The Role of Supercluster Filaments in Shaping Galaxy Clusters

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ABSTRACT

Context. In a hierarchical Λ CDM Universe, cosmic filaments serve as the primary channels for matter accretion into galaxy clusters, influencing the shape of their dark matter halos.

Aims. We investigate whether the elongation of galaxy clusters correlates with the orientation of surrounding filaments, providing the first observational test of this relationship in large supercluster regions.

Methods. We have identified and characterized cosmic filaments in two dimensions within the two superclusters that are part of the low-redshift sub-survey of the Chilean Cluster Galaxy Evolution Survey (CHANCES): the Shapley supercluster and the Horologium-Reticulum supercluster. We analyze the alignment between filament directions—traced by galaxy distributions—and the triaxiality of cluster gravitational potentials—traced by X-ray emission—using publicly available optical and X-ray data.

Results. We have found that most (82%) of the X-ray clusters are associated with and interconnected by the optically detected filaments. The clusters-filaments alignment analysis shows that the elongation of most clusters is well aligned with nearby filaments, providing observational confirmation of theoretical predictions, with the alignment progressively reducing at larger cluster-centric distances (> 1.6 r_{200}).

Conclusions. Overall, our results support the notion that filaments are the main source of galaxy accretion at redshift below 0.1, and additionally provide evidence that matter accretion through filaments shapes the gravitational potential of galaxy clusters. We propose this measurement as a simple observational proxy to determine the direction of accretion in clusters, which is key to understanding both galaxy evolution and the merger history of galaxy clusters.

Key words. galaxies: clusters: general – galaxies: clusters: intracluster medium – (cosmology:) large-scale structure of Universe

1. Introduction

The Large-scale Structure (LSS) of the Universe is composed by an intricate and inhomogeneous distribution of matter known as the cosmic web. This structure is constituted by four main components: nodes (also referred to as galaxy clusters) containing up to thousands of galaxies in a sphere of $\sim 1-2$ Mpc radius, filaments, sheet-like walls, and large-scale voids spanning up to hundreds of megaparsecs in size (e.g. Cautun et al. 2014). This web-like structure has been shaped by the anisotropic nature of the gravitational collapse (Peebles 1980), following a well-defined sequence that began with regions collapsing along one axis to form walls, then along another axis to form filaments, and finally collapsing in all directions to form nodes (e.g. Zel'Dovich 1970; Arnold et al. 1982; Shandarin & Klypin 1984).

Although filaments occupy less than ten percent of the total volume of the present Universe, they contain more than half of the mass (e.g. Cautun et al. 2014; Tempel et al. 2014; Cui et al. 2019; Martizzi et al. 2019), and are the main channels through which it is transported across the cosmic web. The intersections of filaments host galaxy clusters, where the mass den-

sity $1 + \delta^1$ exceeds ~ 100 the background average density (e.g. Cautun et al. 2014). Clusters are thought to grow from the accretion of dark matter, gas, and galaxies. If this accretion happens mainly through cosmic filaments (as suggested, for example, by Kravtsov & Borgani (2012), Cautun et al. (2014) and Umehata et al. (2019)), a connection is expected between the cluster geometry, its gravitational potential, and the orientation of its associated filaments.

Indeed, the flow of matter into galaxy clusters is highly anisotropic (e.g. Gouin et al. 2021), rather than uniformly from all sides, indicating preferential directions along which accretion occurs through the filaments, and several studies have focused on studying this correlation on isolated systems using different indicators. Considering that cluster members tend to be distributed preferentially in line with the position angle (PA) of the major axis of the Brightest Cluster Galaxy (BCG) (e.g. Sastry 1968), Smith et al. (2023) studied the relation between the position angle of the BCG and the projected orientation of the filaments connected to the clusters, founding a strong sign of alignment between the distribution of galaxies and the PA of the BCG, as well

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For simplicity, Cautun et al. (2014) computed the density ρ in units of the mean background density $\bar{\rho}$ as $1 + \delta = \rho/\bar{\rho}$.

as with the LSS filaments around the clusters, even at distances of ~ 10 Mpc. From the theoretical side, using 324 simulations of massive clusters and their surrounding environment from The ThreeHundred project (Cui et al. 2018; Mostoghiu et al. 2019; Wang et al. 2018; Arthur et al. 2019; Ansarifard et al. 2020; Santoni et al. 2024), Kuchner et al. (2020) have also shown strong signs of alignment between the major axis of the cluster darkmatter halos and the connected filaments.

Cosmic filaments play a key role in shaping the structure of galaxy clusters through anisotropic and directional matter accretion. As a result, the asphericity of clusters is a natural consequence of their alignment with these filaments, and reflects their relatively recent formation and the less evolved and relaxed state of their dark matter halos compared, for instance, to galaxy-sized halos (Flores et al. 2007). Analyses of simulation data (e.g. Cui et al. 2018; Kuchner et al. 2020) indicate that cluster halos are well approximated by ellipsoids defined by three principal axes, with a tendency toward prolateness over oblateness. From the observational side, it has been demonstrated that galaxy clusters are not spherical objects based on evidence from the optical distribution of cluster galaxies (e.g. Carter & Metcalfe 1980; Binggeli 1982; Shin et al. 2018), Sunyaev-Zel'dovich pressure maps (e.g. Sayers et al. 2011), strong and weak gravitational lensing (e.g. Oguri et al. 2009, 2010, 2012), and surface brightness maps in X-ray (e.g. Kawahara 2010; Lau et al. 2012). For a detailed review about the asphericity of galaxy clusters, see Limousin et al. (2013).

Several studies have shown that the elliptical shape of galaxy clusters is not fixed, but varies with redshift (z) and mass (e.g. Allgood et al. 2006; Despali et al. 2014; Suto et al. 2016; Vega-Ferrero et al. 2017), with more massive halos tending to be more elliptical than their lower-mass counterparts. Additionally, clusters connected to a larger number of filaments tend to be more elliptical, less dynamically relaxed, and accreting more mass (Gouin et al. 2021). The latter, combined with the fact that filaments are the main channels through which galaxy clusters are fed, suggests that a useful approach to studying cluster accretion is to characterize their gravitational potential and examine how it correlates with the surrounding filaments. This can help to identify which regions of clusters are most affected by filamentary inflow and provide insights into their dynamical state.

One of the most direct ways to characterize the geometry and gravitational potential of galaxy clusters in observations, and consequently the mass accretion onto them, is through X-ray surface brightness maps. It is well established that galaxy clusters emit X-rays (Sarazin 1986), with this radiation originating from the diffuse gas distributed within them, the so-called intra-cluster medium (ICM), which typically resides at temperatures of $10^7 - 10^8$ K. Unlike galaxies in clusters, the ICM is a collisional system that, as the gas falls into the cluster potential well, it converts its kinetic energy into thermal energy (Kravtsov & Borgani 2012) through the thermal bremsstrahlung process, the main cooling mechanism of the ICM (e.g. Sarazin 1986), transforming the kinetic energy of the ions into X-ray radiation.

