



Let

 $C_n = \{f : [n] \to \mathbb{N} \mid \text{the convex hull around } \{(1, f(1)), \dots, (n, f(n))\} \text{ forms an } n\text{-gon}\}$  and then let a(n) denote the least upper bound over all functions in  $C_n$ 

$$a(n) = \min\{\max\{f(k) \mid k \in [n]\} \mid f \in C_n\}$$

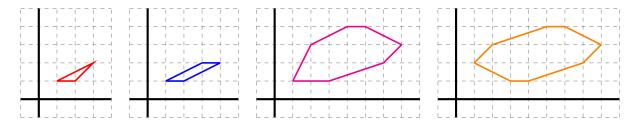


Figure 1: Examples of a(3) = 2, a(4) = 2, a(7) = 4, and a(8) = 4, where the polygons with an even number of vertices have rotational symmetry.

Question. Do these polygons converge to something asymptotically?

## Related.

- 1. Does a(2n) = a(2n 1) for all n?
- 2. Do the minimal 2n-gons always have a representative with rotational symmetry?
- 3. Are minimal 2n-gons unique (up to vertical symmetry) with finitely many counterexamples?
- 4. What is the asymptotic growth of a(n)?

## References.

A285521: "Table read by rows: the n-th row gives the lexicographically earliest sequence of length n such that the convex hull of (1, a(1)), ..., (n, a(n)) is an n-gon with minimum height." (https://oeis.org/A285521)