

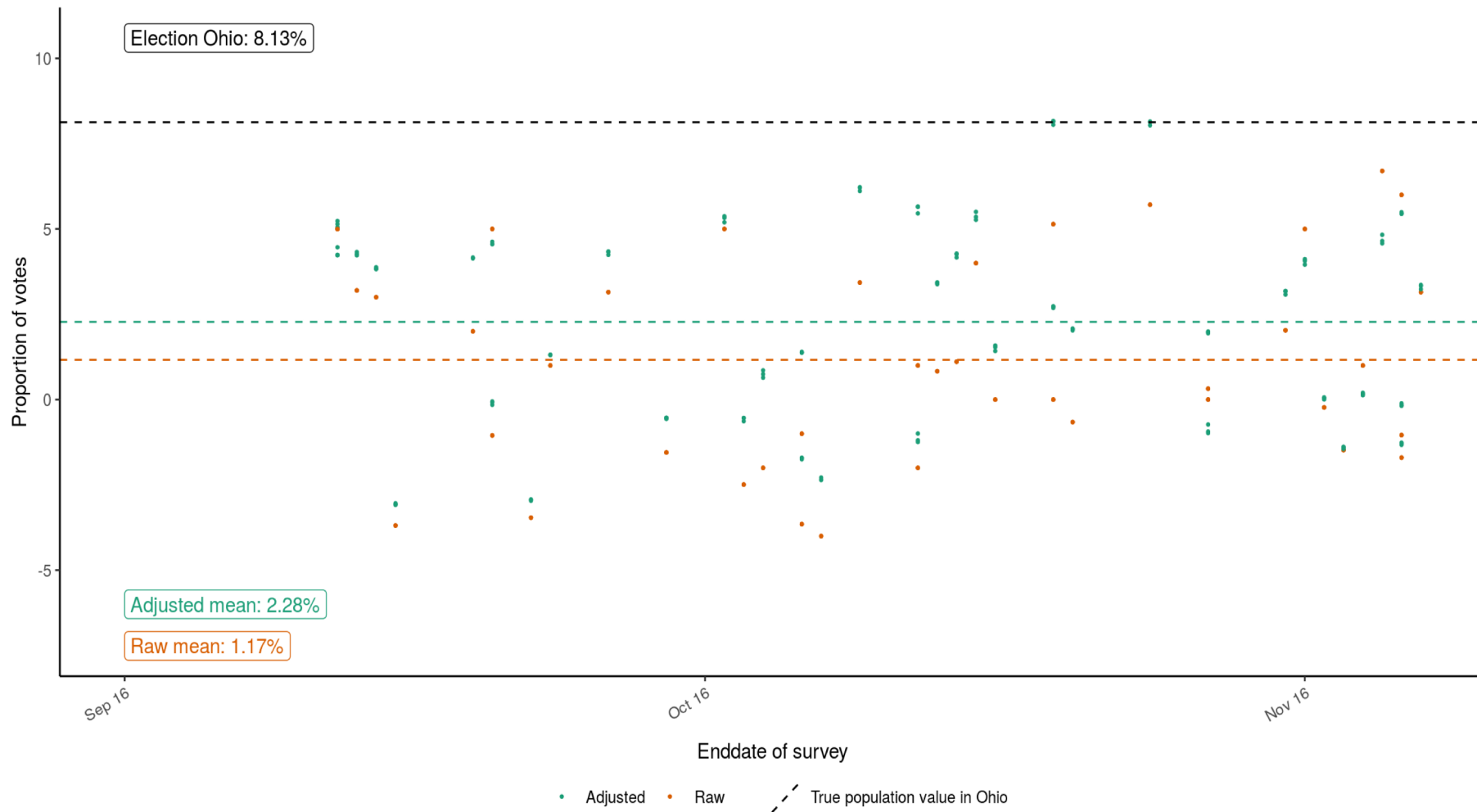
Survey data analysis  
Week 49:  
“Inference for non-probability  
samples”