One of the best environments to study the relationship between clusters and their surroundings is within superclusters. Superclusters can be considered as miniature Universes that contain all the large-scale structure components at the same time, representing the densest and most dynamically active environments where galaxies and their systems formed and evolve (Einasto et al. 2021). Since superclusters are not virialized structures, matter within them continues to interact dynamically, flowing along gravitational potentials toward the most massive structures and giving rise to the formation of walls, filaments, groups, and

clusters (Galárraga-Espinosa et al. 2020). As shown in Tanaka et al. (2007), the likelihood of finding filamentary structures is higher in superclusters. Following the supercluster classification by Einasto et al. (2014), such structures can be identified regardless of whether the supercluster is of the filament-type or spider-type, with filaments appearing in linear configurations in the former and in more radial patterns in the latter.

Given the above, the main goal of this work is to observationally determine, for the first time, whether there is a direct correlation between the projected orientation of optical filaments (as traced by galaxies) and the distribution of X-ray surface brightness in dozens of galaxy clusters that are part of two large nearby supercluster regions: the Shapley supercluster (SSC) and the Horologium-Reticulum supercluster (HRSC). We propose this measurement as a simple method to study the accretion process onto clusters through filaments.

Throughout this paper, M_{Δ} (where $\Delta \in \{200, 500\}$) refers to the mass within r_{Δ} , corresponding to the radius enclosing a density Δ times the critical matter density of the Universe at each redshift. Additionally, we assume cosmological parameters inferred by Aghanim et al. (2020), the most relevant of which are the current expansion rate, $H_0 = 67.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$, and the present-day matter density parameter, $\Omega_m = 0.315$.

For simplicity of the analysis, even though the filamentary structure that we study is inherently highly inhomogeneous, we ignore the question of how to calculate an averaged cosmological expansion model (Buchert 2000, 2001; Räsänen 2011; Krasiński et al. 2010; Bolejko et al. 2011; Wiltshire 2011; Buchert et al. 2015; Koksbang et al. 2024) and instead we adopt the usual assumption that filamentary structure dynamics are affected by the expansion, but the expansion itself is predetermined by the cosmological model parameters as a "background" unaffected by the filamentary structure.

The paper is organized as follows. In Sect. 2, we provide a brief overview of previous studies on the two superclusters considered in this work. In Sect. 3, we describe the optical catalog used to identify the LSS in both superclusters, as well as the X-ray data employed to characterize the galaxy clusters within them. In Sect. 4, we present the methods used for LSS identification, the determination of cluster shapes and inclinations from X-ray data, the projected inclination of filaments, and the analysis of cluster–filament alignments. In Sect. 5, we present the main results. Finally, conclusions and a summary of this work are provided in Sect. 6.

2. Overview of the target superclusters

The two large nearby superclusters studied in this paper were chosen because they contain dozens of clusters interconnected by filaments, and they have good optical and X-ray data available. In addition, they lie within the footprint of the extended ROentgen Survey with an Imaging Telescope Array (eROSITA) X-ray mission and the upcoming CHileAN Cluster galaxy Evolution Survey (CHANCES; Sifón et al. 2025), which will obtain over 500000 galaxy spectra in and around these two superclusters, as well as in 100 other clusters at 0 < z < 0.45, using the 4-metre Multi-Object Spectrograph Telescope (4MOST; de Jong et al. 2019). The survey aims to enable a more detailed and deeper analysis of these structures. Our work serves as a precursor to CHANCES and contributes to validating its target selection strategy (Méndez-Hernández et al. 2025b). In the following (Sect. 2 and 3), we describe the superclusters and the data available.

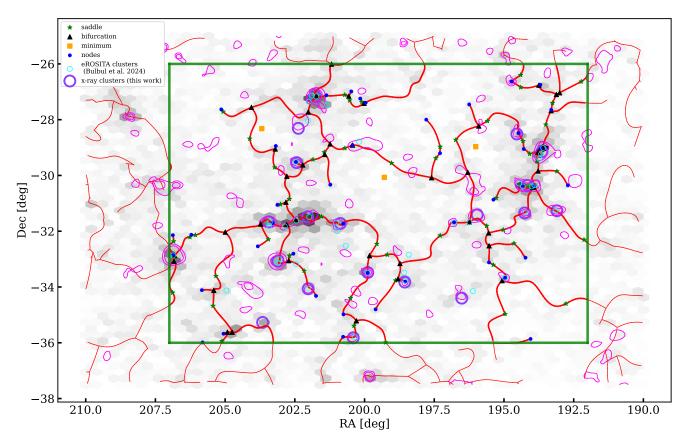


Fig. 1. Large-scale structure identification using DisPerSE in two dimensions within the SSC. Grey-scale hexagons show the density map of photometric members in the supercluster. Red lines indicate optically detected filaments, while different symbols correspond to critical points (see legend). Large-scale X-ray detections in the SSC area are in magenta contours. The cyan circles indicate clusters detected in the 0.2-2.3 keV as extended X-ray sources in the Shapley area and z range considered for this work (Bulbul et al. 2024), while purple circles are the large-scale emission in the band 0.6-2.3 identified as galaxy clusters used in this work. Green rectangle indicates the CHANCES coverage in SSC and the area considered for the optical-X-ray comparative analysis shown in Sect. 4.

2.1. The Shapley supercluster

The SSC is one of the most massive and densest superclusters in the local Universe, encompassing 25 clusters in the redshift range 0.03 < z < 0.06 over a $\sim 15 \times 10 \, \mathrm{deg^2}$ region (Raychaudhury 1989; Quintana et al. 1995a; Ettori et al. 1997; de Filippis et al. 2005; Proust et al. 2006; Quintana et al. 2020). Previous studies, such as Quintana et al. (1995b), based on spectroscopy within and up to 7 deg around the center of the supercluster, indicated that the SSC has a cigar-shape with the eastern side being the closest to us, showing a flattened geometry, which suggests that it is not spherical or virialized. The complex morphology of the SSC comprises a main body at $cz \sim 15000 \, \mathrm{km \, s^{-1}}$ together with walls and filaments of galaxies connecting the three main systems of interacting clusters (the A3558, A3528 and A3571 complexes) as well as a foreground structure connecting the SSC to the Hydra-Centaurus supercluster ($cz \sim 4000 \, \mathrm{km \, s^{-1}}$).

At the heart of the SSC is the high-density SSC core (Dec $\sim -31 \, \text{deg}$) at z = 0.048, comprising three Abell clusters and two poor clusters, forming an elongated structure 2 degrees ($\sim 7 \, \text{Mpc}$) in extent filled with hot gas (Ade et al. 2014). Past dynamical (e.g. Bardelli et al. 1994; Ragone et al. 2006) and X-ray (e.g. Kull & Böhringer 1999; Ettori et al. 2000; Finoguenov et al. 2004) studies revealed cluster-cluster interactions in the core region that is characterized by a complex dynamical state with several subcondensations and a diffuse filamentary X-ray emission across the whole region. More recently, Venturi et al.

(2022) detected a low-brightness intercluster diffuse emission at 1.28 GHz in the SSC core and interpreted it as a radio signature of a minor merger. Using the Shapley Supercluster Survey (ShaSS, Merluzzi et al. 2015), Haines et al. (2018) obtained a detailed map of the region around the supercluster core, which includes 11 SSC clusters. They showed that the 11 systems are all interconnected and lie within a coherent sheet of galaxies that fills the entire survey region without gaps (see also Reisenegger et al. 2000). This study also revealed a stream of galaxies from the northern cluster A3559 to the core.

