

# MASTER SEMINAR: DATA SCIENCE & OPTIMIZATION



## THE FUTURE OF MULTI-VARIANT PRODUCTION: CAR SEQUENCING

Aleksandra Petrenko & Ninh Tran

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# Motivation: Why car sequencing?

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- Customers require more customer-tailored products => the variety of product models is growing
- How to produce various model without cost-intensive work overloads?
- Common approaches: Car Sequencing (CS) and Mixed-Model Sequencing (MMS) => CS is easier to implement

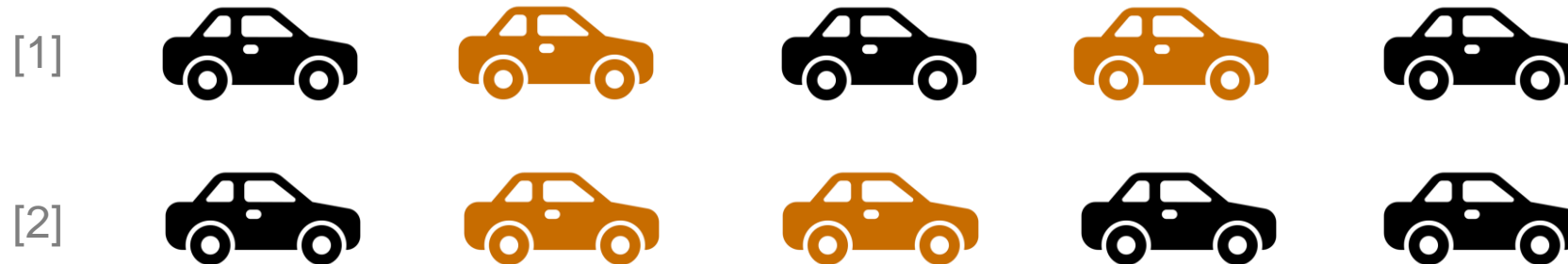




# AGENDA

- 1 INTRODUCTION TO SEQUENCING
- 2 RESEARCH QUESTIONS
- 3 MATHEMATICAL MODEL
- 4 LITERATURE REVIEW
- 5 THE FUTURE OF CAR SEQUENCING
- 6 CONCLUSION REMARKS

- In production planning, sequencing **defines optimal orders** when various products are being produced at a production line in order to **minimize setup costs or avoid work overload**
- Assume there are 2 types of car (**orange** and **black**) processed intermixed in a line
- Comparing between 2 sequences, **which sequence** would not generate work overload?



- Sequencing theory is a **mathematical model** that turns manufacturing goals into **objective functions**, incorporating other **constraints** such as labor utility and capital capacity
- There are **two common approaches: car sequencing (CS)** and **mixed-model sequencing (MMS)**

MMS

- Derives **explicit method for calculating workload**. Therefore, objective function is to **minimize total work generated**
- Tedious effort in collecting operation data

CS

- Based on an **implicit rule  $H_0 : N_0$**  which restricts the number of successive models with long processing time. Therefore, objective function is to **minimize total number of violations** in each subsequence
- Easy to implement





Our work tries to answer the following research questions:

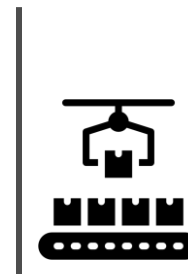
”

- What are the **advantages of car sequencing** compared to mixed-model sequencing?
- What are the **sequencing rules** that generate a result as good as mixed-model sequencing?
- What are the **recent trends** in literature about car sequencing?
- What are the **suggestions for future research**?
- In **which industries** could car sequencing still be applied?

