





Figure 1: The two deltahedra consisting of eight triangles: the octahedron and the biaugmented tetrahedron.

**Question.** How many polytopes can you make out of n equilateral triangles?

## Related.

- 1. What if none of the adjacent faces can be coplanar? (e.g. the "scaled-up" tetrahedron is not allowed)
- 2. How many with some sort of symmetry?
- 3. What if squares or pentagons are used instead?
- 4. What if pentagons and triangles are used?
- 5. How does this generalize to higher dimensions?
- 6. Which n-cell nets can produce the greatest number of distinct polytopes?
- 7. How many n-cell nets can form at least one polytope?

## References.

https://en.wikipedia.org/wiki/Deltahedron

## Note.

The tetrahedron is the only deltahedron with 4 faces.

The triangular bipyramid is the only deltahedron with 6 faces.

There are at least five examples of deltahedra with 10 faces: the pentagonal dipyramid, the augmented octahedron, and the three ways to augment the biaugmented tetrahedron.