We notice that the dynamical analysis of Haines et al. (2018) is the only study based on a spectroscopic catalog which is uniformly complete² across the considered region of the SSC (~ 21 deg² around the SSC core). However, this work is limited to the central region of a very complex structure. Other studies (e.g. Proust et al. 2006; Quintana et al. 2020; Aghanim et al. 2024) traced the whole supercluster structure covering up to 300 deg², agreeing on the map of the filaments as well as with the findings of Haines et al. (2018) for the SSC core. However, these works rely on the photometry from the SuperCOSMOS scans of photographic Schmidt plates³. They are based on collections of spectroscopic redshifts that, as expected, are highly complete (>80 percent) at the bright end of the galaxy luminosity function

² The ShaSS spectroscopic catalog is 95 percent complete at i=18 (see Haines et al. 2018, for details).

http://www-wfau.roe.ac.uk/sss/index.html

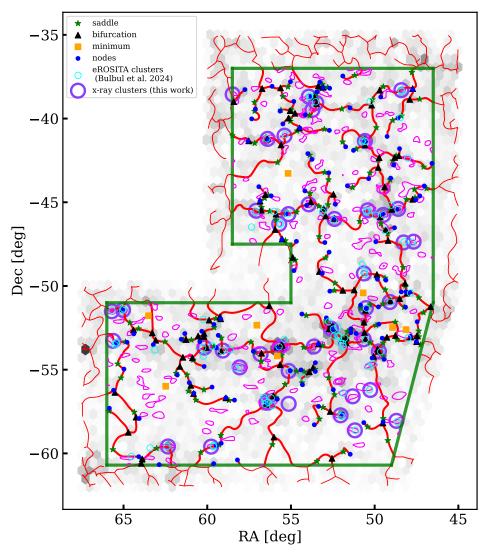


Fig. 2. Same as Fig. 1 but for HRSC. Green polygon indicates the area that CHANCES will observe.

 $(r \le 15)$. Still, their completeness drops to less than 20 percent at r = 17.5 (see Fig. 3 of Quintana et al. 2020) implying that the filaments turn out to be traced mostly by a few bright supercluster galaxies. CHANCES will go a step further, not only providing an accurate map of the filaments and infalling groups, but in particular, mapping the evolution of the supercluster members well outside the cluster cores and down to r = 20.4 - about M* + 5 at the SSC redshift.

2.2. The Horologium-Reticulum supercluster

The HRSC is the second-largest mass concentration in the local Universe (Zucca et al. 1993; Johnston-Hollitt et al. 2008), surpassed only by the SSC. The HRSC contains more than 20 optically identified galaxy clusters (Einasto et al. 2002) in the redshift range 0.04 < z < 0.08 within a region of ~ 150 deg² on the sky (Fleenor et al. 2006), and is composed of at least two major filaments (Einasto et al. 2003). HRSC can be separated into two main groups of galaxy clusters (Einasto et al. 2003), the northern clusters (-48 deg < Dec < -43 deg) at $z \sim 0.07$ and the southern clusters (-57 deg < Dec < -51 deg) at $z \sim 0.06$ (Fleenor et al. 2006). The HRSC center is defined by the double cluster complex A3125/ A3128 (RA ~ 52 deg, Dec ~ -53 deg)

(Rose et al. 2002). At ~ 2.5 deg ($\sim 10\ h^{-1}$ Mpc) east from the A3125/A3128 complex is located A3158, a compact cluster of richness class two (Quintana & Havlen 1979). These three clusters have long been known to be linked by a "bridge" of galaxies (Lucey et al. 1983) within the larger HRSC supercluster structure. The multiwavelength analysis performed by Rose et al. (2002) in A3125/A3128 uncovered rapidly infalling groups and filaments accelerated by the HR potential, suggesting evolving substructures across various mass scales.

Compared to the SSC, the dynamical state of the HRSC environment outside rich systems has not been extensively studied. Fleenor et al. (2006) conducted one of the first studies focusing on the intercluster regions in HRSC by performing wide-field spectroscopy with the Dual Beam Spectrograph. From this study has been revealed a main concentration of intercluster galaxies covering $cz \sim 17000$ - 22500 km s⁻¹ that consists of two major components in redshift space, separated by 2500 km s⁻¹ (35 Mpc), each with a similar inclination in the position-redshift space at the same position angle.

In summary, their high density and gravitational influence make SSC and HRSC significant sites for studying large-scale structure formation and the impact of the environment on galaxy clusters, as well as galaxy evolution.

3. Data

To characterize LSS in supercluster regions and identify the filaments connecting clusters within them, we use optical galaxy data from superclusters selected in the context of target selection for the CHANCES 4MOST survey (Sect. 3.1). These structures are then compared with the X-ray emission observed by eROSITA, as described in Sect. 3.2.

3.1. Optical data from the CHANCES target catalog

While SSC and HRSC have been studied previously, no deep and wide homogeneous spectroscopic datasets are yet available to examine them in detail. This has motivated CHANCES to include these two superclusters in their survey. CHANCES will target galaxies in these regions down to r=20.4, along with galaxies in other 100 clusters at z<0.45 to be observed with the 4MOST spectrograph. CHANCES is split in three subsurveys: CHANCES Low-z (z<0.07), CHANCES Evolution (0.07 < z<0.45) and CHANCES Circumstellar Galactic Medium at z>0.35 (see Haines et al. 2023, for details). The Low-z CHANCES sub-survey targets galaxies brighter than r=20.4 in 50 z<0.07 clusters out to $5 \times r_{200}$ and the two large supercluster regions (SSC, HRSC), which are the focus of this paper. Cluster selection and properties as well as the definition of the superclusters regions are detailed in Sifón et al. (2025).

Galaxy target selection within the superclusters (and CHANCES clusters more broadly) was guided by a combination of photometric redshifts to efficiently identify likely cluster members and exclude outliers. As explained in detail in Méndez-Hernández et al. (2025b), to select targets for CHANCES Low-z sub-survey⁴, we used both publicly available photometric redshifts (z_{phot}) from Legacy Survey DR10 (Zhou et al. 2021), as well as proprietary z_{phot} from S-PLUS. For fainter galaxies (r > 18.5), we use a combination of S-PLUS custom-derived photometric redshifts based on the Legacy Survey to minimize bias against faint red galaxies (Teixeira et al., in prep). In this paper, since the aim is to characterize the LSS minimizing any possible biases, we focus only on bright targets (r < 18.5) where photometric redshifts are most reliable. We also focus exclusively on Legacy Survey DR10 photometric redshifts (and exclude S-PLUS) to ensure homogeneity, as all the area studied is covered homogeneously by Legacy Survey.

Additionally, as in Méndez-Hernández et al. (2025b), available spectroscopic redshifts from the literature were used to confirm supercluster members and remove outliers, and to compute the completeness and purity of the target catalog. Catalog completeness was defined as the fraction of previously known spectroscopic members of the superclusters that are successfully retrieved through the photometric target selection, while purity was defined as the fraction of the selected photometric supercluster candidates that have been spectroscopically confirmed as members. For SSC, completeness and purity are 0.93 and 0.70, respectively, and for HRSC they are 0.91 and 0.94.

The $z_{\rm phot}$ ranges of bright CHANCES low-z sub-survey targets for SSC and HRSC — $0.027 < z_{\rm phot} < 0.073$ and $0.037 < z_{\rm phot} < 0.083$, respectively — were defined to include both photometric member galaxies and the clusters associated with each supercluster. Note that these ranges are wider than those

assumed in previous works (for example, 0.035 < z < 0.058 in Haines et al. (2018) and 0.03 < z < 0.06 in Quintana et al. (2020) for SSC, and 0.04 < z < 0.07 in Rose et al. (2002) for HRSC). This discrepancy arises from our use of $z_{\rm phot}$ for membership determination, which introduces larger uncertainties compared to spectroscopic membership.