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# Today

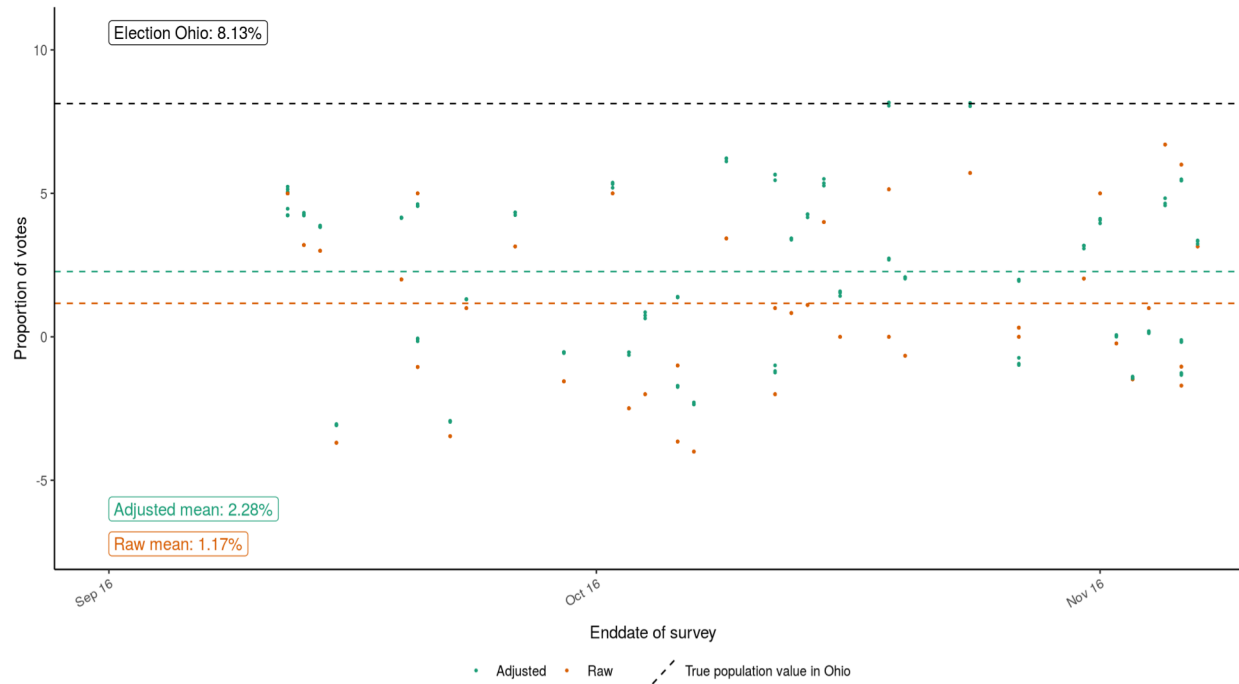
- Lecture
- Inference competition

# Back to week 37 (1)



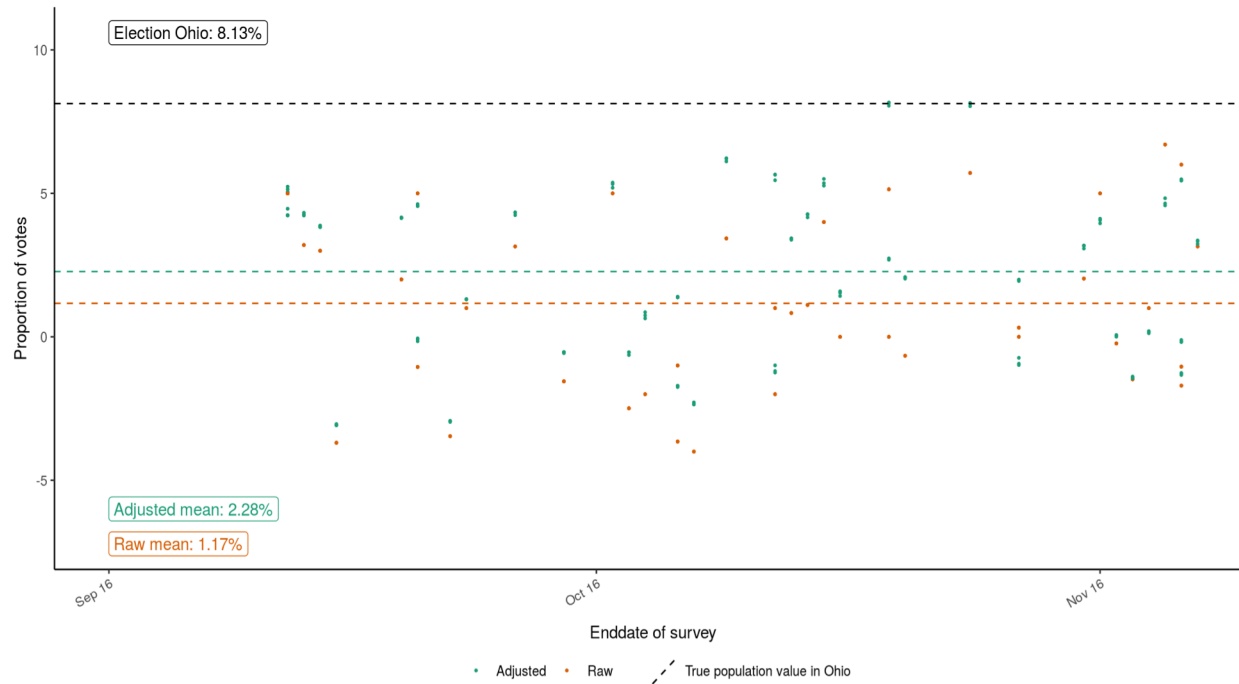
See: [https://utrecht-university.shinyapps.io/SDA\\_shinyelectionbias/](https://utrecht-university.shinyapps.io/SDA_shinyelectionbias/)

