

# Benchmark Programs

Below we show all the experimental results and benchmark programs from the paper. Programs in Section 2 correspond to these in Table 2 (programs with expected affine-sensitivity), while programs in Section 3 correspond to those in Table 3 (programs with expected linear-sensitivity). See the full version of the paper (with appendix) at <https://arxiv.org/abs/1902.04744>.

## 1 BENCHMARKS

Table 2. Experimental Results for Expected Affine-sensitivity (with  $\epsilon = 1$ ,  $L = 1$ )

Example	Time/sec	$\eta(\mathbf{b})$	$K$	$d$	$M$
mini-Roulette	5.97	$13 \cdot x - 13$	-13	11	13
rdwalk	3.91	$-5 \cdot x + 5000$	-5	1	5
prdwalk variant	4.88	$-0.2857 \cdot x + 285.7$	-1.429	5	0.2857
prspeed	4.31	$-1.7143 \cdot x + 1714.3$	-5.143	3	1.7143
race variant	5.43	$-1.43 \cdot h + 1.43 \cdot t$	-4.29	4	2.86
ad. rdwalk 2D	4.55	$-0.77 \cdot x + 0.77 \cdot y$	-2.31	3	1.54
ad. rdwalk 1D Variant	4.49	$2.86 \cdot x$	-2.86	2	2.86
American Roulette	7.66	$20.27 \cdot x - 20.27$	-20.27	35	20.27

Table 3. Experimental Results for Expected Linear-sensitivity (with  $\epsilon = 1$ ,  $L = 1$ )

Example	Time/sec	$\eta(\mathbf{b})$	$K$	$d$	$M$	$c$
mini-roulette variant	12.69	$2.45 \cdot x - 2.45$	-4.91	9	2.45	22.08
single-room heating	5.21	$-0.833 \cdot x + 16.67$	-1.25	2.1	0.833	1.75
double-room heating	5.64	$-2.27 \cdot x_1 + 45.45$	-3.41	2.87	2.27	6.518
rdwalk variant	4.44	$-2.5 \cdot x + 2500$	-7.5	3	2.5	7.5
prdwalk	4.46	$-0.5714 \cdot x + 571.4$	-2.86	5	0.5714	2.86
prspeed variant	5.00	$-0.5333 \cdot x + 533.3$	-2.67	5	0.5333	2.67
race	5.17	$-2 \cdot h + 2 \cdot t$	-6	4	4	6
simple while loop	3.59	$-2 \cdot x + 2000$	-2	1	2	2
pollutant disposal	4.87	$n - 5$	-3	3	1	3
ad. rdwalk 2D variant	6.07	$-0.606 \cdot x + 0.606 \cdot y$	-2.424	4	1.212	2.424
ad. rdwalk 1D	5.16	$1.11 \cdot x$	-2.22	2	1.11	2.22
American roulette variant	14.95	$2.08 \cdot x - 2.08$	-4.15	35	2.08	72.63

## 2 BENCHMARK PROGRAMS FOR EXPECTED AFFINE-SENSITIVITY

```

while  $x \geq 1$  do
  if  $\text{prob}(\frac{6}{65})$  then
     $x := x + 1; w := w + 2$ 
  else if  $\text{prob}(\frac{4}{59})$  then
     $x := x + 2; w := w + 3$ 
  else if  $\text{prob}(\frac{3}{55})$  then
     $x := x + 3; w := w + 4$ 
  else if  $\text{prob}(\frac{2}{52})$  then
     $x := x + 5; w := w + 5$ 
  else if  $\text{prob}(\frac{1}{50})$  then
     $x := x + 11; w := w + 6$ 
  else  $x := x - 1$ 
fi fi fi fi fi od

```

Fig. 1. A Mini-roulette example

```

while  $x \leq 1000$  do
  if  $\text{prob}(0.6)$  then
     $x := x + 1$ 
  else
     $x := x - 1$ 
  fi
od

```

Fig. 2. rdwalk

```

while  $x \leq 1000$  do
  if  $\text{prob}(0.5)$  then
     $x := x + 2$ 
  else
     $x := x + 5$ 
  fi
od