The CHANCES coverage of the SSC consists of 128 deg² plus the remaining area within $5r_{200}$ of A3571 (see Sifón et al. 2025). The SSC region includes ~ 25 galaxy clusters at 0.037 < z < 0.056 (e.g. Haines et al. 2018), with A3558, A3562, and A3528 as prominent components. Other low-z clusters overlap the superclusters in the sky (namely, A3565 and A3574 with Shapley), but they are at noticeably different redshifts, and target overlap is minimal. For the case of HRSC, CHANCES covers an area of ~ 225 deg², containing the HRSC center (RA ~ 52 deg, Dec ~ -53 deg) plus the marginally overlapping $5r_{200}$ area around A3266, at a mean z = 0.06. Similar to SSC, just at the northern border of the HRSC there is a partial area overlap with a lower redshift Fornax cluster, whose contamination is removed using redshift information.

In this work, we considered areas $\sim 1-2$ degrees wider than the CHANCES coverage of the superclusters to characterize the LSS without introducing edge effects within the CHANCES fields. The studied areas can be appreciated in Fig. 1 and 2 along with the CHANCES fields (green).

3.2. X-ray data from eROSITA

The CHANCES survey has a great synergy with eROSITA, complementing the optical information with X-rays to better characterize large-scale structure. The two superclusters studied in this paper are fully covered by eROSITA.

eROSITA is a German telescope onboard the Spectrum-Roentgen-Gamma satellite, which has performed an all-sky Xray survey, and has deeper sensitivity compared to the previous ROSAT All-Sky Survey, with a spatial resolution of 30" (Predehl et al. 2021). The publicly released year 1 eROSITA-DE data (hereinafter eRASS1) cover half of the sky. We used both the 0.6-2.3 keV and 0.2-2.3 keV band images of eROSITA, together with the officially released exposure and background files⁵. We perform a wavelet image decomposition (Vikhlinin et al. 1998, b) to separate the unresolved emission from the cluster emission. Further details on the wavelet decomposition method can be found in Vikhlinin et al. (1998). The sources detected on spatial scales up to 32 arcseconds are excised from the flux extraction, a procedure similar to other published eROSITA analyses (Reiprich et al. 2025). For the redshifts of this study, we benefit from the image reconstructions on scales up to 16 arcminutes. Larger scales require reconsidering the background estimates obtained using in-field estimates after source removal. For the science of this study, these spatial scales are not required.

In our work, we used the 0.6 - 2.3 keV band for the analysis of large-scale emission. This is because the 0.2–2.3 keV band is confusion-limited on scales of 16 arcminutes and has a higher background, due to Galactic foreground emission, and in addition is subject to solar leaks, which lead to a temporal increase in the level of the background below 0.6 keV. In estimating the shape of the emission, we used the surface brightness in units of counts/s/pixel, in which we used the binned pixels of 32 arcseconds on a side.

⁴ The CHANCES-low-z sub-surveys were compiled using the Efficiently Extracting Cluster candidate members with Homogeneity using Optical colour and photometric-z (EECHOz; Méndez-Hernández et al. 2025a) code, available at https://github.com/4MOST-CHANCES/CHANCES-EECHOz-Low-redshift-TargetSelection.

⁵ https://erosita.mpe.mpg.de/dr1

⁶ https://github.com/avikhlinin/wvdecomp

We have run Source Extractor (Bertin & Arnouts 1996) to characterize the sources detected on scales of 2-4 and 8-16 arcminutes, storing the positional angle together with values of major and minor axes. To select the sources associated with the superclusters and to remove clusters at other redshifts, we run the identification of sources using version 8 (Python) of the redsequence Matched-filter Probabilistic Percolation cluster-finding algorithm code (redMaPPer, Rykoff et al. 2014) in scan mode (e.g. as in Ider Chitham et al. 2020; Kluge et al. 2024), which for the location of our sources utilized the 10th Data Release of the DESI Legacy Imaging Surveys (LS-DR10; Dey et al. 2019). To complete the identification of sources, we added the eROSITA sources identified with the 2MRS group catalog (Tempel et al. 2018), which has better sensitivity towards low mass systems at z < 0.04, important for the SSC. Tables A.1 and A.2 show the main properties of the detected X-ray clusters in SSC and HRSC, respectively. We present the X-ray luminosity in the rest-frame 0.1-2.4 keV, applying band and K-corrections computed using the eRASS1 release of eROSITA responses. We refer to Pederneiras et al. (2025) for the weak lensing calibration of eRASS1 luminosities in the 0.1-2.4 keV band and a comparison to previous scaling relations. We report masses and virial radii computed using those scaling relations and X-ray luminosities.

4. Method

Our goal is to compare the shape and alignments of individual clusters to the filaments that connect them in supercluster regions. To do that, we first identify the filament network (Sect. 4.1), before determining the inclination angles of filaments to the galaxy clusters (Sect. 4.2). Finally, we fold in the information of shapes of clusters inferred from X-ray emission (Sect. 4.3)

4.1. Identification of cosmic filaments

Filament detection in both superclusters was performed using the Discrete Persistence Structures Extractor (DisPerSE⁷; Sousbie 2011), a topological tool based on discrete Morse theory and persistence theory. DisPerSE has been widely applied to identify filaments, nodes, walls, and voids from discrete source distributions, both in simulations (e.g. Galárraga-Espinosa et al. 2020; Kuchner et al. 2020) and in observational data (e.g. Bonjean et al. 2020; Smith et al. 2023).

In short, DisPerSE uses the point distribution, in our case the galaxy coordinates, to reconstruct the area of the sky that we are studying as cells, edges, and vertices. To estimate the density field of this distribution, it employs the Delaunay tessellation, where the density around each vertex of the Delaunay complex is calculated using the Delaunay Tessellation Field Estimator (Schaap & Van De Weygaert 2000; Cautun & van de Weygaert 2011). To extract filaments and nodes from this density field, DisPerSE identifies the critical points where the gradient vanishes -such as maxima, minima, and saddle points- and connects them along ridges. The filamentary structure is traced by field lines tangent to the gradient at each point. These filaments are identified by computing small segments that connect topological saddle points to maxima (nodes), forming a continuous skeleton of the cosmic web. In this network, filaments are represented as arcs connecting critical points: maxima, which are of third order in three dimensions and second order in two dimensions, and saddle points, which are of second or first order in three dimensions and of first order in two dimensions.

The significance of each connection is quantified by the persistence, a measure of the significance of topological connections between critical points, and is defined as the density contrast between a pair of critical points. The persistence is typically expressed in units of its standard deviation σ . A higher value of σ allows us to filter and remove noisy structures.

