

Consider partitions of the  $n \times m$  grid into triangles with vertices on gridpoints.



Figure 1: All six partitions of the  $2 \times 1$  grid into triangles with gridpoint vertices, up to dihedral action.

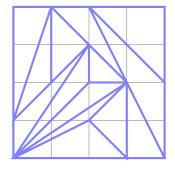


Figure 2: An example of a partitions of the  $4 \times 4$  grid into triangles with no "empty" gridpoints.

Question. How many such partitions exist?

## Related.

- 1. What if these are counted up to rotation/reflection?
- 2. What if this is done on a triangular/hexagonal grid?
- 3. How many partitions with the maximal number of triangles? With k triangles?
- 4. What if all triangles must be right triangles? Acute? Obtuse?
- 5. What if each gridpoint must touch a triangle? What is the minimum number of faces?
- 6. What if each gridpoint must touch as many triangles as possible? What is the minimum number of faces? What's the expected number of faces? (i.e. there's no way to draw a new edge?)
- 7. What if this is done on a grid in hyperbolic space?

**Note.**  $a_1(n) = A051708(n)$ 

## References.

https://oeis.org/A051708

https://codegolf.stackexchange.com/q/176646/53884