

Problem 18.

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Ron Graham's (A006255) sequence is the least k for which there exists a strictly increasing sequence

$$n = a_1 \leq a_2 \leq \dots \leq a_T = k \text{ where } a_1 \cdot \dots \cdot a_T \text{ is square.}$$

A006255 is bounded above by A072905, the least $k > n$ such that $k \cdot n$ is square.

Question. Does there exist any n for which $A006255(n) = A072905(n)$. In other words, is there any non-square n for which $n \cdot A006255(n)$ is square?

Related.

1. Does the gap $A072905(n) - A006255(n)$ have a nonzero lower bound?

