

BATES COLLEGE

SENIOR THESIS

Physics Simulations Using Javascript

Author:

Peter Krieg

Advisor:

Gene Clough

*Presented to The Department of Physics, Bates College
In Partial Fulfillment of the Requirements for the
Degree of Bachelor of Science*

Lewiston, Maine
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Declaration of Authorship

I, Peter Krieg, declare that this thesis titled, 'Physics Simulations Using Javascript' and the work presented in it are my own. I confirm that:

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- Where any part of this thesis has previously been submitted for a degree or any other qualification at this University or any other institution, this has been clearly stated.
- Where I have consulted the published work of others, this is always clearly attributed.
- Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this thesis is entirely my own work.
- I have acknowledged all main sources of help.
- Where the thesis is based on work done by myself jointly with others, I have made clear exactly what was done by others and what I have contributed myself.

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Abstract

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Bachelor of Sciences

Physics Simulations Using Javascript

by Peter Krieg

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Abbreviations

HTML	HyperText Markup Language
JS	JavaScript
API	Application Programming Interface

Dedicated to my parents

Introduction

0.1 What is a Physics Simulation?

The purpose of this thesis is to present a series of physics simulations, each modeling a specific problem of physics as realistically as possible. These simulations differ from *animations*, which can be seen as predictable representations that always display the same visual. Animations are analagous to a movie script: no matter how many times you watch the movie, it will always end in the same way. Simulations, on the other hand, need to adapt to variable conditions, and be based partly on random processes. This brings up the topic of *dynamic* vs. *static* animation. Most of the physics simulations in this thesis will be dyamic because they present a unique viewing each time they are run, and can also involve user feedback which influences the outcome of the simulation.

Any simulation requires creating the illusion of motion. Almost every form of projected motion media uses frames to accomplish this. Researchers have shown that to make the simulation look realistic, it must be presented at a rate of around 60-100 frames per second. Anything far slower than this, and the human eye will detect the “choppiness” of the simulation. People can’t detect anything much faster than 100 frames per second, so there is no need to project media faster than that, with the exception of slow-motion videography.

0.2 Methods of Producing a Simulation

The physics simulations in this thesis differ greatly from common animations. Movies and cartoons, for example, operate by displaying a series of images similar to one another, and displaying them as many frames per second to create the illusion of motion. My simulations, on the other hand, function by providing the *information* for each frame, and then providing the data for *how* the animation can be created. These instructions are passed onto the HTML5 canvas API, which creates the visual which can be seen in the web browser. Because physics simulations contain instructions instead of a series of images, the files of code take up far less space than a movie file would, for example. This is one primary advantage of coded simulations. Every simulation follows a similar set of steps, which can be simplified below:

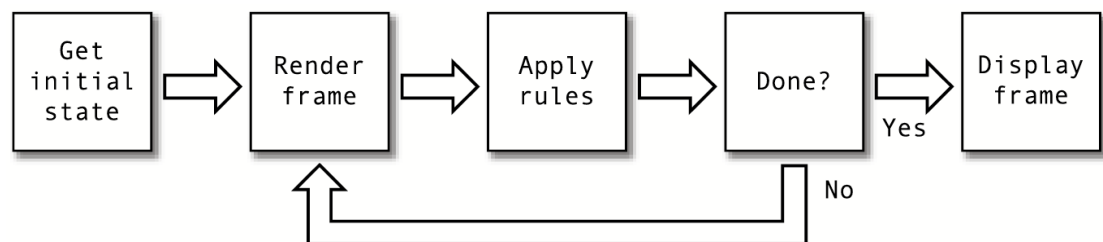


FIGURE 1: The frames of a general simulation

The canvas API gets the initial state of the simulation, which could be the position of a ball, for example. Then, the frame is *rendered* by applying rules to the canvas element, and changing the initial state of the simulation. Once the rules have been applied, and all conditions are satisfied, the frame is rendered, and then displayed on the canvas element, to be seen in the web browser.

To produce any realistic simulation, the steps in figure 1 must be repeated multiple times per second. In fact, these steps must be repeated 60 times per second to achieve the desired 60 frames per second outlined in the previous section. Luckily, the canvas API is capable of running the instructions very quickly to make this simulation possible.

0.2.1 The Code

To program the simulations in this thesis, I chose to write the code in javascript. This scripting language is easy to view in any modern browser: therefore, all the simulations of this thesis can be viewed online. Javascript combines seamlessly with HTML5, which is why I mostly decided to use it for this thesis. The evolution of HTML (HyperText Markup Language) has progressed from simple web documents to complex web applications. For this thesis, every simulation utilizes the HTML5 `<canvas>` element, which has been used since around 2011. The HTML5 canvas API allows programmers to write javascript code that accesses the element and runs visual displays through a web browser. The HTML needed to include a canvas can be seen below:

```
1 <!doctype html>
2 <html>
3   <body>
4     <canvas id="canvas" width="500" height="500" >
5   </body>
6   <script>
7     var canvas = document.getElementById('canvas');
8     var context = canvas.getContext('2d');
9   </script>
10 </html>
```

Listing 1: The bare bones code necessary for an HTML document to include the canvas element

The above code displays the most basic HTML combined with javascript necessary to begin any simulation. Lines 7-8 are the only ones that actually contain javascript: this is the simple step necessary for the canvas API to recognize the HTML document. These two steps are necessary for any physics simulation. The step on line 7 initializes a JS variable and sets it equal to the canvas element on the web document object. The second step

All web browsers include some form of javascript interpreter: whenever the browser encounters a `<script>` element, it “passes” the code onto the JS interpreter. In listing 1, the HTML and JS code are written in the same document for clarity. While this is an

acceptable practice, all future simulations will involve the HTML referencing to external JS documents to keep the contents separate.

While this thesis can contain code excerpts, figures, and screen-shots of various simulations, it obviously can't contain the flow of images itself. Therefore, I have put the entire thesis and its simulations on my personal website, which can be found at: <http://www.peterkrieg.com/thesis>. You can navigate by each chapter and view the simulations outlined in thesis.

Chapter 1

Some Basic Simulations

While the introduction outlined the computer programming necessary to produce simulations in general, this chapter will start to deal with the physics necessary to make simulations seem realistic. In this chapter, I will outline some examples of simulations with balls bouncing, and discussing the basic mechanics involved through the code.

1.1 Basic Ball Bouncing

A ball bouncing will show the basic kinematic equations, and how they are used in the javascript code. The following example displays a ball being dropped with an initial v_x , and bouncing off the walls and floor of the canvas element. The full code is shown

below:

```
1 var canvas = document.getElementById('canvas');
2 var context = canvas.getContext('2d');
3
4 canvas.height = screen.height-200;
5 canvas.width = screen.width -100;
6
7 var radius = 20;
8 var color = 'red';
9 var g = .1635; // acceleration due to gravity
10 var x = 40; // initial horizontal position
11 var y = 40; // initial vertical position
12 var vx = parseFloat(prompt('what is the initial horizontal speed of ball you
    would like?(recommended values of 1-20)')); // initial horizontal speed
13 var vy = 0; // initial vertical speed
14
15 window.onload = init;
16
```

```

17 function init() {
18     setInterval(onEachStep, 1000/60); // 60 fps
19 };
20
21 function onEachStep() {
22     vy += g; // gravity increases the vertical speed
23     x += vx; // horizontal speed increases horizontal position
24     y += vy; // vertical speed increases vertical position
25
26     if (y > canvas.height - radius){ // if ball hits the ground
27         y = canvas.height - radius; // reposition it at the ground
28         vy *= -0.8; // then reverse and reduce its vertical speed
29     }
30     if (x > canvas.width - radius){ // if ball hits right wall
31         x = canvas.width - radius; // reposition it right at wall
32         vx *= -0.8; // then reduce and reverse horizontal speed
33     }
34     if (x < radius){ // if ball hits left wall
35         x = radius; // reposition it right at wall
36         vx *= -0.8 // then reverse and reduce horizontal speed
37     }
38     drawBall(); // draw the ball
39 };
40
41 function drawBall() {
42     with (context){
43         clearRect(0, 0, canvas.width, canvas.height);
44         fillStyle = color;
45         beginPath();
46         arc(x, y, radius, 0, 2*Math.PI, true);
47         closePath();
48         fill();
49     };
50 };

```

Listing 1.1: A basic ball bouncing simulation

This code functions by first setting up the canvas to be an appropriate size, on lines 1-5. Then, the simple variables of radius, color, initial positions/velocities, and acceleration are initialized. As mentioned in the introduction, the canvas HTML element defines positions in terms of pixels, with the top left corner of the canvas being the origin. Therefore, the ball is initialized to appear at (40, 40) which is near the top left corner for any computer screen. The value of g , the gravitational constant, is set to .1635 to accurately represent its value near Earth's surface, of $9.81 \frac{m}{s^2}$. To understand why this value makes sense, it is necessary to understand the units of velocity on the HTML canvas. The position during the simulation is given in terms of pixels, which of course differs from the SI unit of meters. However, as long as g can be initialized to be $9.81 \frac{px}{s^2}$, the simulation will still look physically accurate. This can be explained with the equation below:

$$9.81 \frac{px}{s^2} = .1635 \frac{\frac{px}{s}}{frame} \times \frac{60frame}{s} \quad (1.1)$$

The value of g is calculated based on the fact that the simulation was run at 60 frames per second. Time is a central component of all physics, and for the simulations to behave realistically they must carefully take that into account.

