

HASH TABLES

CONTIGUOUS ARRAYS

0x40

“foo”

0x41

“bar”

0x42

“baz”

0x43

0x44

0x45

0x46

PROBLEMS WITH CONTIGUOUS ARRAYS

“hello”

0x40

0x41

0x42

0x43

0x44

0x45

0x46

“doe” - “a deer”
“ray” - “drop of golden sun”
“me” - “a name”

dictionary /'dɪkʃənə
book listing (usu. al
explains words
giving
language. 2 reference
the terms of a pa

Dictionary

The Dictionary ADT

- AKA Associative Array, Map, or Symbol Table
- Stores **key-value** pairs (e.g. "location" : "NY")
- **Unique keys**
- **Modify & lookup**
 - Set value for key
 - Get value for key
- **Dynamic alteration**
 - Add new pairs
 - Delete existing pairs



How to implement this ADT?

The classic data structure: a Hash Table

High-concept: an array to hold **values**, and a *hash function* that transforms a string **key** into a numerical **index**

A simple hash function

```
function hash (keyString) {  
  let hashed = 0;  
  for (let i = 0; i < keyString.length; i++) {  
    hashed += keyString.charCodeAt(i);  
  }  
  return hashed % 7; // number of spaces in array  
}
```

“NAME”

“Grace”