# Back to week 37 (1)



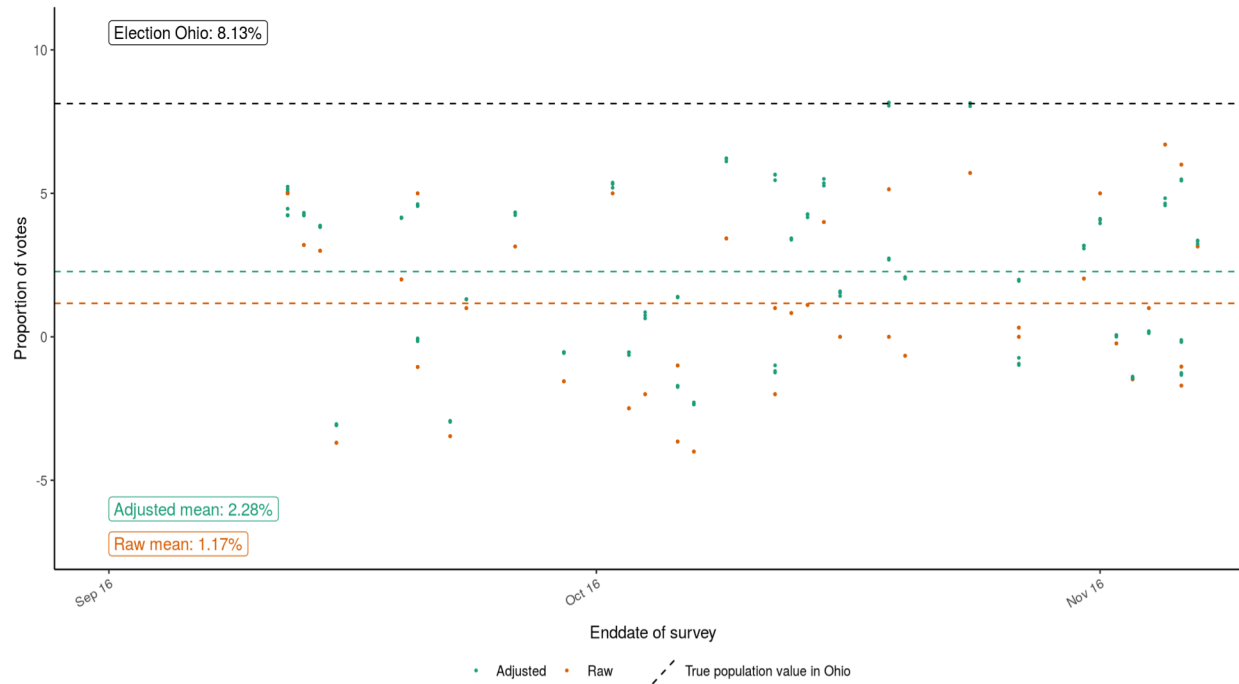
- Adjustments only help a bit on average
- For individual polls they sometimes make matters worse!