```

Fig. 3. A Variant of prdwalk

```

while  $x \leq 1000$  do
  if  $\text{prob}(0.75)$  then
     $x := x + 0$ 
  else
    if  $\text{prob}(2/3)$  then
       $x := x + 2$ 
    else
       $x := x + 3$ 
    fi
  fi
od

```

Fig. 4. prspeed

```

while  $h \leq t$  do
   $t := t + 1$ ;
  if prob(0.5) then
     $h := h + 1$ 
  else
    if prob(0.6)
       $h := h + 4$ 
    else
      skip
    fi
  fi
od

```

Fig. 5. A Variant of race

```

while  $x \leq y$  do
  if prob(0.5) then
    if prob(0.7) then
       $x := x + 3$ 
    else
       $y := y + 2$ 
    fi
  else
    if prob(0.7) then
       $x := x + 2$ 
    else
       $y := y + 1$ 
    fi
  fi
od

```

Fig. 6. Adversarial random walk in two dimensions

```

while  $x \geq 0$  do
   $x := x + 1$ ;
  if prob(0.5) then
    if prob(0.9) then
       $x := x - 2$ 
    else
       $x := x + 1$ 
    fi
  else
     $x := x - 1$ 
  fi
od

```

Fig. 7. A Variant of Adversarial random walk in one dimension

```

while  $x \geq 1$  do
  if prob(1/304) then
     $x := x + 35$ ;  $w := w + 35$ 
  else if prob(2/303) then
     $x := x + 17$ ;  $w := w + 17$ 
  else if prob(3/301) then
     $x := x + 11$ ;  $w := w + 11$ 
  else if prob(2/149) then
     $x := x + 8$ ;  $w := w + 8$ 
  else if prob(5/294) then
     $x := x + 6$ ;  $w := w + 6$ 
  else if prob(6/289) then
     $x := x + 5$ ;  $w := w + 5$ 
  else if prob(12/283) then
     $x := x + 2$ ;  $w := w + 2$ 
  else if prob(2/271) then
     $x := x - 0.5$ 
  else if prob(18/269) then
     $x := x + 1$ ;  $w := w + 1$ 
  else if prob(2/251) then
     $x := x - 0.5$ 
  else
     $x := x - 1$ 
  fi fi fi fi fi fi fi fi fi fi
od

```

Fig. 8. American Roulette

### 3 BENCHMARK PROGRAMS FOR EXPECTED LINEAR-SENSITIVITY

```

 $r_1 \sim \text{unif}(1, 2), r_2 \sim \text{unif}(2, 3),$ 
 $r_3 \sim \text{unif}(3, 4), r_4 \sim \text{unif}(4, 5),$ 
 $r_5 \sim \text{unif}(8, 9), r_6 \sim \text{unif}(1, 2);$ 
while  $x \geq 1$  do
  if  $\text{prob}(\frac{6}{65})$  then
     $x := x + r_1; w := w + 2$ 
  else if  $\text{prob}(\frac{4}{59})$  then
     $x := x + r_2; w := w + 3$ 
  else if  $\text{prob}(\frac{3}{55})$  then
     $x := x + r_3; w := w + 4$ 
  else if  $\text{prob}(\frac{2}{52})$  then
     $x := x + r_4; w := w + 5$ 
  else if  $\text{prob}(\frac{1}{50})$  then
     $x := x + r_5; w := w + 6$ 
  else  $x := x - r_6$ 
fi fi fi fi fi od

```

Fig. 9. A variant of Mini-roulette example

```

 $w_1 \sim \text{unif}(-0.3, 0.3), w_2 \sim \text{unif}(-0.2, 0.2);$ 
while  $0 \leq x_1 \leq 20 \wedge 0 \leq x_2 \leq 20$  do
   $\begin{pmatrix} x_1 \\ x_2 \end{pmatrix} := \begin{pmatrix} x_1 + 0.03 * (10 - x_1) + 0.04 * (x_2 - x_1) + 1.5 + w_1 \\ x_2 + 0.02 * (10 - x_2) + 0.04 * (x_1 - x_2) + w_2 \end{pmatrix};$ 
   $n := n + 1$ 
od

```

Fig. 11. Double-Room Heating

```

 $w \sim \text{unif}(-0.3, 0.3);$ 
while  $0 \leq x \leq 20$  do
   $x := x + 0.03 * (10 - x) + 1.5 + w;$ 
   $n := n + 1$ 
od

