# **Softmax exercise**

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the <u>assignments page</u> (<a href="http://vision.stanford.edu/teaching/cs231n/assignments.html">http://vision.stanford.edu/teaching/cs231n/assignments.html</a>) on the course website.

This exercise is analogous to the SVM exercise. You will:

- implement a fully-vectorized **loss function** for the Softmax classifier
- implement the fully-vectorized expression for its analytic gradient
- · check your implementation with numerical gradient
- use a validation set to tune the learning rate and regularization strength
- · optimize the loss function with SGD
- · visualize the final learned weights

## In [ ]:

```
import random
import numpy as np
from cs231n.data_utils import load_CIFAR10
import matplotlib.pyplot as plt

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading extenrnal modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipytho
n
%load_ext autoreload
%autoreload 2
```

```
In [ ]:
```

```
def get CIFAR10 data(num training=49000, num validation=1000, num test=1000, num
_{dev=500}:
    Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
    it for the linear classifier. These are the same steps as we used for the
    SVM, but condensed to a single function.
    # Load the raw CIFAR-10 data
    cifar10 dir = 'cs231n/datasets/cifar-10-batches-py'
    # Cleaning up variables to prevent loading data multiple times (which may ca
use memory issue)
    try:
       del X train, y train
       del X_test, y_test
       print('Clear previously loaded data.')
    except:
       pass
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
    # subsample the data
    mask = list(range(num training, num training + num validation))
    X val = X train[mask]
    y val = y train[mask]
    mask = list(range(num training))
    X_{train} = X_{train}[mask]
    y train = y train[mask]
    mask = list(range(num test))
    X \text{ test} = X \text{ test[mask]}
    y_test = y_test[mask]
    mask = np.random.choice(num training, num dev, replace=False)
    X_{dev} = X_{train[mask]}
    y_{dev} = y_{train[mask]}
    # Preprocessing: reshape the image data into rows
    X train = np.reshape(X train, (X train.shape[0], -1))
    X_{val} = np.reshape(X_{val}, (X_{val.shape}[0], -1))
    X_test = np.reshape(X_test, (X_test.shape[0], -1))
    X \text{ dev} = \text{np.reshape}(X \text{ dev}, (X \text{ dev.shape}[0], -1))
    # Normalize the data: subtract the mean image
    mean image = np.mean(X train, axis = 0)
    X_train -= mean_image
    X_val -= mean_image
    X test -= mean image
    X dev -= mean image
    # add bias dimension and transform into columns
    X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
    X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
    X test = np.hstack([X test, np.ones((X test.shape[0], 1))])
    X_{dev} = np.hstack([X_{dev}, np.ones((X_{dev}.shape[0], 1))])
    return X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev
# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev = get_CIFAR10_data
```

```
()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
print('dev data shape: ', X_dev.shape)
print('dev labels shape: ', y_dev.shape)
```

Train data shape: (49000, 3073)
Train labels shape: (49000,)
Validation data shape: (1000, 3073)
Validation labels shape: (1000,)
Test data shape: (1000, 3073)
Test labels shape: (1000,)
dev data shape: (500, 3073)
dev labels shape: (500,)

# **Softmax Classifier**

Your code for this section will all be written inside cs231n/classifiers/softmax.py.

### In [ ]:

```
# First implement the naive softmax loss function with nested loops.
# Open the file cs231n/classifiers/softmax.py and implement the
# softmax_loss_naive function.

from cs231n.classifiers.softmax import softmax_loss_naive
import time

# Generate a random softmax weight matrix and use it to compute the loss.
W = np.random.randn(3073, 10) * 0.0001
loss, grad = softmax_loss_naive(W, X_dev, y_dev, 0.0)

# As a rough sanity check, our loss should be something close to -log(0.1).
print('loss: %f' % loss)
print('sanity check: %f' % (-np.log(0.1)))
```

loss: 2.370793

sanity check: 2.302585

#### **Inline Question 1**

Why do we expect our loss to be close to -log(0.1)? Explain briefly.\*\*

#### YourAnswer:

Since the parameter of weight W is uniformly distributed, then probability of predicting the right lable is  $\frac{1}{10}=0.1$ . (The number of class is 10). The loss function of softmax is  $L=-log(\frac{e^{f_{y_i}}}{\sum_j e^{f_j}})=-log(0.1)$ 

### In [ ]:

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```
# Complete the implementation of softmax loss naive and implement a (naive)
# version of the gradient that uses nested loops.
loss, grad = softmax loss naive(W, X dev, y dev, 0.0)
# As we did for the SVM, use numeric gradient checking as a debugging tool.
# The numeric gradient should be close to the analytic gradient.
from cs231n.gradient check import grad check sparse
f = lambda w: softmax loss naive(w, X dev, y dev, 0.0)[0]
grad numerical = grad check sparse(f, W, grad, 10)
# similar to SVM case, do another gradient check with regularization
loss, grad = softmax loss naive(W, X dev, y dev, 5el)
f = lambda w: softmax loss naive(w, X dev, y dev, 5e1)[0]
grad numerical = grad check sparse(f, W, grad, 10)
numerical: -3.584262 analytic: -3.584262, relative error: 1.015706e-
numerical: -0.712968 analytic: -0.712968, relative error: 2.469600e-
numerical: 1.964334 analytic: 1.964334, relative error: 2.454082e-08
numerical: 0.579612 analytic: 0.579612, relative error: 1.132592e-07
numerical: 2.074250 analytic: 2.074250, relative error: 6.018710e-09
numerical: -0.699314 analytic: -0.699314, relative error: 8.416069e-
80
numerical: 0.915196 analytic: 0.915196, relative error: 9.957081e-08
numerical: -3.078736 analytic: -3.078736, relative error: 4.248062e-
numerical: -5.636788 analytic: -5.636788, relative error: 1.017677e-
numerical: 0.287363 analytic: 0.287363, relative error: 3.168856e-07
numerical: 0.787721 analytic: 0.787721, relative error: 8.145083e-08
numerical: -2.636386 analytic: -2.636386, relative error: 5.160017e-
09
numerical: 0.468095 analytic: 0.468095, relative error: 4.628773e-08
numerical: 2.650473 analytic: 2.650473, relative error: 2.473295e-08
numerical: 3.169773 analytic: 3.169773, relative error: 2.405508e-08
numerical: 0.984871 analytic: 0.984871, relative error: 1.569300e-08
numerical: -0.866793 analytic: -0.866793, relative error: 4.092280e-
numerical: 1.672245 analytic: 1.672245, relative error: 9.048004e-09
numerical: 1.216457 analytic: 1.216457, relative error: 3.640168e-08
numerical: -1.268623 analytic: -1.268623, relative error: 3.700293e-
```

### In [ ]:

```
# Now that we have a naive implementation of the softmax loss function and its g
radient,
# implement a vectorized version in softmax loss vectorized.
# The two versions should compute the same results, but the vectorized version s
hould be
# much faster.
tic = time.time()
loss naive, grad naive = softmax loss naive(W, X dev, y dev, 0.000005)
toc = time.time()
print('naive loss: %e computed in %fs' % (loss naive, toc - tic))
from cs231n.classifiers.softmax import softmax loss vectorized
tic = time.time()
loss vectorized, grad vectorized = softmax loss vectorized(W, X dev, y dev, 0.00
0005)
toc = time.time()
print('vectorized loss: %e computed in %fs' % (loss vectorized, toc - tic))
# As we did for the SVM, we use the Frobenius norm to compare the two versions
# of the gradient.
grad difference = np.linalg.norm(grad naive - grad vectorized, ord='fro')
print('Loss difference: %f' % np.abs(loss naive - loss vectorized))
print('Gradient difference: %f' % grad difference)
```

naive loss: 2.370793e+00 computed in 0.345840s vectorized loss: 2.370793e+00 computed in 0.003938s

Loss difference: 0.000000 Gradient difference: 0.000000

### In [ ]:

```
# Use the validation set to tune hyperparameters (regularization strength and
# learning rate). You should experiment with different ranges for the learning
# rates and regularization strengths; if you are careful you should be able to
# get a classification accuracy of over 0.35 on the validation set.
from cs231n.classifiers import Softmax
results = {}
best val = -1
best softmax = None
# TODO:
# Use the validation set to set the learning rate and regularization strength.
# This should be identical to the validation that you did for the SVM; save
# the best trained softmax classifer in best softmax.
# Provided as a reference. You may or may not want to change these hyperparamete
rs
learning rates = [1e-7, 5e-7]
regularization strengths = [2.5e4, 5e4]
# *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
for learning rate in learning rates:
   for strength in regularization strengths:
       softmax = Softmax()
       loss hist = softmax.train(X train, y train, learning rate=learning rate,
reg=strength, num iters=2000, verbose=False)
       train pred = softmax.predict(X train)
       val pred = softmax.predict(X_val)
       train accuracy = np.sum(y train == train pred) / train pred.shape[0]
       val accuracy = np.sum(y val == val pred) / val pred.shape[0]
       if (val accuracy > best val):
           best val = val accuracy
           best softmax = softmax
       results[(learning rate, strength)] = train accuracy, val accuracy
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
# Print out results.
for lr, reg in sorted(results):
   train accuracy, val accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
              lr, reg, train accuracy, val accuracy))
print('best validation accuracy achieved during cross-validation: %f' % best val
```

```
lr 1.000000e-07 reg 2.500000e+04 train accuracy: 0.328898 val accura
cy: 0.340000
lr 1.000000e-07 reg 5.000000e+04 train accuracy: 0.306673 val accura
cy: 0.319000
lr 5.000000e-07 reg 2.5000000e+04 train accuracy: 0.317612 val accura
cy: 0.336000
lr 5.000000e-07 reg 5.000000e+04 train accuracy: 0.299102 val accura
cy: 0.317000
best validation accuracy achieved during cross-validation: 0.340000
```

### In [ ]:

```
# evaluate on test set
# Evaluate the best softmax on test set
y_test_pred = best_softmax.predict(X_test)
test_accuracy = np.mean(y_test == y_test_pred)
print('softmax on raw pixels final test set accuracy: %f' % (test_accuracy, ))
```

softmax on raw pixels final test set accuracy: 0.351000

#### Inline Question 2 - True or False

Suppose the overall training loss is defined as the sum of the per-datapoint loss over all training examples. It is possible to add a new datapoint to a training set that would leave the SVM loss unchanged, but this is not the case with the Softmax classifier loss.

### YourAnswer: True

*YourExplanation*: If we add a data point which is predicted correctly, the loss that this data point bringing in is 0. Then the svm loss won't increase. But in softmax case, there will always be non-zero loss no matter the prediction is right or wrong, according to the loss function.

#### In [ ]:

```
# Visualize the learned weights for each class
w = best_softmax.W[:-1,:] # strip out the bias
w = w.reshape(32, 32, 3, 10)

w_min, w_max = np.min(w), np.max(w)

classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship'
, 'truck']
for i in range(10):
   plt.subplot(2, 5, i + 1)

# Rescale the weights to be between 0 and 255
   wimg = 255.0 * (w[:, :, :, i].squeeze() - w_min) / (w_max - w_min)
   plt.imshow(wimg.astype('uint8'))
   plt.axis('off')
   plt.title(classes[i])
```



### In [ ]: