

$$\begin{aligned}\dot{x} &= Ax + Bu \\ y &= Cx\end{aligned}\tag{1}$$

Let  $\mathcal{A}$  be the set of matrices with eigenvalues  $l_i = \lambda_i$  and constants (determined by the transfer function)  $k_j = c_j$ . Define  $\epsilon_i = |\lambda_i^* - \lambda_i|$  and  $j = |k_j^* - k_j| : j > i$  Let  $\mathcal{L}$  be the set of matrices where  $\sum_i^n \alpha_i \epsilon_i < \epsilon_0$

$$P \in \mathcal{P} \text{ if } PB = B \text{ and } CP^{-1} = C \text{ and } PAP^{-1} \in \mathcal{A} \tag{2}$$

$$\text{For } C = [1 \ 0] \text{ and } B = [1 \ 1]^T, P_p = \begin{bmatrix} 1 & 0 \\ p & 1-p \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} P_p A P_p^{-1} + \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix} P_q A P_q^{-1} \notin \mathcal{L}$$

$$\lambda_{1,2} = \frac{1}{2} \left( \lambda_1 + \lambda_2 + x - \bar{x} \pm \left( (\lambda_1 - \lambda_2)^2 - (x - \bar{x}) \left( (x + 3\bar{x}) + 2(\lambda_1 + \lambda_2) + \frac{4(\lambda_1 - \bar{x})(\lambda_2 - \bar{x})}{k + \bar{x}} \right) \right)^{1/2} \right)$$

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