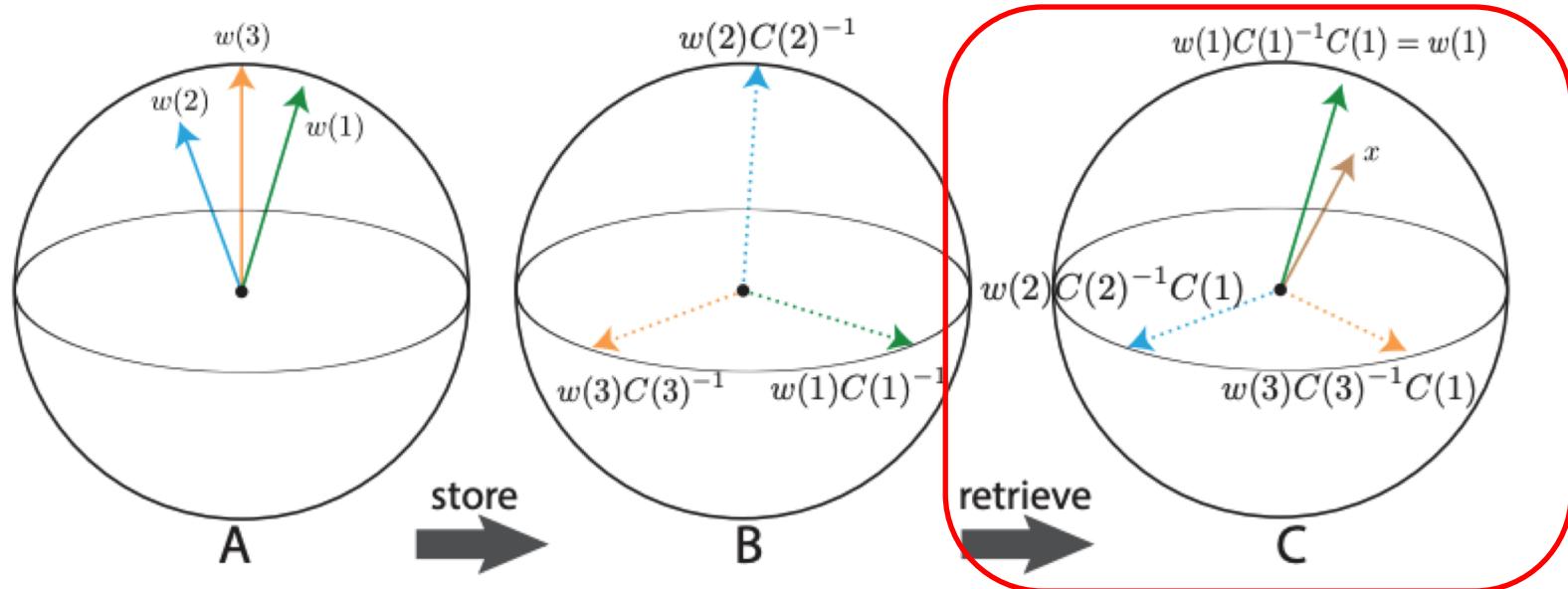
Destructive weight sharing:

$$G_i \in \{b \circ p | b \in B(N_i), p \in P(N_i)\}$$

Random sign flip      permutation

We prove the orthogonality of two generated kernels (see Appendix)

# Why Orthogonal? Retrieval from the Associative Memory

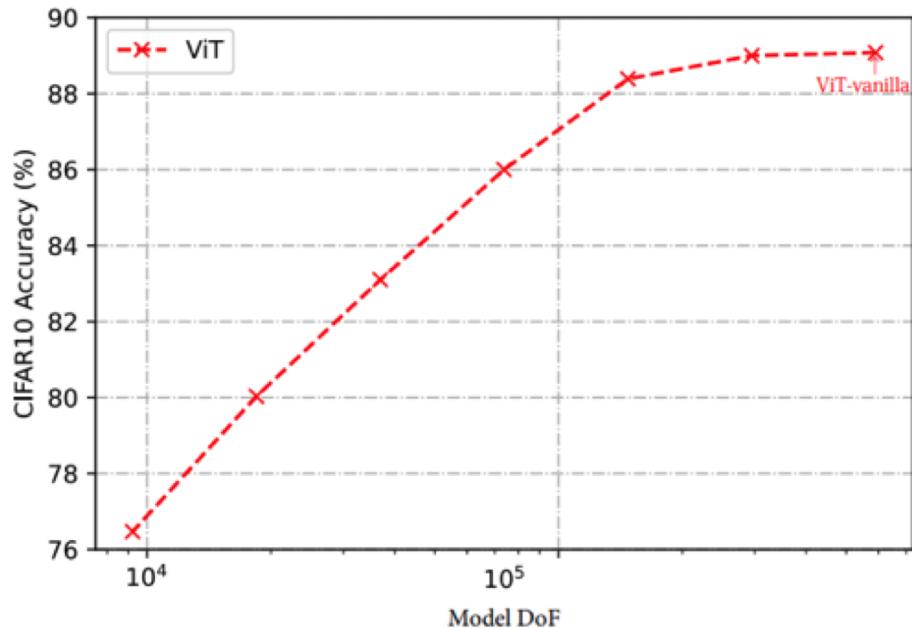
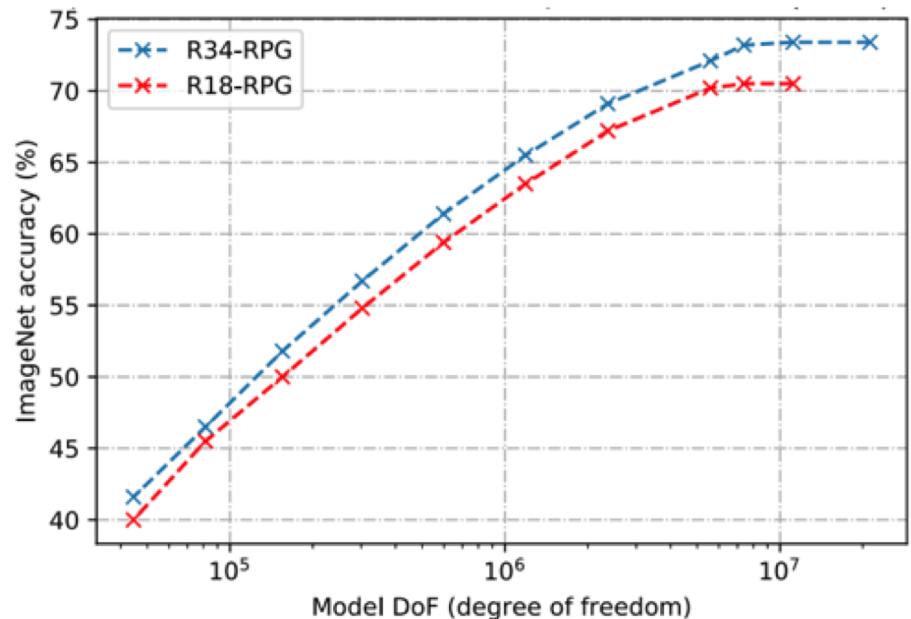


# Extreme Model DoF Compression

Acc. (%)	R18-RPG			R18-vanilla	R34-RPG			R34-vanilla
<b>ImageNet</b>	40.0	67.2	70.5	70.5	41.6	69.1	<b>73.4</b>	<b>73.4</b>
<b>CIFAR100</b>	60.2	75.6	77.6	77.6	61.7	76.5	<b>78.9</b>	<b>79.1</b>
<b>Model DoF</b>	45K	2M	5.5M	11M	45K	2M	11M	21M

For ImageNet classification, RPG achieves 96% of ResNet18's performance with only 18% DoF (the equivalent of one convolutional layer)  
RPG achieves 52% of ResNet34's performance with only 0.25% DoF!