“

## Problem formulation

- Assume that there are 2 models of cars that are **processed intermixed** in a production line
  -  Black model (a car **without** feature “O”, with **shorter processing time  $p = 2$** )
  -  Orange model (a car that **requires a feature/option “O”**, with **longer processing time  $p = 7$** )
- The problem concerns the **order** of car to **avoid work overload**
- What is the design of one workstation on a production line?
  - Conveyor used to place the models **moves from left to right**
  - Operators return to the left border to proceed the next product



Left-border station



Right-border station

## Problem formulation

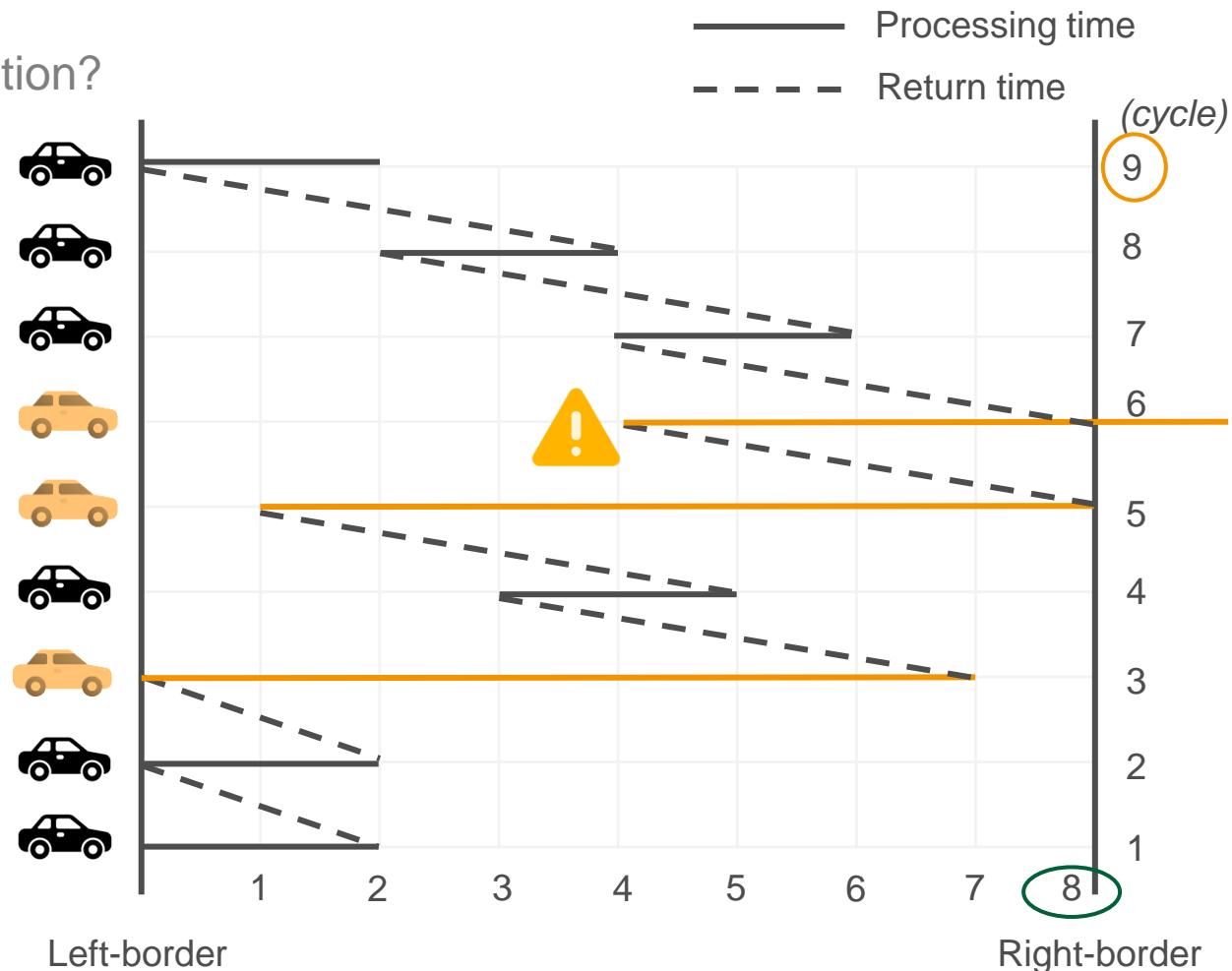
- How does work overload incur at the workstation?