# Back to week 37 (1)



- Adjustments only help a bit on average
- For individual polls they sometimes make matters worse!
- Grade of pollster/ sample size/ population dont make the difference

# We have an inference problem



- Adjustments only help a bit on average
- For individual polls they sometimes make matters worse!
- Grade of pollster/ sample size/ population dont make the difference
- Problems with weighting
- A lot of polls are **not** probability based

# Cornesse et al (2020)

- When is a non-probability sample not too bad?
  - 
  -
- Global adjustment approaches
  - i.e. Conceptualize as design-based
- Estimate-specific approaches

# Cornesse et al (2020)

- When is a non-probability sample not too bad?
  - in change estimates? (perhaps regression?)
  - When controls are accurate (quota)
- Global adjustment approaches
  - i.e. Conceptualize as design-based
- Estimate-specific approaches



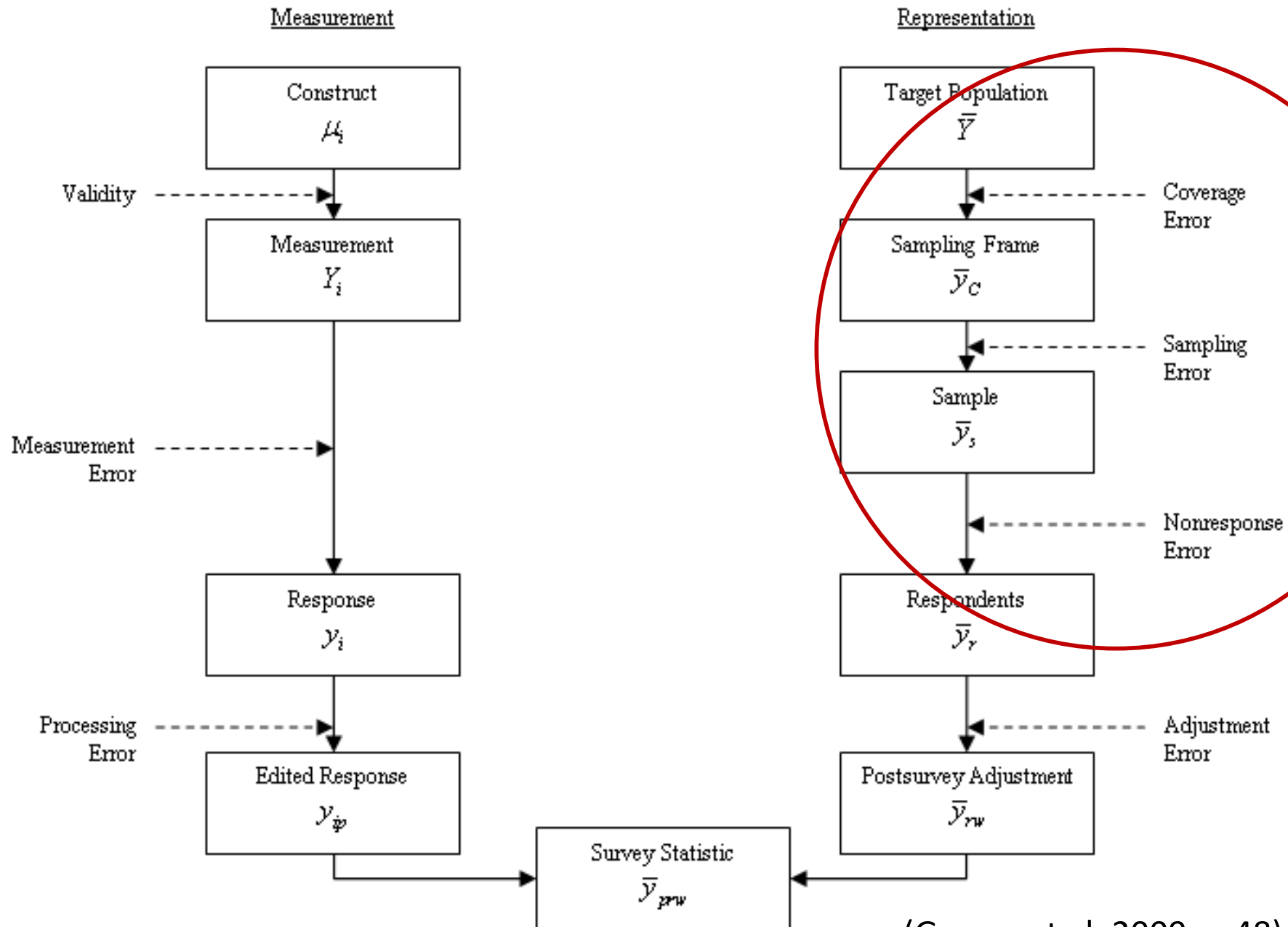
# Inference: perspectives from other fields

- Natural sciences
  - Laws of nature: gravity works everywhere
- Social sciences broadly
  - We need descriptives about our population
  - Causal inference with experiments not possible?
- Behavioral sciences (psychology)

# Inference: perspectives from other fields

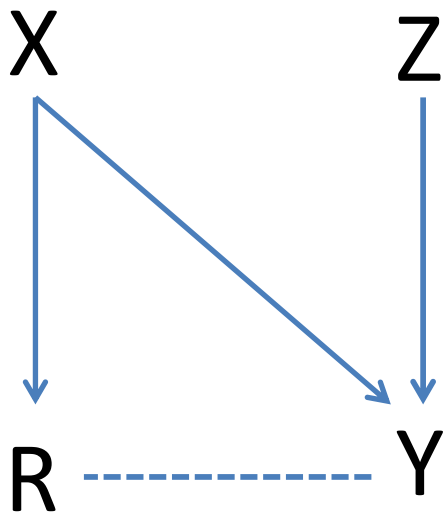
- Natural sciences
  - Laws of nature: gravity works everywhere
- Social sciences broadly
  - We need descriptives about our population
  - Causal inference with experiments not possible?
    - Regression, mediation etc.
  - Focus on external validity
- Behavioral sciences (psychology?)
  - Central role of experiments for causal analysis
  - Focus on internal validity

# Selection bias vs. TSE



(Groves et al. 2009, p.48)

# Selection bias as missing data problem



# Meng 2018 – linking data quality, quantity

- $\rho(R,G)$ : correlation between selection bias (R) and variable of interest
- $\sigma(G)$ : variation in population of variable of interest
  - E.g. If everyone votes for Clinton, no problem
- Data quantity:  $\sqrt{\frac{1-f}{f}}$  (week 39)
  - f=sampling fraction from population.

$$\overline{G}_n - \overline{G}_N = \underbrace{\rho_{R,G}}_{\text{Data Quality}} \times \underbrace{\sqrt{\frac{1-f}{f}}}_{\text{Data Quantity}} \times \underbrace{\sigma_G}_{\text{Problem Difficulty}} .$$

- P. 690 (eq 2.3)

# Meng 2018 – linking data quality, quantity

- R mechanism (response)
  - Design based
    - Sampling probabilities are known
    - Nonresponse propensities are modeled.
  - Non-probability: selection probabilities are unknown
- G: estimate of interest (e.g. a mean)
  - Y in missing data literature

$$\overline{G}_n - \overline{G}_N = \underbrace{\rho_{R,G}}_{\text{Data Quality}} \times \underbrace{\sqrt{\frac{1-f}{f}}}_{\text{Data Quantity}} \times \underbrace{\sigma_G}_{\text{Problem Difficulty}} .$$

- If correlation  $[R,G] = 0$ , no problem with any data
- If R does not vary over elements, no problem

# Meng 2018 – final

When can we draw inferences for Big Data (non-probability samples)?

