

Consider Ron Graham's sequence for lcm, that is, look at sequences such that

$$n = a_1 < a_2 < \dots < a_T = k \text{ and } \text{lcm}(a_1, \dots, a_T) \text{ is square.}$$

Question. Let $A300516(n)$ be the least k (as a function of n) such that such a sequence exists?

$$\begin{aligned} a(1) &= 1 \quad \text{via } (1) \\ a(2) &= 4 \quad \text{via } (2, 4) \\ a(3) &= 3 \quad \text{via } (3, 9) \\ a(4) &= 4 \quad \text{via } (4) \\ a(5) &= 25 \quad \text{via } (5, 25) \\ a(6) &= 12 \quad \text{via } (6, 9, 12) \\ a(7) &= 49 \quad \text{via } (7, 49) \\ a(8) &= 16 \quad \text{via } (8, 16) \end{aligned}$$

Figure 1: Examples of $A300516(n)$ for $n \in \{1, 2, \dots, 8\}$.

Related.

1. For what values n is $A300516(n)$ nonsquare?
2. For what values n does the corresponding sequence have three or more terms?
3. What is the analogous sequence for perfect cubes, etc?

References.

<https://oeis.org/A300516>