



The chromatic polynomial of a graph G, $\chi_G(n)$ gives the number of ways to color the vertices of the graph such that no two vertices of the same color are connected by an edge.

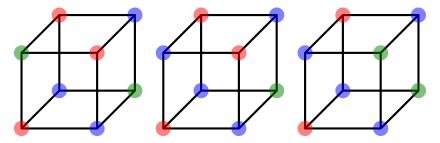


Figure 1: Three examples of 3-colorings of the cube. The chromatic polynomial of the cubic graph is $\chi_{Q_3}(n)=a(n)=n^8-12n^7+66n^6-214n^5+441n^4-572n^3+423n^2-133n$.

Question. Is there a way to generate the chromatic polynomial of an n-cube in polynomial time with respect to n?

Related.

- 1. What about up to permutations of the colors and/or isometries of the cube?
- 2. What about simplices, cross-polytopes, and demicubes?
- 3. What about other polytopes such as associahedra, permutahedra, and the 24-, 120-, and 600-cells?

References.

Problem 61.

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