

Consider polyominoes where each cell has one of  $n$  colors, and each distinct pair of colors is adjacent (horizontally or vertically) to each other somewhere in the polyomino. Let an  $n$ -minimum polyomino be one that has the minimum number of cells.

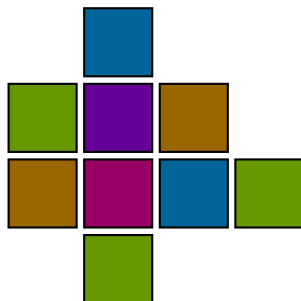


Figure 1: An example of a minimum polyomino for  $n = 5$ ;  $a(5) = 9$

**Question.** How many such  $n$ -minimum polyominoes exist?

**Related.**

1. What if the “distinct” restriction is lifted? (e.g. a blue label must somewhere be adjacent to another blue label.)
2. What is a way to determine the size of an  $n$ -minimum polyomino for large  $n$ ?
3. What if this is done on a triangular or hexagonal grid?
4. What if this is done on a three dimensional cube lattice?