

Consider attempting to fill in a $n \times n$ Latin square with the numbers 1 through n, one number at a time. A clumsy filling is an incomplete filling in which no more valid moves are possible.

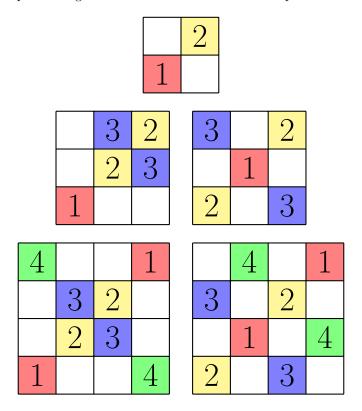


Figure 1: Clumsy filling for n=2,3,4 can be achieved with 2, 5, and 8 or fewer entries respectively; thus $a(2)=2, a(4) \leq 5$, and $a(4) \leq 8$.

Question. Let a(n) be the fewest number of entries required for a clumsy filling. What is a(n)?

Related.

- 1. How many "essentially different" fillings are there? (Two fillings are the same if related by permuting the symbols or dihedral action of the board.)
- 2. Can minimal clumsy fillings be built iteratively, as suggested by the leftmost diagrams in the example?
- 3. What if this is done on a group table instead of a Latin square (quasigroup table)?