

Let $a_3(n)$ be the least k > n such that nk or nk^2 is a cube, and let A299117 be the image of $a_3(n)$.

Question. Is there another way to characterize what integers are in A299117?

Note. The function a_3 is an injection.

A299117 contains every cube, because $a(n^3) = (n+1)^3$.

A299117 contains the square of every prime, because $a(p) = p^2$.

Related.

- 1. Does A299117 contain every square?
- 2. Does A299117 contain any squarefree number?
- 3. What about the generalization: the image of a_{β} where $a_{\beta}(n)$ is the least k > n such that nk, $nk^2, \ldots, nk^{\beta-2}$, or $nk^{\beta-1}$ is a β -th power? Prime β is an injection—is this well behaved?

References.

https://oeis.org/A277781 https://oeis.org/A299117