```

Fig. 10. Single-Room Heating

```

 $r \sim \text{unif}(1, 3);$ 
while  $x \leq 1000$  do
  if  $\text{prob}(0.6)$  then
     $x := x + r$ 
  else
     $x := x - r$ 
  fi
od

```

Fig. 12. A variant of rdwalk

```

 $r_1 \sim \text{unif}(0, 2), r_2 \sim \text{unif}(0, 5);$ 
while  $x \leq 1000$  do
  if prob(0.5) then
     $x := x + r_1$ 
  else
     $x := x + r_2$ 
  fi
od

```

Fig. 13. prdwalk

```

 $r \sim \text{unif}(2, 4);$ 
while  $h \leq t$  do
   $t := t + 1;$ 
  if prob(0.5) then
     $h := h + r$ 
  else
    skip
  fi
od

```

Fig. 15. race

```

 $r_1 \sim \text{unif}(1, 2), r_2 \sim \text{unif}(2, 3),$ 
 $r_3 \sim \text{unif}(3, 5);$ 
while  $x \leq 1000$  do
  if prob(0.75) then
     $x := x + r_1$ 
  else
    if prob(2/3) then
       $x := x + r_2$ 
    else
       $x := x + r_3$ 
    fi
  fi
od

```

Fig. 14. A Variant of prspeed

```

 $r \sim \text{unif}(0, 1);$ 
while  $x \leq 1000$  do
   $x := x + r$ 
od

```

Fig. 16. A Simple Probabilistic While Loop

```

 $r \sim \text{unif}(0, 1);$ 
while  $x \leq 1000$  do
   $x := x + r$ 
od

```

Fig. 17. A Simple Probabilistic While Loop

```

 $r_1, r_2 \sim \text{unif}(2, 4), r'_1, r'_2 \sim \text{unif}(1, 2);$ 
while  $x \leq y$  do
  if prob(0.5) then
    if prob(0.7) then
       $x := x + r_1$ 
    else
       $y := y + r'_1$ 
    fi
  else
    if prob(0.7) then
       $x := x + r_2$ 
    else
       $y := y + r'_2$ 
    fi
  fi
od

```

Fig. 18. A Variant of adversarial random walk in two dimensions

```

     $r \sim \text{unif}(-1, 1);$ 
while  $x \geq 0$  do
     $x := x + r;$ 
    if prob(0.5) then
        if prob(0.9) then
             $x := x - 1$ 
        else
             $x := x + 1$ 
        fi
    else
         $x := x - 1$ 
    fi
od

```

Fig. 19. Adversarial random walk in one dimension

```

 $r_1 \sim \text{unif}(30, 35), r_2 \sim \text{unif}(12, 17),$ 
 $r_3 \sim \text{unif}(9, 11), r_4 \sim \text{unif}(7, 8),$ 
 $r_5 \sim \text{unif}(5, 6), r_6 \sim \text{unif}(3, 5)$ 
 $r_7 \sim \text{unif}(2, 3), r'_7 \sim \text{unif}(0.5, 1),$ 
 $r_8 \sim \text{unif}(1, 2), r'_8 \sim \text{unif}(0.5, 1),$ 
 $r_9 \sim \text{unif}(1, 2);$ 
while  $x \geq 1$  do
    if prob(1/304) then
         $x := x + r_1; w := w + 35$ 
    else if prob(2/303) then
         $x := x + r_2; w := w + 17$ 
    else if prob(3/301) then
         $x := x + r_3; w := w + 11$ 
    else if prob(2/149) then
         $x := x + r_4; w := w + 8$ 
    else if prob(5/294) then
         $x := x + r_5; w := w + 6$ 
    else if prob(6/289) then
         $x := x + r_6; w := w + 5$ 
    else if prob(12/283) then
         $x := x + r_7; w := w + 2$ 
    else if prob(2/271) then
         $x := x - r'_7$ 
    else if prob(18/269) then
         $x := x + r_8; w := w + 1$ 
    else if prob(2/251) then
         $x := x - r'_8$ 
    else
         $x := x - r_9$ 
    fi fi fi fi fi fi fi fi fi fi
od

```

Fig. 20. A Variant of American Roulette