HASH
FUNCTION

5

0x40

0x41

0x42

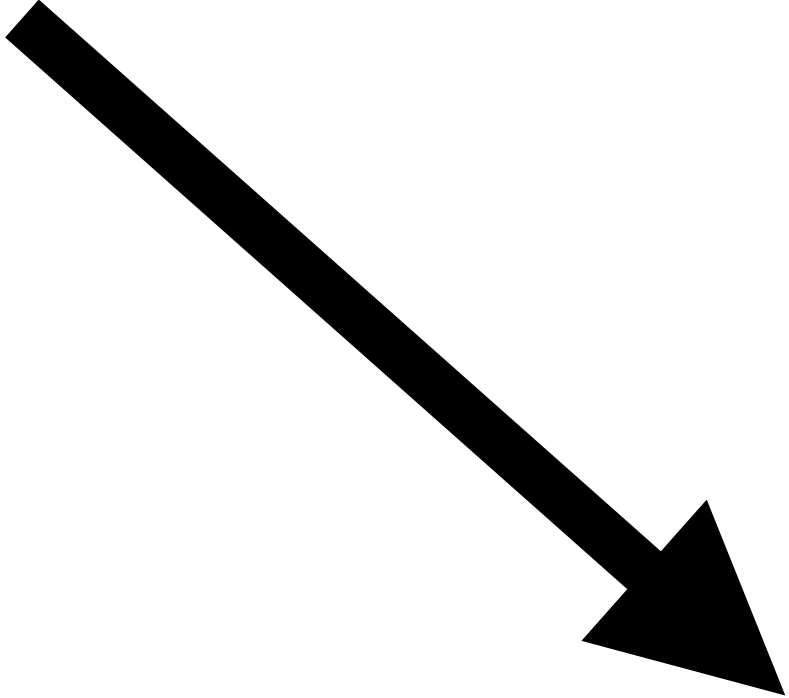
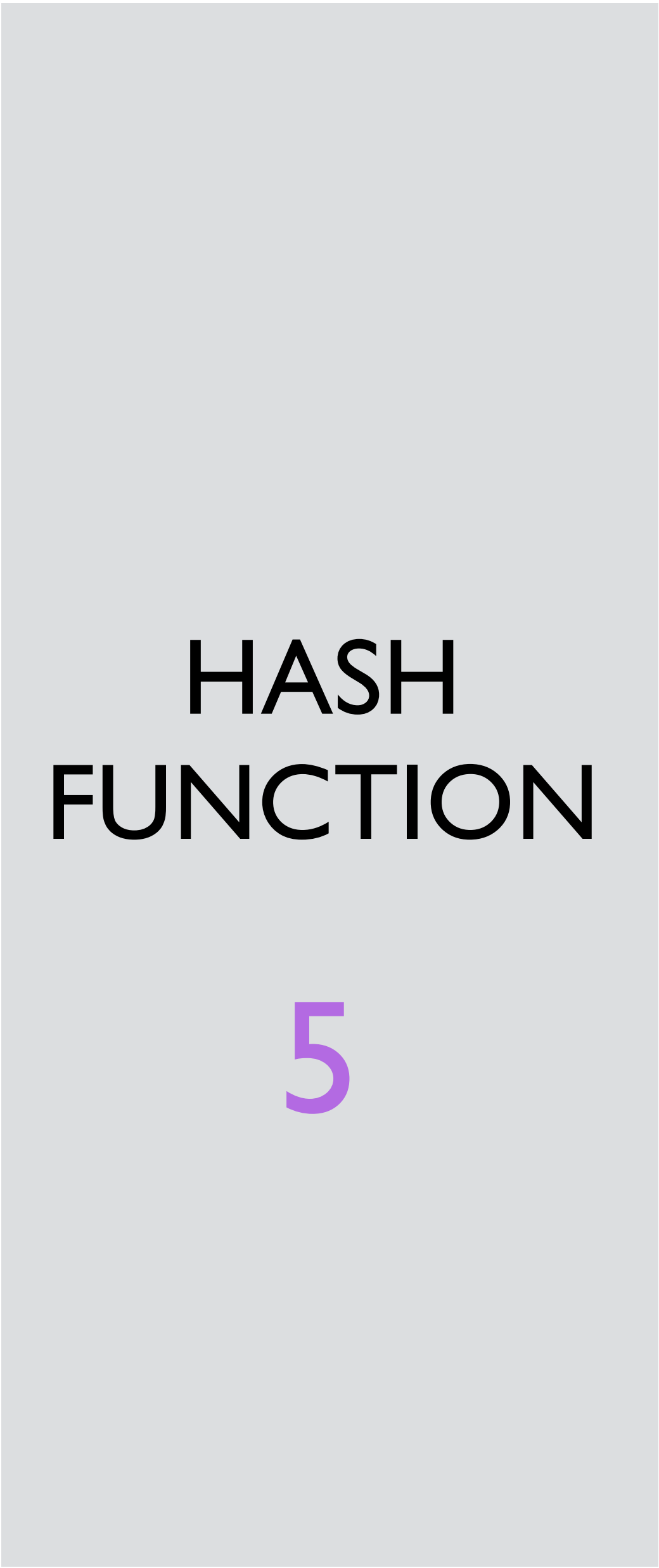
0x43

0x44

0x45

0x46

“NAME”



0x40

0x41

0x42

0x43

0x44

0x45

0x46

“Grace”


```
contact.name = 'Grace'  
contact.phone = 8675309
```

Example with a 9-bucket array

1. We want to store the value **'Grace'** for the key **'name'**.
2. Hashing the string **'name'** yields the numerical index **3**.
3. Store **'Grace'** at index **3**.
4. Now store the value **8675309** for key **'phone'**
5. **'phone'** hashes to **7**
6. Store **8675309** at index **7**

| Index | Data |
|-------|---------|
| 0 | |
| 1 | |
| 2 | |
| 3 | Grace |
| 4 | |
| 5 | |
| 6 | |
| 7 | 8675309 |
| 8 | |

Fetching/changing values

1. Q: what is the value for the key **'name'**?
2. Hashing the string **'name'** yields the numerical index **3**.
3. Find the value at index **3**.
4. Result: **'Grace'**
5. Similar steps for checking the key **'phone'**, gets the value **8675309**.

| Index | Data |
|-------|---------|
| 0 | |
| 1 | |
| 2 | |
| 3 | Grace |
| 4 | |
| 5 | |
| 6 | |
| 7 | 8675309 |
| 8 | |

Anyone see a problem?