In our work, the filaments were detected in two dimensions, using as input the positions of the photometric members on the sky, considering for each supercluster just one redshift slice that encompasses the total redshift range mentioned in Sect. 3.1. The Delaunay tessellation was done assuming smooth boundary conditions. To extract filaments and critical points, we assumed a persistence threshold of 3σ , and a smoothness level of the skeleton of 20. Fig. 1 and 2 show the LSS identification for SSC and HRSC, respectively. Different symbols represent different critical points given by DisPerSE. At the same time, we have included in the two figures the large-scale X-ray detections (magenta contours) from our own data reduction (see Sect. 3.2) in the SSC and HRSC area, as well as the clusters from the eRASS1 Galaxy groups and clusters primary catalog (cyan circles; Bulbul et al. 2024) that lie within the redshift range assumed for photometric members. Note that the resolution on the density map of photometric members (grey-scale density map) used in the figures is too low to see all the clusters from the public catalog. Additionally, in Fig. 1 and 2, we have included the X-ray catalog of large-scale sources used in this work as purple circles. Note that, compared to the public catalog, the sources in our catalog are extended, and in some cases, multiple sources listed separately in the public catalog correspond to a single source in our case.

To validate our method for selecting supercluster members and identifying filaments, we compared the filamentary structures detected using photometric data with those obtained in a smaller region uniformly covered by spectroscopic observations from the ShaSS survey (see Sect. 2.1), complemented by a compilation of additional spectroscopic data in the same ShaSS area from Quintana et al. (1995b), Quintana et al. (1997), Drinkwater et al. (2004), Proust et al. (2006), Jones et al. (2009), and Quintana et al. (2020), to include the majority of spectroscopically confirmed sources in the region. A match of the sky positions was performed in order to remove sources with duplicates across the different spectroscopic catalogs. Filaments from the spectroscopic catalog were detected in two dimensions, like those from the photometric catalog, using a galaxy sample within the redshift range adopted by Quintana et al. (2020) (0.03 < z < 0.06), providing a more accurate membership of galaxies in the SSC core, while for the filaments extracted from the photometric sample we adopted the redshift range for the SSC described in Sect. 3.1. The left panel of Fig. 3 shows in orange the filaments detected from the photometric catalog in that area and in green the filaments obtained using the spectroscopic data. Note that the orange filaments in this Fig. are not the same as the red filaments in Fig. 1 due to the different area in which we ran Dis-PerSE. However, the main structures in the SSC core prevail. When comparing the spectroscopically detected filaments with the photometric ones in the same area, we find that qualitatively, the two networks agree well, except for a photometric filament detected at RA ~ 201 deg that is not detected on the spectral sample. We notice that Higuchi et al. (2020), using ShaSS data, measured a mass peak at RA=202.1 deg, Dec=-32.7 deg, identified as a background cluster at z = 0.17. The cluster position matches that of the pronounced curve of the photometric redshift filament. This background cluster, together with other structures

⁷ https://www2.iap.fr/users/sousbie/disperse.html

behind the supercluster (see Fig. 7 of Haines et al. 2018), may contribute to tracing the filaments, considering the wider redshift range adopted for the photo-z and their larger errors with respect to the spectroscopic redshifts.

To quantify the similarities (or discrepancies) between the LSS skeletons obtained from the photometric and spectroscopic samples, we followed the method introduced in Sousbie (2011) and used in Sarron et al. (2019), Laigle et al. (2018), and Kuchner et al. (2020), which provides an indicator of the reliability of filament extraction using two-dimensional photometric and spectroscopic data. For this purpose, we measured the projected distances between the photometric and spectroscopic skeletons to obtain the differential distribution (PDF). The projected distances were computed between each segment point on the photometric network and the nearest segment point on the spectroscopic network. The right panel of Fig. 3 shows the resulting PDF obtained by comparing photometric to spectroscopic (orange curve) and spectroscopic to photometric (green curve) filaments, from which we obtained median values of 0.36 Mpc and 0.29 Mpc, respectively. Given the common assumption that filament thickness is of the order $\sim 0.7 - 1$ Mpc (e.g. Colberg et al. 2005; Tempel et al. 2014; Martínez et al. 2016; Kooistra et al. 2019; Sarron et al. 2019; Kuchner et al. 2020), our median values suggest a typical offset smaller than the characteristic filament thickness.

4.2. Characterization of cosmic filaments

We ultimately want to compare the location and projected orientation of filaments with the shape of the clusters.

To do this, we first create catalogs of optical filaments connected to X-ray clusters, adopting the definition used in Kuchner et al. (2020). In that work, a filament is defined as a segment that is connected to a cluster and extends beyond a sphere of 1 r_{200} (in three-dimensional space) around the center of the main dark matter halo. Since our work was carried out using two-dimensional data (positions projected in the plane of the sky), the corresponding set of filaments connected to a cluster is those exiting a circumference projected on the sky of $1r_{200}$ centered on the position of the X-ray peak. To compute the projected inclination, we use the filament segment located between 0.8 and 1.2 times the r_{200} of the corresponding X-ray cluster. This range is chosen to approximate a straight section of the filament, ensuring a more reliable inclination estimate. In addition, we also compute projected filament inclinations at 1.4–1.8 and 3.0–3.4 times the r_{200} to investigate how the alignment between filaments and clusters varies with distance from the cluster center.

Then, to determine the average projected inclinations of filaments connected to galaxy clusters, we used the Probabilistic model-based Hough Transform technique (PHT, Tino et al. 2011), a Bayesian method to determine alignments in data points based on the original idea of the Hough Transform (Hough 1962). If N is the total number of segment points of a filament, a Gaussian noise model with covariance $\Sigma_{\alpha,r}^{8}$ is assumed for each segment point. The model assumed in this work is given by

$$p(x|\alpha, r) = \frac{1}{2\pi |\Sigma_{\alpha, r}|} \exp\left[-\frac{1}{2}(x^T - (r \cdot \cos \alpha, r \cdot \sin \alpha))\right]$$
$$\Sigma_{\alpha, r}^{-1}(x - (r \cdot \cos \alpha, r \cdot \sin \alpha)^T). \tag{1}$$

From this, PHT determines the probability density for each point x of belonging to a straight-line model defined by the parameter pair (α, r) — the inclination angle and the perpendicular distance from the origin to the line in polar coordinates, respectively. In our case, the model corresponds to a straight line passing through the origin, and includes a neighborhood region around the origin. In our case, the origin corresponds to each point along the filament segment over which we iterate during the computation. This origin changes from point to point. However, the distance to neighboring points — computed in two dimensions on the sky as an angular separation — remains fixed. In this work, we adopt a constant neighbor distance of 1.0 deg, in order to include the largest possible number of points in the calculation of the projected inclination of the filament segment. even near the segment ends where fewer neighboring points are available. Note that, given the observational noise $\Sigma_{\alpha,r}$, points closer to the origin matter less than those farther away, so it is important to adopt a neighbor distance that accounts for the overall segment inclinations. After that, we compute the marginal posterior over the angle parameter by integrating out r, conditioned on the observation \mathbf{x} .

Finally, the Hough accumulator is obtained by summing all the marginalized probabilities to obtain the set of inclination angles $\mathcal{A} = \{\alpha_1^{max}, \alpha_2^{max}, ..., \alpha_N^{max}\} \in [0 \text{ deg}, 180 \text{ deg}]$ of the line to which the greatest number of points belongs, i.e., the inclination angles where there is the greatest number of aligned points in all the N segment points. Further details on the PHT method can be found in Tino et al. (2011).

