Complex Numbers

AI24BTECH11034 - Tanush Sri Sai Petla*

Section-A

Fill in the blanks

1. If the expression

 $\left[\sin\left(\frac{x}{2}\right) + \cos\left(\frac{x}{2}\right) + i\tan(x)\right]$ (1987 - 2Marks) $[1+2i\sin\frac{x}{2}]$

is real, then the set of all possible values of x is..... 2. For any two complex numbers z_1, z_2 and any real

 $|az_1 - bz_2|^2 + |bz_1 + az_2|^2 = \dots$ (1988 – 2*Marks*) 3. If a,b,c are the numbers between 0 and 1 such that the points $z_1 = a + i$, $z_2 = 1 + biandz_3 = 0$ form an equilateral triangle, then $a = \dots$ and $b = \dots$

(1989 - 2Marks)

number a and b.

4. ABCD is a rhombus. Its diagonals AC and BD intersect at the point M and satisfy BD = 2AC. If the points D and M represent the complex numbers 1 + i and 2 - i respectively, then A represents the complex number.... or.... (1993 - 2Marks)

5. Suppose Z_1, Z_2, Z_3 are the vertices of an equilateral triangle inscribed in the circle |z| = 2.If $Z_1 = 1 + i\sqrt{3}$ then $Z_2 =, Z_3 =$ (1994–2*Marks*)

B True/False

1. For complex number $z_1 = x_1 + iy_1$ and $z_2 = x_2 + iy_2$, we write $z_1 \cap z_2$, if $x_1 \le x_2$ and $y_1 \le y_2$. then for all complex numbers z with $1 \cap z$, we have $\frac{1-z}{1+z} \cap 0$ (1981 - 2Marks)

2. If the complex numbers z_1, z_2 and z_3 represent the vertices of an equilateral triangle such that $|z_1| = |z_2| = |z_3|$ then $z_1 + z_2 + z_3 = 0$ (1984 – 1*Mark*)

3. If three complex numbers are in A.P. then they lie on a circle on the complex plane. (1985 - 1Mark)

4. The cube roots of unity when represented on Argand diagram form the vertices of an equilateral triangle. (1988 - 1Mark)

C MCQs with One Correct Answer

1) If the cube roots of unity are $1, \omega, \omega^2$, then the roots of the equation $(x + 1)^8 = 0$ are (1979)

- a) $(a) -1, 1 + 2\omega, 1 + 2\omega^2$
- b) (b) $-1, 1 2\omega, 1 2\omega^2$
- c) (c) -1, -1, -1
- d) (d) None of these

2) The smallest positive integer for which $(\frac{1+i}{1-i})^n =$ 1 is (1980)

- a) (a) n = 8
- b) (b) n = 16
- c) (c) n = 12
- d) (d) None of these

3) The complex number z = x + iy which satisfy the equation (1981 - 2Marks)

$$\left|\frac{z-5i}{z+5i}\right| = 1$$
lie on

- a) (a) the x-axis
- b) (b) the straight line y = 5
- c) (c) a circle passing through the origin
- d) (d) None of these

4) If $z = (\frac{\sqrt{3}}{2} + \frac{i}{2})^5 + (\frac{\sqrt{3}}{2} - \frac{i}{2})^5$, then (1982 -2Marks)

- a) (a) Re(z) = 0
- b) (b) Im(z) = 0
- c) (c) Re(z) > 0, Im(z) > 0
- d) (*d*) Re(z) > 0, Im(z) < 0

5) The inequality |z-4| < |z-2| represents the (1982 - 2Marks)region given by

- a) (a) $Re(z) \ge 0$
- b) (b) Re(z) < 0
- c) (c) Re(z) > 0
- d) (d) None of these