1. Data quality:  $\rho(R,G)$ : 0
  - design based philosophy
  - Quality and quantity are independent (?)
2. Data quantity:  $f$  very large (close to 1)
  - Big data philosophy
  - Quality and quantity negatively correlated?
3.  $\sigma(G)$ : very small

$$\overline{G}_n - \overline{G}_N = \underbrace{\rho_{R,G}}_{\text{Data Quality}} \times \underbrace{\sqrt{\frac{1-f}{f}}}_{\text{Data Quantity}} \times \underbrace{\sigma_G}_{\text{Problem Difficulty}} .$$

# Solutions

- 1. Global correction methods
  - Pseudo design based estimation (Elliott & Valliant 2017)
- 2. Estimate-specific methods
  - Calibration (Little, 2004)
    - non-prob -> probability
  - Superpopulation modeling (e.g. Elliott & Valliant, 2020)
  - Mass imputation (Yang and Kim, 2020)
- 3. Sensitivity analyses
  - Meng: for  $p(R, G)$
  - Pattern mixture models for NMAR (e.g West 2020)



# Pseudo design based

non-probability based

gender	age	education	health	Favourite
0	34	1	5	vanilla
1	54	2	5	lemon
1	12	3	4	Choc
1	56	3	5	vanilla
0	87	4	2	strawb
1	45	5	3	zabaione
1	67	6	4	lemon
1	23	6	5	stracciac
0	16	2	5	vanilla
1	24	4	4	stracciac
1	56	2	4	stracciac
1	78	3	2	vanilla

Taste	percentage
Vanilla	33%
Lemon	16%
Stracciac	25%
Zabaione	8%
Strawberry	8%
Chocolate	8%

# Pseudo design based

non-probability based

gender	age	education	health	Favourite
0	34	1	5	vanilla
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1	45	5	3	zabaione
1	67	6	4	lemon
1	23	6	5	Banana
0	16	2	5	vanilla
1	24	4	4	pear
1	56	2	4	stracciac
1	78	3	2	vanilla

Other Probability based survey

gender	age	education	health	P(Response)
0	34	1	5	.24
1	54	2	5	.44
1	12	3	4	.23
1	56	3	5	.56
0	87	4	2	.36
1	45	5	3	.56
1	67	6	4	.44
1	23	6	5	.33
0	16	2	5	.32
1	24	4	4	.43
1	56	2	4	.42
1	78	3	2	.43



# Pseudo design based

non-probability based

gender	age	education	health	P(Response)	Favourite
0	34	1	5	.24	vanilla
1	54	2	5	.44	lemon
1	12	3	4	.23	Choc
1	56	3	5	.56	vanilla
0	87	4	2	.36	strawb
1	45	5	3	.56	zabaione
1	67	6	4	.44	lemon
1	23	6	5	.33	straccia
0	16	2	5	.32	vanilla
1	24	4	4	.43	straccia
1	56	2	4	.42	straccia
1	78	3	2	.43	vanilla

Taste	Raw percentage	Weight (1/p)
Vanilla	33%	1/.39
Lemon	16%	1/.44
Straccia	25%	1/.39
Zabaione	8%	1/.56
Strawberry	8%	1/.36
Chocolate	8%	1/.23

# Pseudo design based

non-probability based

gender	age	education	health	P(Response)	Favorite
0	34	1	5	.24	vanilla
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1	24	4	4	.43	straccia
1	56	2	4	.42	straccia
1	78	3	2	.43	vanilla

Taste	Raw percentage	Weight (1/p)	Weighted %
Vanilla	33%	1/.39	33%
Lemon	16%	1/.44	14%
Straccia	25%	1/.39	24%
Zabaione	8%	1/.56	6%
Strawberry	8%	1/.36	9%
Chocolate	8%	1/.23	14%
Ave		.40	

# Estimate specific methods

- Calibration (Little, 2004)
  - Bayes
- Superpopulation modeling (e.g. Elliott & Valliant, 2020)
- Mass imputation (Yang and Kim, 2020)

## 2.1 Calibration

- Conduct a large nonprobability sample
  - Small s.e., large bias(?)
- Conduct a small probability based sample
  - Large s.e., small bias
- Weight non-probability based -> prob based
  - Small bias (?), small s.e.
  - You can use lots of survey questions, because you conduct 2 surveys
  - Expensive, time consuming

## 2.1 Little (2004) Calibrated bayes

- Model based (regression) vs. design based
- Solution:
  - Use a model that includes design-based features
    - E.g. A fixed-effects regression model to deal with clustering
  - Bayesian modeling for variance estimation
    - Priors (often uninformative)
    - Posteriors for variance estimation
    - Remember convergence, traceplots,, and how imputations are generated in Mice?