The overall projected inclination angle ϕ_{fil} of a filament connected to a cluster is computed considering the vector average, which is determined from the set of complex components $X = \{\cos(2\alpha_i^{max}) \mid i = 1, 2, ..., N\}$ and $Y = \{\sin(2\alpha_i^{max}) \mid i = 1, 2, ..., N\}$. Thus, ϕ_{fil} comes from the following equation:

$$\phi_{fil} = \frac{\arctan(\overline{Y}, \overline{X})}{2},\tag{2}$$

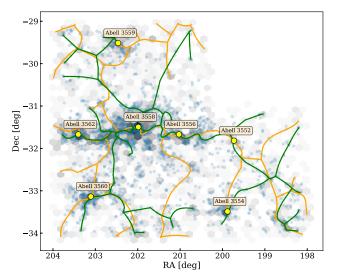
where \overline{X} and \overline{Y} are the mean values of X and Y, respectively.

Fig. 4 illustrates how filaments connected to X-ray clusters are defined, as well as how their projected inclinations are computed using the PHT technique. Note that the spacing between the segment points is not uniform, so in some cases, defining segments connected to X-ray clusters based on a projected distance criterion between 0.8 and 1.2 r_{200} resulted in only one point per segment, making it impossible to determine a projected filament inclination. In those cases, the nearest adjacent point was also included in addition to the one within 0.8 to 1.2 r_{200} , in order to be able to define the projected inclination of the segment.

4.3. Shapes of clusters inferred from X-ray emission

Cluster shapes were characterized with the shape of the X-ray emission, which, for simplicity, was assumed to be ellipsoidal. Major and minor axes and the positional angle estimated by Source Extractor are intended to describe the detected object as an elliptical shape. a and b are the lengths of the semi-major and semi-minor axes, respectively. More precisely, they represent the maximum and minimum spatial dispersion of the object profile along any direction. ϕ_x is the position-angle of the a axis relative to the first image axis, which in eRASS1 mosaics is RA with negative delta. It is counted positive in the direction of the second axis (which is Dec). By definition, ϕ_x is the position angle

⁸ For this work, we assumed $\Sigma_{\alpha,r} = \begin{bmatrix} \sigma_{\alpha}^2 & 0 \\ 0 & \sigma_r^2 \end{bmatrix}$, with $\sigma_r = 0.35$ deg and $\sigma_{\alpha} = 20.5$ deg



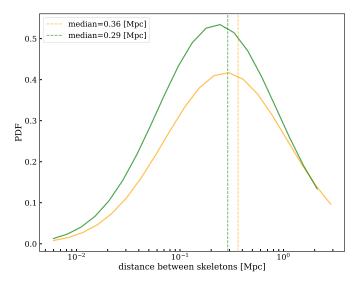


Fig. 3. *Left:* Two-dimensional reconstruction of the filament network using the spectroscopic sample (green segments) and photometric members (red segments) in the SSC core. Grey map indicates the density of photometric members in the area, while blue circles are the spectral members. Orange circles indicate known X-ray clusters in the SSC (Haines et al. 2018). *Right:* Probability distribution of the distances between skeletons of filament networks from photometric to spectroscopic (orange curve) and spectroscopic to photometric (green curve) members within the ShaSS area. Orange and green vertical dashed lines show the median distance between skeletons obtained from the two comparisons.

for which the major axis is maximized ⁹. Only wavelet images with unresolved spatial scales removed were used in our analysis. We provide the X-ray cluster characterization on both 2–4 and 8–16 arcminute scales and use the barycenter of X-ray emission defined by the corresponding scales.

5. Results

We have identified the LSS in both superclusters that are part of CHANCES, considering as tracers of the cosmic filaments the two-dimensional distribution of photometric members based on the target selection strategy described in Sect. 3.1. Additionally, we have constructed a catalog of clusters detected on X-ray by eROSITA, comprising a total of 58 X-ray clusters, in a z range of $0.027 \le z \le 0.073$ for the SSC, and $0.037 \le z \le 0.083$ for the HRSC, with estimated optical richnesses λ^{10} ranging between $5 < \lambda < 90$. Of the total number of X-ray clusters, 19 are part of SSC, while the remaining 43 belong to HRSC. We have also created a catalog of filaments connected to these clusters. We determined and compared the inclinations of the clusters based on X-ray emission and their connected main filaments. In this section, we report the main results obtained from these analyses.

5.1. X-ray clusters in the identified LSS

Since galaxy clusters are interconnected by cosmic filaments, it is natural to expect X-ray emission from clusters associated with nearby filaments. To compare the projected distribution of our detected filaments and X-ray clusters, as well as quantify their similarities (or discrepancies), we performed a cross-match between the X-ray clusters and the detected filaments, assuming the r_{200} of each X-ray cluster as the threshold distance (projected on the sky) for the match. From this exercise, we found that 15 (80%) X-ray sources in the SSC are connected to at least one filament, while 48 (78%) satisfy this condition in the HRSC.

Based on the idea that clusters are located at filament intersections, we have considered both maxima and bifurcation points from DisPerSE as nodes. Under this assumption, we find that 63% of the clusters detected in X-rays within the SSC are also detected in the optical (as node or bifurcation points detected by DisPerSE), while for HRSC this percentage raises to 67%. Of course, these fractions depend on the richness threshold adopted for X-ray clusters, the tolerance of positions in the sky, as well as the persistence level assumed for the structures detected on the projected distribution of photometric members.

Taking the above into account, if both superclusters are considered, we find that 82% of the X-ray clusters are connected to filaments. Additionally, 66% of the clusters were successfully detected based on the distribution of photometric members in the optical, a percentage similar to that obtained when considering only X-ray clusters connected to filaments.

5.2. Typical cluster spacing in superclusters and field

In addition to comparing the filaments and nodes from the optical with the clusters in X-rays, we computed the typical projected separation between closest clusters in SSC and HRSC, in order to determine whether there is a significant difference compared to the average minimum separation of isolated clusters. As this value depends on the richness λ threshold of the considered clusters, for this exercise, we just considered X-ray clusters with $\lambda > 10$.

We obtained that the median minimum separation among X-ray clusters in the SSC is ~ 4 Mpc, while in the HRSC this separation is ~ 4.6 Mpc. We note that these values correspond to lower limits, as we are considering only the projected positions of clusters on the sky, rather than the three-dimensional distribution of clusters within the superclusters. For the same reason, the smaller value for the SSC may be due to the inclination of the line-of-sight axis with respect to us. As a control sample, we used the eRASS1 catalog of optical identifications of eRASS1 sources that are galaxy clusters from Kluge et al. (2024) to estimate the average cluster separation. We considered the clusters in the redshift range 0.08 < z < 0.15, similar as the

⁹ https://sextractor.readthedocs.io/en/latest/Position.html

¹⁰ The richness λ is defined as the membership probabilities multiplied by the scaling factor *S* (see Kluge et al. 2024, for details).