The remainder of the code involves 3 functions that call one another to create the flow of the simulation. The first function, `init` (“initialize”) is called when the browser window is loaded (line 15). This function simply delays the next function, `onEachStep`, by 16.66 ms, meaning that the function essentially runs 60 times per second, producing the desired 60 frames per second. Line 18 accomplishes this in a crude method: simulations later will involve more sophisticated techniques. The `onEachStep` function contains the instructions for each frame of the simulation. It involves multiple conditional if-statement loops that create the illusion that the ball bounces off of the walls and floor.

All 3 conditional loops involve a coefficient of restitution, or C_r . This is a mechanical property, representing how “bouncy” the ball is, and measures the ratio of the kinetic energy after and before the impact. This is derived below:

$$C_r = \sqrt{\frac{KE_f}{KE_i}} = \sqrt{\frac{\frac{1}{2}mv_f^2}{\frac{1}{2}mv_i^2}} = \frac{v_f}{v_i} \quad (1.2)$$

A C_r value of .8 was used for this simulation, which is comparable to that of a tennis ball^[2]. The variable `Cr` represents this value in the code, and is simply multiplied by the velocity before impact, so the following equation results:

$$v_f = v_i * C_r \quad (1.3)$$

An essential part of any physics simulation involves *collision detection*. For the simple bouncing ball simulation, this is accomplished by conditional loops for if the ball's position exceeds the canvas constraints.

The last function of the program, drawBall, simply contains commands for the canvas API to draw. While these commands can be very complicated and intricate to create the exact visual aesthetic desired, the extent of these commands is not the purpose of this thesis. Basically, this function works by “erasing” the canvas of any previous graphics, and then creating a new visual with the arc() method.

The logic of the program can be summarized through the flow chart below:

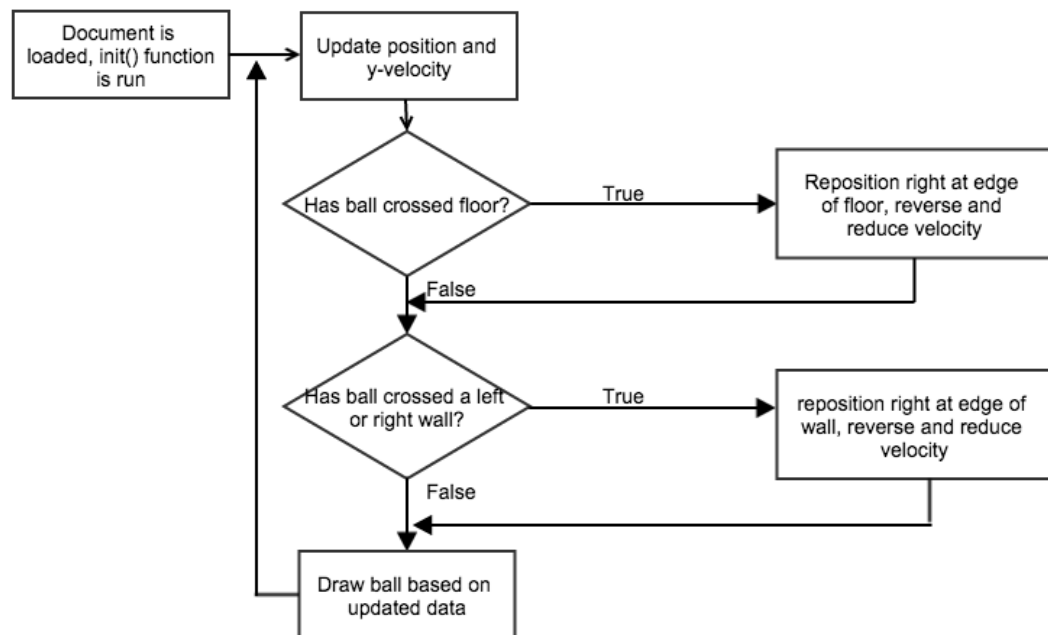


FIGURE 1.1: The logic flow chart of the basic bouncing ball simulation

1.2 More Advanced Ball Bouncing

While the previous example realistically incorporated the basic kinematic equations into account, it still fails to recognize important fundamentals of physics. The simulation in

this chapter will still be a simple ball bouncing, but will take into account air resistance and friction.

Appendix A

Appendix Title Here

THE APPENDIXGOESHERE

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Bibliography

- [1] Leslie Lamport, *TEX: a document preparation system*. Addison Wesley, Massachusetts, 2nd edition, 1994.
- [2] Roux, A., & Dickerson, J.(2007). ISB Journal of Physics *Coefficient of Restitution of a Tennis Ball*. Retrieved November 10, 2014, from <http://www.isb.ac.th/HS/JoP/vol1/Papers/Tennis>.