

Complex Numbers

AI24BTECH11034 - Tanush Sri Sai Petla*

Section-A

Fill in the blanks

1. If the expression

$$\frac{[\sin(\frac{x}{2}) + \cos(\frac{x}{2}) + i \tan(x)]}{[1 + 2i \sin(\frac{x}{2})]}$$

is real, then the set of all possible values of x is... equation

2. For any two complex numbers z_1, z_2 and any real number a and b . $\left| \frac{z-5i}{z+5i} \right| = 1$ lie on

$$|az_1 - bz_2|^2 + |bz_1 + az_2|^2 = \dots \quad (1988 - 2 \text{ Marks})$$

3. If a, b, c are the numbers between 0 and 1 such that the points $z_1 = a + i, z_2 = 1 + bi$ and $z_3 = 0$ form an equilateral triangle, then $a = \dots$ and $b = \dots$

4. If $z = (\frac{\sqrt{3}}{2} + \frac{i}{2})^5 + (\frac{\sqrt{3}}{2} - \frac{i}{2})^5$, then $(1982 - 2 \text{ Marks})$

4. ABCD is a rhombus. Its diagonals AC and BD intersect at the point M and satisfy $BD = 2AC$. If the points D and M represent the complex numbers $1 + i$ and $2 - i$ respectively, then A represents the complex number..... or.....

5. Suppose Z_1, Z_2, Z_3 are the vertices of an equilateral triangle inscribed in the circle $|z| = 2$. If $Z_1 = 1 + i\sqrt{3}$ then $Z_2 = \dots, Z_3 = \dots$

5. Suppose Z_1, Z_2, Z_3 are the vertices of an equilateral triangle inscribed in the circle $|z| = 2$. If $Z_1 = 1 + i\sqrt{3}$ then $Z_2 = \dots, Z_3 = \dots$

6. True/False

1. For complex number $z_1 = x_1 + iy_1$ and $z_2 = x_2 + iy_2$, we write $z_1 \cap z_2$, if $x_1 \leq x_2$ and $y_1 \leq y_2$. then for all complex numbers z with $1 \cap z$, we have $\frac{1-z}{1+z} \cap 0$

2. If the complex numbers z_1, z_2 and z_3 represent the vertices of an equilateral triangle such that $|z_1| = |z_2| = |z_3|$ then $z_1 + z_2 + z_3 = 0$

3. If three complex numbers are in A.P. then they lie on a circle on the complex plane.

4. The cube roots of unity when represented on Argand diagram form the vertices of an equilateral triangle.

C MCQs with One Correct Answer

1. If the cube roots of unity are $1, \omega, \omega^2$, then the roots of the equation $(x + 1)^8 = 0$ are

$$(a) -1, 1 + 2\omega, 1 + 2\omega^2$$

$$(b) -1, 1 - 2\omega, 1 - 2\omega^2$$

$$(c) -1, -1, -1$$

$$(d) \text{None of these}$$

2. The smallest positive integer for which $(\frac{1+i}{1-i})^n = 1$ is

$$(a) n=8$$

$$(b) n=16$$

$$(c) n=12$$

$$(d) \text{None of these}$$

3. The complex number $z = x + iy$ which satisfy the equation

$$\left| \frac{z-5i}{z+5i} \right| = 1$$

$$(a) \text{the } x\text{-axis}$$

$$(b) \text{the straight line } y=5$$

$$(c) \text{a circle passing through the origin}$$

$$(d) \text{None of these}$$

$$(a) \operatorname{Re}(z)=0$$

$$(b) \operatorname{Im}(z)=0$$

$$(c) \operatorname{Re}(z) > 0, \operatorname{Im}(z) > 0$$

$$(d) \operatorname{Re}(z) > 0, \operatorname{Im}(z) < 0$$

5. The inequality $|z - 4| < |z - 2|$ represents the region given by

$$(a) \operatorname{Re}(z) \geq 0$$

$$(b) \operatorname{Re}(z) < 0$$

$$(c) \operatorname{Re}(z) > 0$$

$$(d) \text{None of these}$$

$$(1980)$$