Collisions

1. Now we want to store the value `grace@gmail.com` for the key `email`.
2. Hashing `email` yields the numerical index `7`.
3. But we **already have** a value there (for `phone`)!
4. Because there are many more possible keys than buckets, collisions are inevitable.

| Index | Data |
|-------|---------|
| 0 | |
| 1 | |
| 2 | |
| 3 | Grace |
| 4 | |
| 5 | |
| 6 | |
| 7 | 8675309 |
| 8 | |

How to resolve collisions?

Two main strategies

- **Open addressing:** if a bucket is full, find the next empty bucket. Place the value in that spot instead of the original.

- **Separate chaining:** every bucket stores a secondary data structure, like a linked list. Collisions create new entries in that data structure.

Separate chaining: adding a value

1. We want to store the value `grace@gmail.com` for the key `email`.
2. Hashing `email` yields the numerical index `7`.
3. That bucket already contains `8675309`.
4. Add the value to the Linked List as a new `node`.

| Index | Linked List in bucket |
|-------|-------------------------------|
| 0 | |
| 1 | |
| 2 | |
| 3 | <Grace> |
| 4 | |
| 5 | |
| 6 | |
| 7 | <8675309> → <grace@gmail.com> |
| 8 | |

We still have a problem...


Separate chaining: retrieving a value

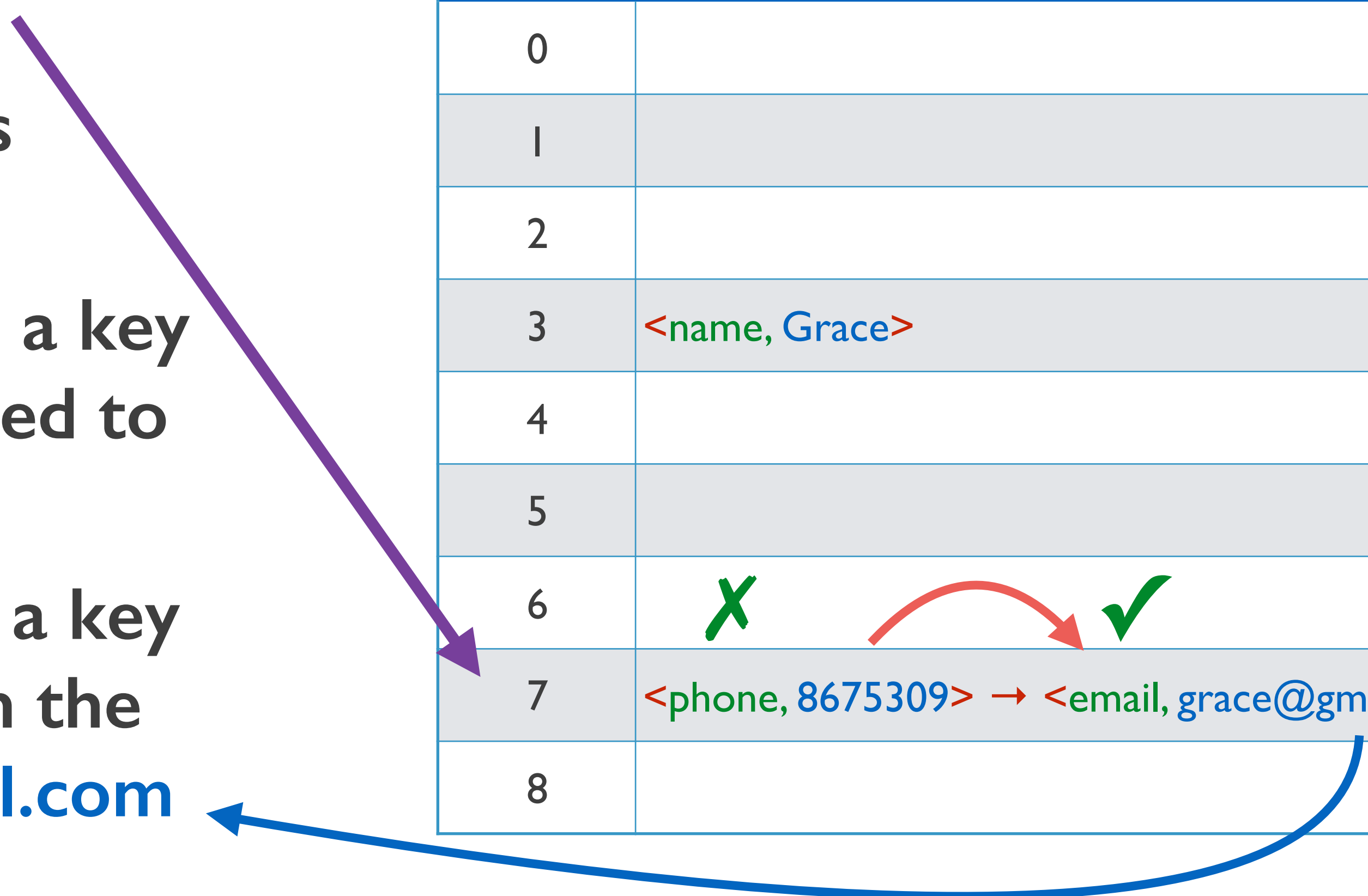
1. What is the value for the key **email**?
2. Hashing **email** yields the numerical index **7**.
3. In bucket **7** there is a linked list.
4. There are *two nodes* in that list; how do we know which value is for the key **email**?

