

# Chapter 1

## Session 1

### 1.1 Matrix notes

**Multiplying Matrices:** Number of columns in the first matrix must equal the number of rows in the second matrix

$$n \times m * m \times z = n \times z$$
$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \times \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 1*a + 2*c & 1*b + 2*d \\ 3*a + 4*c & 3*b + 4*d \end{bmatrix}$$

# Chapter 2

## test

### 2.1 Linear Regression with One Variable/Univariate Linear Regression

Link: Model Representation

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

To break it apart, it is  $\frac{1}{2}\bar{x}$  where  $\bar{x}$  is the mean of the squares of  $h_{\theta}(x^{(i)}) - y^{(i)}$ , or the difference between the predicted value and the actual value.

This function is otherwise called the "Squared error function", or "Mean squared error". The mean is halved ( $\frac{1}{2}$ ) as a convenience for the computation of the gradient descent, as the derivative term of the square function will cancel out the  $\frac{1}{2}$  term.

### 2.2 Model and Cost Function

Link: Model and Cost Function

We can measure the accuracy of our hypothesis function by using a cost function. This takes an average difference (actually a fancier version of an average) of all the results of the hypothesis with inputs from x's and the actual output y's.

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

### 2.3 Batch Gradient Descent for Linear Regression One Variable

Link: Gradient Descent for Linear Regression

When **specifically applied to the case of linear regression**, a new form of the gradient descent equation can be derived. We can substitute our actual cost function and our actual hypothesis function and modify the equation to:

*Repeat until convergence :*

$$\begin{aligned}\theta_0 &:= \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})x_0^{(i)} \\ \theta_1 &:= \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})x_1^{(i)}\end{aligned}$$

where  $m$  is the size of the training set,  $\theta_0$  a constant that will be changing **simultaneously** with  $\theta_1$  and  $x_i$ ,  $y_i$  are values of the given training set (data).  $h_{\theta}$  is the hypothesis, in this case

Univariate Linear Regression - section 2.1. It is possible to omit  $x_0^{(i)}$  as it is 1 in case of univariate linear regression. Note also that

$$\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_0^{(i)} = \frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1)$$

$$\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_1^{(i)} = \frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1)$$

Where  $J(\theta_0, \theta_1)$  is the Model and Cost Function in section 2.2.

### Generalised algorithm

*Repeat until convergence :*

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

(for  $j = 1$  and  $j = 0$ )

## 2.4 Unclassified

**Supervised Learning** <https://www.coursera.org/learn/machine-learning/lecture/1VkBb/supervised-learning>.

We give the algorithm data sets with right answers (Training set). Algorithm must produce more right answers.

Training set -  $\mathcal{L}$  Learning Algorithm -  $\mathcal{L}$  outputs function  $h$  (hypothesis). Job of hypothesis is get the size of house as input and output estimated value.  $h$  maps from  $x$ 's to  $y$ 's

**Regression** House price prediction is regression problem - predict continuous valued output (price).

**Classification** Classification: Predict a discrete valued output (0 or 1). It can be more than two values.

Also contains a different way of plotting classification problems - different symbols on one axis instead of two axes.

**Unsupervised Learning** <https://www.coursera.org/learn/machine-learning/lecture/olRZo/unsupervised-learning>

Given data with the same label. "Here is a data set, find some structure in it".

**Clustering algorithm** E.g. breast cancer thing. Or google news e.g. clusters news related to specific news story. Genes issue - cluster people.

**Examples** : Organise computing clusters, social network analysis, Market segmentation, Astronomical data analysis. Cocktail party problem: Overlapping voices

### 2.4.1 Model Representation

**Training set:** Data set with right answers

### 2.4.2 Notation

$m$	Number of training examples
$x's$	“input” variable / features
$y's$	“output” variable / “target” variable
$(x, y)$	one training example
$(x^{(i)}, y^{(i)})$	$i^{\text{th}}$ training example
$h(\text{hypothesis})$	maps from $x's$ to $y's$
Linear Regression with one variable or Univariate linear regression	$h_{\theta}(x) = \theta_0 + \theta_1 x$
$\theta_0, \theta_1$	Model Parameters
Linear Regression Cost Function	
Linear Regression Minimize Square Difference Minimise over $\theta_0 \theta_1$	$\frac{1}{2m} \sum_{i=1}^m ((h_{\theta}(x^{(i)})) - y^{(i)})^2$
Cost function (Squared error cost function) Minimise cost function over $\theta_0 \theta_1$	$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m ((h_{\theta}(x^{(i)})) - y^{(i)})^2$
Batch Gradient Descent	For minimising. It goes to a local minimum. Batch because it looks at the entire training set.
$\alpha$	Learning rate (Always positive)
Linear Regression	It is always a Convex function (Bowl-shaped)

Table 2.1: Symbols