## 2.2 Superpopulation modeling

- Non-probability based surveys don't use sample frames
  - We can rake or calibrate to population statistics: gender, age, region, ethnicity, income, education
- However, what if take an effort to collect more population statistics?
  - Netflix subscription? Voting Behavior, customer of a company, member of organization



## 2.2 Superpopulation modeling

- However, what if take an effort to collect more population statistics?
  - Netflix subscription? Voting Behavior, customer of a company, member of organization
- i.e. More elaborate weighting

Source: <https://www.pewresearch.org/methods/2018/01/26/reducing-bias-on-benchmarks/>

### Topics and corresponding benchmarks

Topic	Benchmark
<b>Civic engagement</b>	How often talks with neighbors
	Trusts neighbors
	Participated in a school group, neighborhood, or community association
	Volunteered in past year
<b>Family</b>	Marital status
	Presence of children in household
	Household size
<b>Financial</b>	Employment status
	Home ownership
	Family income
	Household member received food stamps
	Health insurance
<b>Personal</b>	Lived in house or apartment one year ago
	Active duty military service
	U.S. citizenship
	Gun ownership
	Smoking
	Food allergies
	Voted in 2012
<b>Political engagement</b>	Voted in 2014
	Contacted or visited a public official in past year
<b>Technology</b>	Tablet or e-reader use
	Texting or instant messaging
	Social networking

Note: See Appendix D for the source of each benchmark, the question text, the response categories, the benchmark estimate, and additional notes.

"For Weighting Online Opt-In Samples, What Matters Most?"

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## 2.3 Mass imputation

- We know the population distribution:
  - Gender, age, education, income, region, etc.
- In some cases we have frame data
- Why not impute the whole population?

# Mass imputation

- We know the population distribution:
  - Gender, age, education, income, region, etc.
- In some cases we have frame data
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1	56	2	4	straccia
1	78	3	2	???
1	56	4	5	???
....	...	...	..	???
You have X million rows, only X thousand of these have Y				

# 3. Sensitivity analyses

- Cf Meng (2018)
- Pattern Mixture modeling
  - Enter an additional parameter in the model (e.g a selection bias parameter)
  - This parameter can take different forms
    - Covary with Y and all other parameters
  - Simulate
  - Similar to Heckman selection models.

See Andridge, R. R., & Little, R. J. (2011). Proxy pattern-mixture analysis for survey nonresponse. *Journal of Official Statistics*, 27(2), 153.

# Exercise (class + THE)

- Competition!
  - Three non-probability samples
  - Sample size 30.000
  - June/July 2016
  - You get 15.000 cases
  - And a superpopulation dataset (Mercer, Lau & Kennedy, 2018)
- Goal: adjust your sample:
  - Choose your variables
  - Calibrate, rake, impute?
- Prize: eternal fame and a survey related present

# Next week

- Lecture on “designed big data”
- Keep working on your group assignments
- In two weeks -> presentation
  - See schedule on Blackboard
  - Grading rubric

# More reading?

- Andridge, R. R., & Little, R. J. (2011). Proxy pattern-mixture analysis for survey nonresponse. *Journal of Official Statistics*, 27(2), 153.
- Chen, S., Yang, S., & Kim, J. K. (2020). Nonparametric Mass Imputation for Data Integration. *Journal of Survey Statistics and Methodology*.
- Elliott, M. R., & Valliant, R. (2017). Inference for nonprobability samples. *Statistical Science*, 32(2), 249-264.
- Kim, J. K., Park, S., Chen, Y., & Wu, C. (2018). Combining non-probability and probability survey samples through mass imputation. *arXiv preprint arXiv:1812.10694*.
- Rafei, A., Flannagan, C. A., & Elliott, M. R. (2020). Big Data for Finite Population Inference: Applying Quasi-Random Approaches to Naturalistic Driving Data Using Bayesian Additive Regression Trees. *Journal of Survey Statistics and Methodology*, 8(1), 148-180.
- Valliant, R. (2020). Comparing alternatives for estimation from nonprobability samples. *Journal of Survey Statistics and Methodology*, 8(2), 231-263.