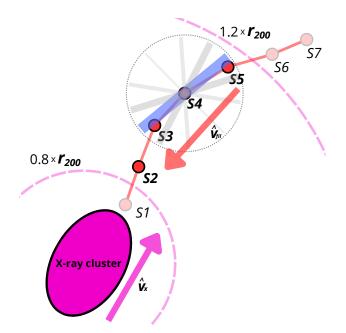


Fig. 4. Schematic representation of the definition of filament segments connected to the X-ray cluster and the computation of their projected inclinations using the PHT technique. Red circles indicate the segment points [S1, S2, ..., S7] that are part of the detected filament network. Dashed magenta lines represent 0.8 and 1.2 times the r_{200} around the X-ray peak, respectively. Dark red segment points [S2, S3, S4, S5], located between the dashed curves, are used to compute the mean projected inclination of the filament segment connected to the galaxy cluster (magenta ellipse). The PHT operator is centered at the position of S4, with each line representing a possible local alignment angle of the segment points, based on the positions of the points within the dashed circumference. Line thickness corresponds to the probability of alignment at that specific angle, with the thickest blue line denoting the most probable inclination angle at S4. The same procedure is applied at S2, S 3 and S 5 to ultimately compute the mean projected alignment angle using Eq. 2, represented as the red vector \hat{v}_{fill} . The inclination angle of the X-ray cluster is represented as the magenta vector \hat{v}_x .

redshift range considered for the SSC and HRSC, with $\lambda > 10$. We used the clusters located in the deepest part of eRASS1 area 45 deg <RA< 90 deg, -60 deg <Dec< -25 deg to compute the distances to the nearest clusters in the full catalog with a redshift difference below 0.02. The median projected separation of the clusters was 8.3 Mpc. The value obtained for isolated clusters is ~ 1.8 times higher than the mean minimum separation of clusters in SSC, and ~ 2 times the value obtained for HRSC. These results can be considered as lower limits that can be improved once CHANCES spectroscopy is available.

5.3. Alignment between optical filaments and X-ray clusters

For the X-ray clusters connected to filaments, we further investigated the morphology of the X-ray emission in relation to the underlying distribution of galaxies observed in the optical. To this end, we compared the inclination angle of the major axis of the X-ray emission with the projected orientation of the connected segment of the optical filaments.

To quantify the alignment between the X-ray morphology of the clusters and their associated filaments, we defined a normalized vector \hat{v}_x that points in the direction of the inclination angle ϕ_x of the major axis of the X-ray cluster, and the normalized vector \hat{v}_{fil} , which points in the direction of the projected inclination angle ϕ_{fil} of the filament connected to the corresponding X-ray

cluster. Following the definition used in Altay et al. (2006), the measure of alignment between an X-ray cluster and a connected filament is

$$|\cos(\phi_{x,fil})| = |\hat{v}_x \cdot \hat{v}_{fil}|,\tag{3}$$

where $\phi_{x,fil}$ is the angle between \hat{v}_x and \hat{v}_{fil} .

A $|\cos(\phi_{x,fil})|$ value close to 1 implies a good filament-cluster alignment ($\phi_{x,fil} = 0$ deg), while a value close to 0 implies the contrary ($\phi_{x,fil} = 90$ deg). We have found a strong trend that filaments connected to X-ray clusters preferentially align with the major axis of this cluster, as shown in the alignment distribution of Fig. 5, where at a distance of $1r_{200}$ (0.8 r_{200} -1.2 r_{200} ; dark blue line) ~ 40% of the connected filaments have a $|\cos(\phi_{x,fil})|$ ~ 1. If we increase the $|\cos(\phi_{x,fil})|$ range to 0.8 this percentage reaches \sim 55%. The remaining possible values follow an almost uniform distribution, with no evidence of another preferred direction. Note that we have calculated the distribution using four equally sized bins, each spanning an angular difference of 20.5 deg, based on the angular covariance value σ_{α} used to determine the projected inclination angle of the detected filaments. In this way, our comparison is performed within the minimum angular resolution achievable.

In order to quantify the detected alignment signal between clusters and filaments, we have compared the observed distribution with a uniform distribution of $|\cos(\phi_{x,fil})|$ (gray-dashed horizontal line in Fig. 5). The comparison was performed using the Chi-squared test with a 95% significance level. We found that at a distance of $1r_{200}$, the observed distribution yields a χ^2 statistic of approximately 10.9, with a p-value of 0.012, indicating that the detected signal significantly deviates from a uniform distribution. As the distance from the cluster center increases, the distribution becomes increasingly similar to a uniform distribution (χ^2 statistic of 0.8 and p-value of 0.85 at $1.6r_{200}$, and χ^2 statistic of 0.9 and p-value of 0.81 at $3.2r_{200}$, see Fig. 5).

6. Discussion and Conclusions

Mass accretion rates in galaxy clusters play a crucial role in galaxy evolution, including pre-processing effects (e.g. Sampaio et al. 2021). A preferential accretion direction leads to an alignment between filaments and cluster shapes. Here, we present the first observational test of this correlation, showing that the alignment between filament elongation and cluster morphology provides a simplified statistical approach to studying the complex process of galaxy accretion.

Our results confirm a significant alignment between filaments and the major axes of galaxy clusters, comparable with findings from simulations. For instance, Kuchner et al. (2020) found that filaments tend to align with the major axis of the clusters in the inner region, a result that agrees with previous theoretical studies (Hahn et al. 2007; Youcai et al. 2009; Ganeshaiah Veena et al. 2018) and is further supported by the high fraction of alignment revealed in our analysis at $1r_{200}$ from the cluster center. Regardless of the latter, our analysis focuses on clusters within superclusters, using X-ray emission to trace their gravitational potential and photometric members to identify filaments, while simulations typically study isolated clusters in three dimensions based on dark matter and gas particle distribution. To enable a more direct comparison between our findings and simulations, studies employing X-ray mocks of superclusters are still required. We will conduct a similar analysis based on supercluster simulations, where X-ray mocks are being produced.

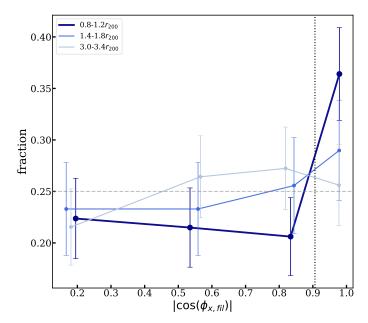


Fig. 5. Distribution of the alignment between optical filaments connected to galaxy clusters and the major axis of each cluster as inferred from its X-ray emission. Fractions and 68% confidence intervals were computed in equal-sized angular bins, following the method described in Damsted et al. (2023). Different colors indicate different projected cluster–filament distances used to compute the projected filament inclination. The gray-dashed horizontal line represents the uniform distribution, while the black-dotted vertical line indicates an alignment threshold of less than 25 degrees.

Despite clusters in the SSC and HRSC being closer to each other than clusters in the field, the influence of the supercluster environment does not appear to significantly affect the cluster-filament alignment. We note the use of the X-ray emission as a tracer of the cluster shape and the lack of access to the three-dimensional distribution of clusters and filaments. A control sample of isolated clusters is needed to understand how this correlation behaves in less dense environments. To address this, we will further test it by extending our analysis to the full CHANCES low-z cluster sample in future work. The spectroscopic follow-up by CHANCES will also provide improved mass accretion rate estimates, allowing for a more comprehensive analysis of the impact of cluster growth on galaxy evolution.

While our current data relies heavily on photometric redshifts to reconstruct the filament network in two dimensions, this does not reduce the reliability of the alignment statistics, as alignments with two-dimensional X-ray maps only work in the observer plane anyway, and it is anticipated that only the strongest filaments would dominate the alignment. With a more complete study, offered by the spectroscopy, we can fold in the connectivity to the picture.

Photometric redshifts have proven to be effective in tracing the most prominent components of the large-scale structure, as validated by comparisons with available spectroscopic data. The observed alignment of filaments detected in optical data with the X-ray elongation of clusters supports the idea that most of the mass accretion onto clusters occurs through these filaments.

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Appendix A: X-ray cluster properties

Tables A.1 and A.2 list the main properties of the galaxy clusters detected by eROSITA in the 0.6–2.3 keV band and used in this work.

