

Consider all rectangles with all corners on gridpoints on an $n \times m$ grid.

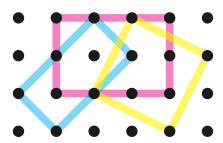


Figure 1: An example of three rectangles with all corners on gridpoints of a 4×6 grid.

Question. How many such rectangles exist?

Related.

- 1. How many squares exist? Rhombuses? Parallelograms? Kites? Quadrilaterals?
- 2. What if we want to count only "primitive" squares, in the sense that the sides of the square only intersect gridpoints at the corners?
- 3. Number of rectangles on the cylinder? Torus? Möbius strip?
- 4. Number of "rotation classes", where two squares are equivalent if one can be transformed into the other by shifting and stretching?
- 5. Number of "orientation classes" where two squares are equivalent if one can be transformed into the other by shifting?
- 6. How many right triangles?
- 7. What if this is done on an $n \times m \times k$ grid?
- 8. What if the rectangles must be diagonal?
- 9. What if this is done on a triangular lattice with equilateral triangles? Primitive equilateral triangles?
- 10. How many tetrahedra are in an n-sided tetrahedra?

References.

Problem 1.

https://oeis.org/A000332 https://oeis.org/A085582

https://arxiv.org/pdf/1605.00180.pdf

http://people.missouristate.edu/lesreid/POW03_01.html