



A Heronian 2-simplex (triangle) is a triangle with both integer sides and integer area. A Heronian n -simplex is an n -simplex with integer volume and where all sides are Heronian $(n - 1)$ -simplices.

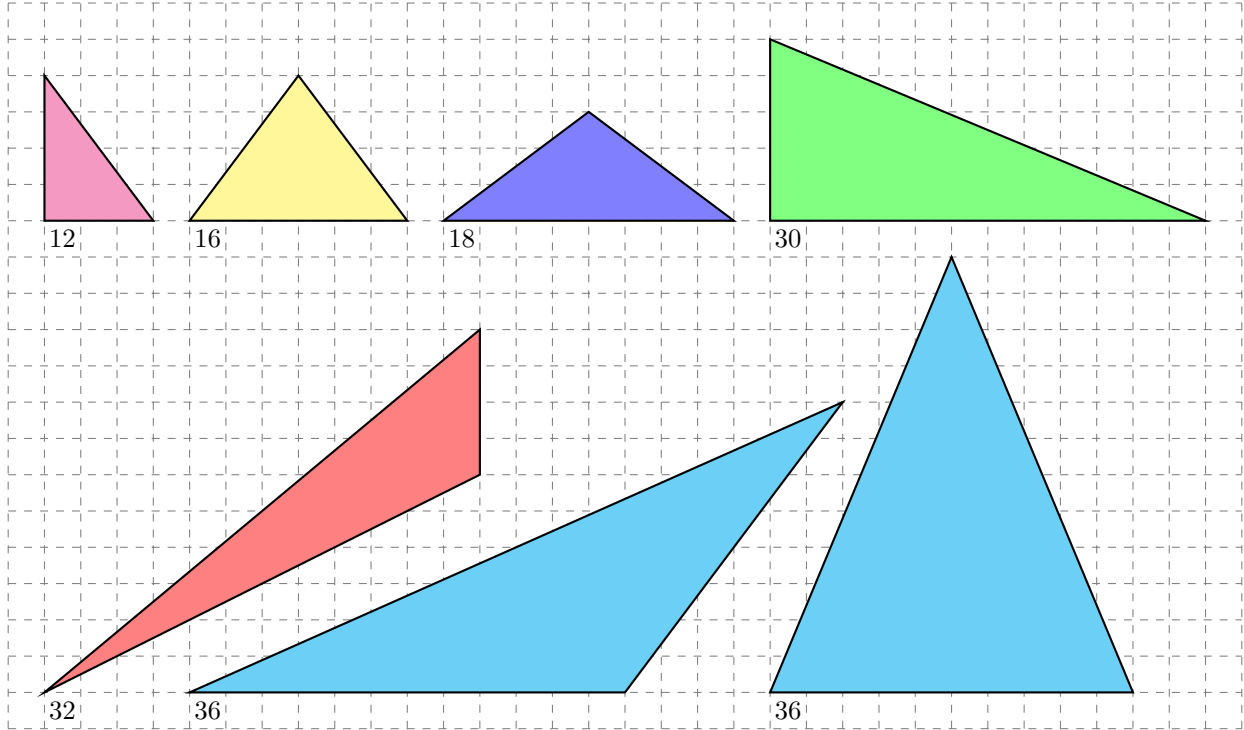


Figure 1: The seven smallest primitive Heronian triangles as measured by perimeter.

Question. Do Heronian n -simplices exist for all integers n ?

Related.

1. Do infinitely many primitive Heronian n -simplices exist for each n ?
2. What is the smallest Heronian n -simplex for each n as measured by volume? As measured by largest side? As measured by sum of sides? As measured by “surface area” (sum of volume of $(n - 1)$ -degree facets)?
3. Are all Heronian n -simplices lattice simplices?
4. What if the definition is relaxed so that only the volume and the edges must be integers?

References.

<https://www.jstor.org/stable/2695390>
<https://oeis.org/A272388>
https://en.wikipedia.org/wiki/Heronian_tetrahedron
<https://en.wikipedia.org/wiki/Simplex>