Table A.1. Properties of the 19 X-ray clusters in the SSC.

(1) RA (J2000) (deg)	(2) Dec (J2000) (deg)	(3) z	(4) r ₂₀₀ (Mpc)	(5) M_{200} $(10^{14} \mathrm{M}_{\odot})$	(6) L_x $(10^{44} \text{ erg s}^{-1})$	(7) a (arcmin)	(8) b (arcmin)	$ \begin{array}{c} (9) \\ \phi_x \\ (\text{deg}) \end{array} $
200.866	-31.722	0.048	1.154	1.685	0.288	23.077	13.485	99.297
194.167	-30.357	0.055	1.638	4.904	1.542	23.071	10.082	90.257
202.038	-31.482	0.048	1.895	7.530	2.987	20.378	10.598	114.657
194.537	-28.514	0.066	1.053	1.301	0.196	19.932	9.228	110.027
193.639	-29.149	0.054	1.722	5.468	1.824	19.823	11.397	162.367
193.102	-31.267	0.054	1.529	3.899	1.076	15.827	9.373	98.757
203.439	-31.667	0.049	1.600	4.342	1.264	15.789	12.028	87.947
195.959	-31.410	0.055	0.895	0.770	0.085	15.678	10.128	42.037
196.513	-34.399	0.063	1.042	1.251	0.184	14.735	10.393	43.477
203.108	-33.074	0.049	1.400	3.003	0.711	12.645	11.380	170.867
194.259	-31.345	0.056	1.106	1.459	0.232	12.240	7.531	57.987
199.884	-33.480	0.046	1.066	1.298	0.191	11.428	7.626	59.357
202.439	-29.538	0.049	0.946	0.943	0.116	10.168	6.812	48.587
203.655	-35.271	0.052	0.796	0.541	0.049	9.386	6.156	47.727
202.022	-34.065	0.049	0.937	0.907	0.110	8.209	7.028	3.427
202.374	-28.311	0.034	0.639	0.279	0.017	12.788	9.123	92.087
198.556	-33.824	0.050	0.909	0.820	0.094	8.507	6.139	166.757
200.405	-35.823	0.050	0.866	0.706	0.074	8.491	7.671	63.977
201.756	-27.168	0.036	1.375	2.794	0.625	18.500	14.155	29.658

Notes. Columns are: (1) and (2): right ascension and declination of the cluster center, defined by the X-ray peak from the eROSITA detections (purple circles in Fig. 1); (3): redshift of the cluster; (4) and (5): radius and corresponding mass enclosing a mean density of 200 times the critical mass density of the Universe at the cluster redshift; (6): X-ray luminosity of the cluster; (7) and (8): major and minor axes of the ellipse fitted to the X-ray emission of the cluster; (9): inclination angle of the major axis (see Sect. 4.3).

Table A.2. Same as Table A.1 but for the clusters identified in the HRSC.

(1) RA (J2000) (deg)	(2) Dec (J2000) (deg)	(3) z	(4) r_{200} (Mpc)	$M_{200} \ (10^{14} \mathrm{M}_{\odot})$	(6) L_x $(10^{44} \text{ erg s}^{-1})$	(7) a (arcmin)	(8) b (arcmin)	$ \begin{array}{c} (9) \\ \phi_x \\ (\text{deg}) \end{array} $
	52.25 0	0.042	0.064	0.600	0.070	22.107	6.026	20.044
65.623	-53.279	0.043	0.864	0.698	0.072	22.197	6.926	39.044
53.629	-53.618	0.065	1.014	1.155	0.163	18.062	11.314	124.794
52.402	-45.997	0.069	1.327	2.596	0.580	17.659	9.299	83.586
59.071	-53.856	0.038	0.745	0.446	0.036	17.606	7.950	101.114
50.653	-53.184	0.077	1.282	2.360	0.505	17.431	7.174	75.184
50.415	-45.483	0.072	1.247	2.162	0.437	17.117	9.452	129.886
56.394	-41.214	0.060	1.337	2.634	0.588	16.653	9.010	93.116
49.744	-53.906	0.054	0.942	0.915	0.112	16.604	7.522	20.254
48.699	-58.057	0.064	0.968	1.001	0.130	16.311	9.410	100.613
56.459	-56.976	0.059	1.252	2.159	0.430	15.960	11.344	169.563
47.675	-47.354	0.082	1.171	1.809	0.336	15.475	6.498	141.945
55.133	-55.079	0.044	1.027	1.173	0.163	14.379	11.010	17.844
58.065	-54.861	0.046	1.066	1.314	0.195	13.985	9.499	73.544
52.605	-52.547	0.060	1.466	3.464	0.900	13.969	11.746	8.205
55.662	-53.628	0.059	1.840	6.851	2.611	13.816	10.886	85.154
55.385	-41.024	0.062	0.856	0.692	0.073	13.439	6.583	92.726
51.180	-58.624	0.077	0.924	0.884	0.109	12.946	5.639	44.862
62.348	-59.587	0.058	0.952	0.948	0.119	12.880	6.695	84.332
49.484	-45.756	0.077	1.228	2.074	0.412	12.617	8.572	153.116
57.082	-45.508	0.070	1.080	1.402	0.222	12.507	7.169	38.246
48.272	-47.400	0.082	0.980	1.060	0.146	12.381	7.818	75.335
53.490	-39.061	0.063	1.006	1.123	0.155	11.765	9.191	158.716
53.935	-45.124	0.069	0.942	0.927	0.116	10.938	7.263	174.526
48.595	-45.395	0.077	1.571	4.344	1.310	10.925	9.996	72.356
60.167	-53.680	0.072	0.942	0.931	0.117	10.913	7.392	74.114
55.148	-45.705	0.070	1.194	1.893	0.355	10.627	7.472	88.186
65.029	-51.430	0.070	1.100	1.479	0.241	10.478	6.078	31.255
50.583	-41.338	0.063	1.366	2.814	0.653	10.305	10.152	119.746
48.406	-38.305	0.081	1.208	1.983	0.386	10.011	7.417	130.096
50.642	-49.254	0.070	0.887	0.777	0.088	9.819	4.657	76.715
50.521	-51.322	0.070	1.122	1.569	0.265	9.713	6.749	146.965
65.700	-51.512	0.043	1.086	1.385	0.210	9.301	7.254	157.285
53.931	-38.689	0.062	0.865	0.715	0.077	9.059	5.949	107.506
49.095	-50.957	0.074	0.934	0.909	0.113	8.988	7.618	72.395
58.482	-38.555	0.079	0.946	0.948	0.122	8.939	6.166	115.646
59.766	-59.597	0.062	0.806	0.577	0.055	8.723	6.508	113.682
52.036	-57.725	0.067	0.986	1.062	0.143	8.604	7.479	114.043
51.313	-56.591	0.060	1.953	8.204	3.467	8.489	6.541	124.393
55.136	-57.040	0.057	0.848	0.670	0.069	7.817	5.086	137.213
50.264	-56.213	0.083	1.040	1.266	0.192	7.596	5.600	102.503
53.720	-39.484	0.073	0.874	0.745	0.083	7.389	5.648	75.866
55.700	-46.298	0.070	1.052	1.296	0.196	7.329	6.339	40.266
56.812	-54.074	0.070	0.726	0.426	0.034	7.027	5.241	159.274
'								

Notes. Columns are as in Table A.1.