# Log-Linear DoF-Accuracy Relationship



- Accuracy and model DoF follow a *power law*.
- The exponents of the power laws are the same for ResNet18-RPG and ResNet34-RPG on ImageNet.
- RPG enables *under-parameterized* models for *large-scale* datasets such as ImageNet, which may unleash new findings.

# RPG Performs Better at the Same Model DoF

Image Classification

	DoF	Acc. (%)
<b>R18-vanilla</b>	11M	77.5
<b>R34-RPG.blk</b>	11M	78.5
<b>R34-RPG</b>	11M	<b>78.9</b>
<b>R34-random weight share</b>	11M	74.9
<b>R34-DeepCompression [23]</b>	11M	72.2
<b>R34-Hash [12]</b>	11M	75.6
<b>R34-Lego [67]</b>	11M	78.4
<b>R34-vanilla</b>	21M	<b>79.1</b>

Pose Estimation

Acc. (DoF)	CPM [62]	RPG	No shared w.
<b>1x sub-net</b>		84.7 (3.3M)	
<b>2x sub-nets</b>	86.1 (3.3M)	86.5 (3.3M)	87.1 (6.7M)
<b>4x sub-nets</b>	86.5 (3.3M)	87.3 (3.3M)	88.0 (13.3M)

Multitask Regression

RMSE (%)	Depth	Normal
<b>Vanilla model</b>	25.5	41.0
<b>RPG with shared BN</b>	24.7	40.3
<b>Reuse &amp; new BN</b>	24.0	39.4
<b>Reuse &amp; new BN &amp; perm. and reflect.</b>	<b>22.8</b>	<b>39.1</b>

# RPG can be Pruned and Quantized for Faster Runtime

## Pruning RPG

fine-grained pruning

	acc before	acc after ↓ DoF	acc drop	model DoF
<b>R18-IMP [18]</b>	92.3	90.5	1.8	274k
<b>R18-RPG</b>	95.0	93.0	2.0	274k

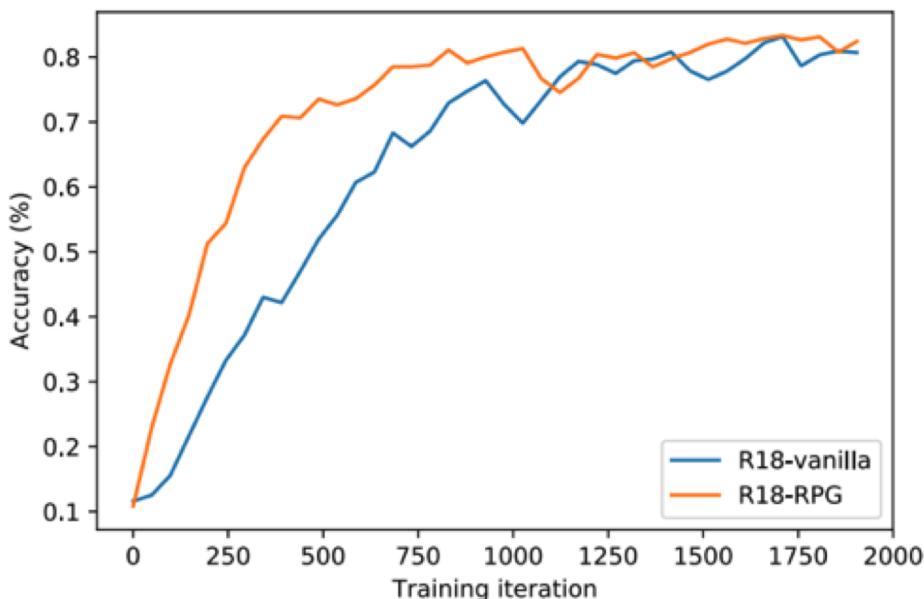
coarse-grained pruning

	DoF before pruning	Pruned acc.	FLOPs
<b>R18-Knapsack</b>	11.2M	69.35%	1.09e9
<b>Pruned R18-RPG</b>	5.6M	69.10%	1.09e9

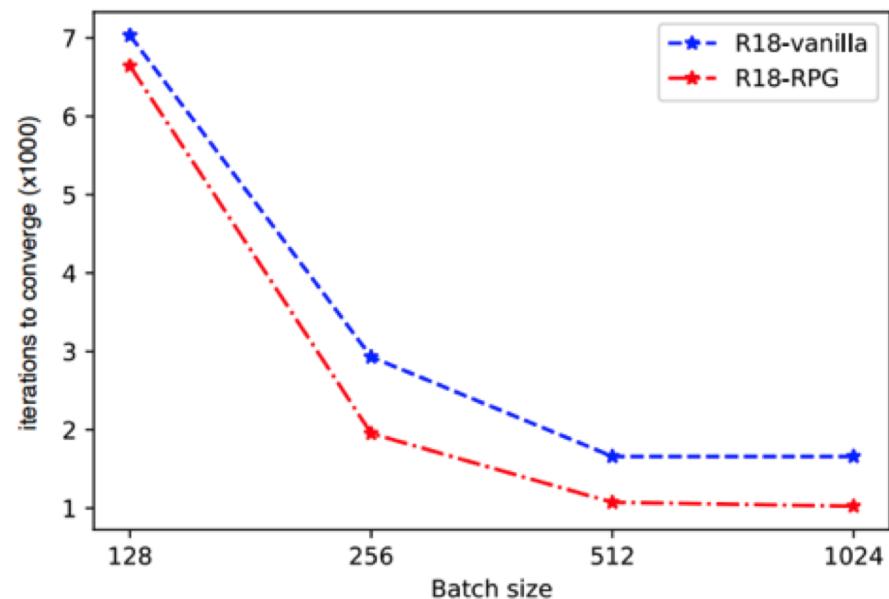
## Quantize RPG

	# Params	Acc before	Acc after ↓ quantization	Acc drop
<b>R18-vanilla</b>	11M	69.8	69.5	0.3
<b>R18-RPG</b>	5.6M	70.2	70.1	0.1

# RPG Converges Faster

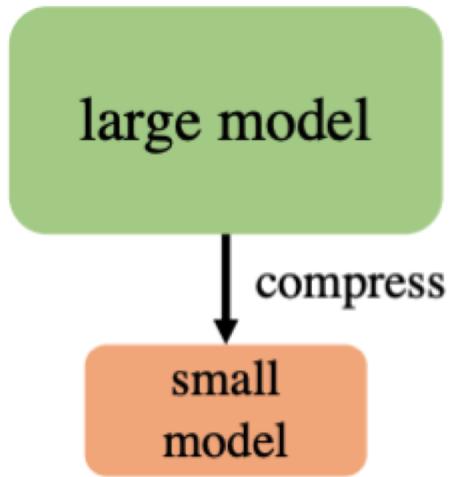


RPG converges faster than the vanilla model

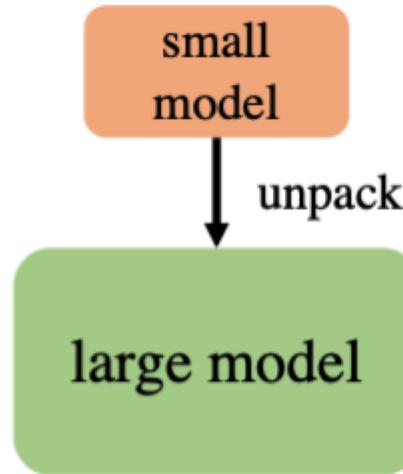


RPG converges faster for different batch sizes

# Summary: New Paradigm for Compact and Optimal Deep Learning



**a)** Existing method



**b)** Our method (RPG)

RPG directly optimizes a lean model with a small DoF.  
Faster and higher accuracy.