

Consider arrangements of n lines in the plane.

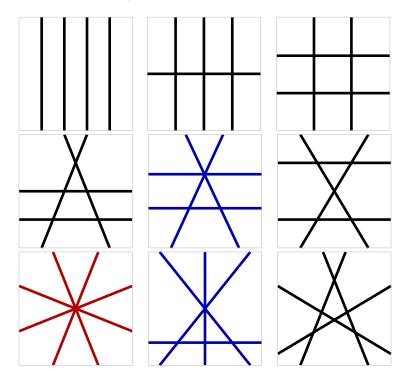


Figure 1: There are A241600(4) = 9 arrangements of 4 lines in the plane, which split the plane into 5, 8, 9, 10, 9, 10, 8, 10, and 11 parts respectively.

Question. How many nonisomorphic ways can n lines split the plane into k parts?

Related.

- 1. What if only two lines can go through a single point?
- 2. What if circles are used instead of lines? Circles on a sphere? Lines on a torus?
- 3. Hyperplanes in higher dimensional space?
- 4. How many arrangements are there if the bounded regions must have equal area?
- 5. How many different polygons can be embedded such that every side is on a line? Convex polygons?

References.

OEIS sequences A241600, A177862, and A250001.