| Index | Linked List in bucket |
|-------|-------------------------------|
| 0 | |
| 1 | |
| 2 | |
| 3 | <Grace> |
| 4 | |
| 5 | |
| 6 | ? ? |
| 7 | <8675309> → <grace@gmail.com> |
| 8 | |

Separate chaining: store value *and* key

1. Hashing **email** yields the numerical index **7**.
2. In bucket **7** there is a linked list.
3. The **head** node has a key of **phone**, so we need to keep looking.
4. The **next** node has a key **email**, so we return the value: **grace@gmail.com**

| Index | Linked List in bucket |
|-------|---|
| 0 | |
| 1 | |
| 2 | |
| 3 | <name, Grace> |
| 4 | |
| 5 | |
| 6 |  |
| 7 | <phone, 8675309> → <email, grace@gmail.com> |
| 8 | |



**So... how is a hash table better
than a linked list?**

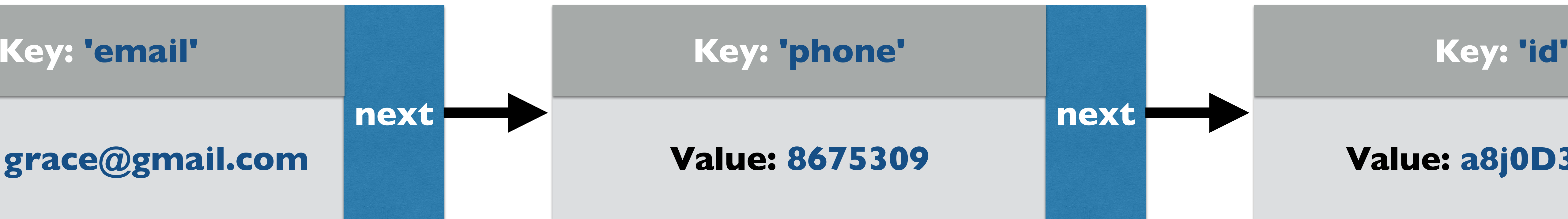
Performance

- ◉ Assume many buckets and a good hashing function
- ◉ *Usually*: assign or check pair takes just 1 step (hash invocation)
- ◉ *Sometimes*: collisions occur
 - Traverse a few nodes of a linked list; but *just a few* (still pretty fast)
 - Way better than having to traverse *all the data* in the entire structure!



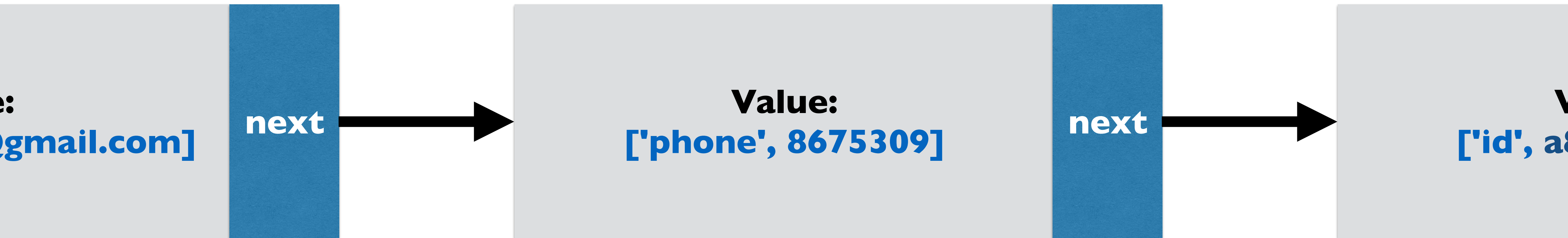
List nodes with key-value pairs — how?

Solution 1: *Association List*



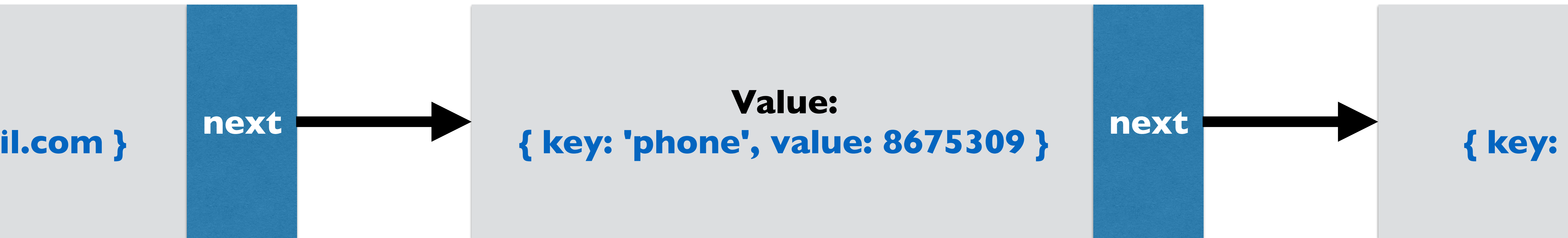
- Nodes have key as well as **value** & **next**
 - Advantage: best for purpose, most straightforward.
 - Downside: need a custom LL implementation

Solution 2: store an array



- LL node value is an array, index 0 stores HT key & 1 stores HT value
 - Downside: referring to indices 0 and 1 isn't very descriptive / easy to read

Solution 3: store a struct



- LL node value is itself a data structure with **key** & **value** prop.s
 - Seems like cheating, but you can hand-wave this by pretending we are using "structs" — pre-defined memory structures that cannot add/delete keys. In fact we can apply this same reasoning to our LL implementation, where nodes themselves are structs.
 - Referring to the "value of the linked list node value" gets confusing.

WHAT ABOUT JS?

Sound familiar?

- **JavaScript Objects**
- **JS *Engines* (like V8) implement most Objects as structs**
 - V8 defines a new struct every time you add a property
 - If this would be madness (ex: you are storing a phone book), it switches to using a hash table
- **In the end, the Object specified in EcmaScript is a data *type*; we know what behavior it should exhibit, but not necessarily how it is implemented at runtime. That's up to the engine.**