- A workstation is set up as described:

- $T$  cycles ( $T = 9$ )
- Border length  $l_k$  ( $l = 8$ )

- Movement of cars within the workstation:

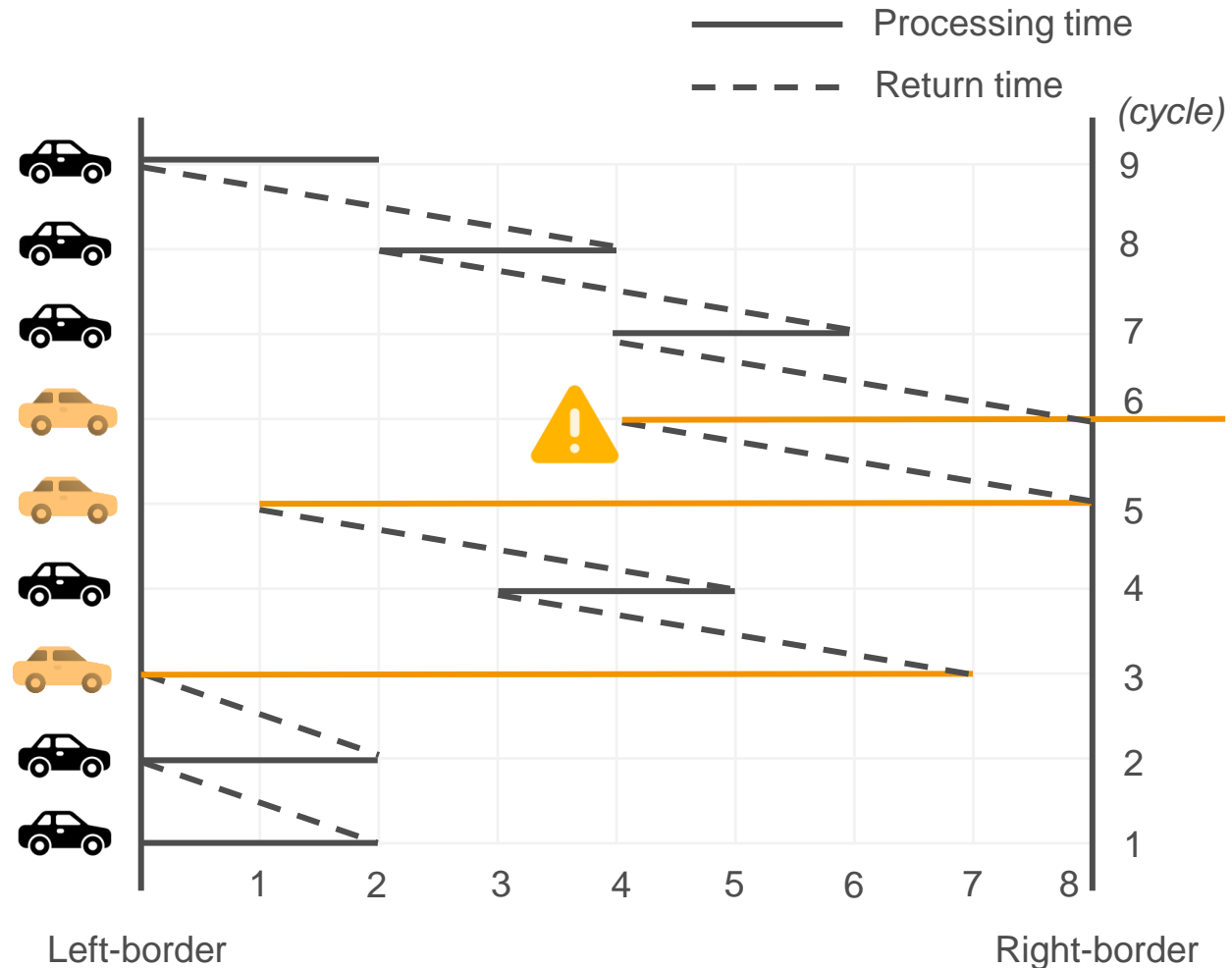
- A black car enters a station
- After handling, operator comes back and continue until finish the 5<sup>th</sup> car
- However, he **cannot finish the 6<sup>th</sup>** car and work overload incur
- We assume it is compensated and the line continue until the end





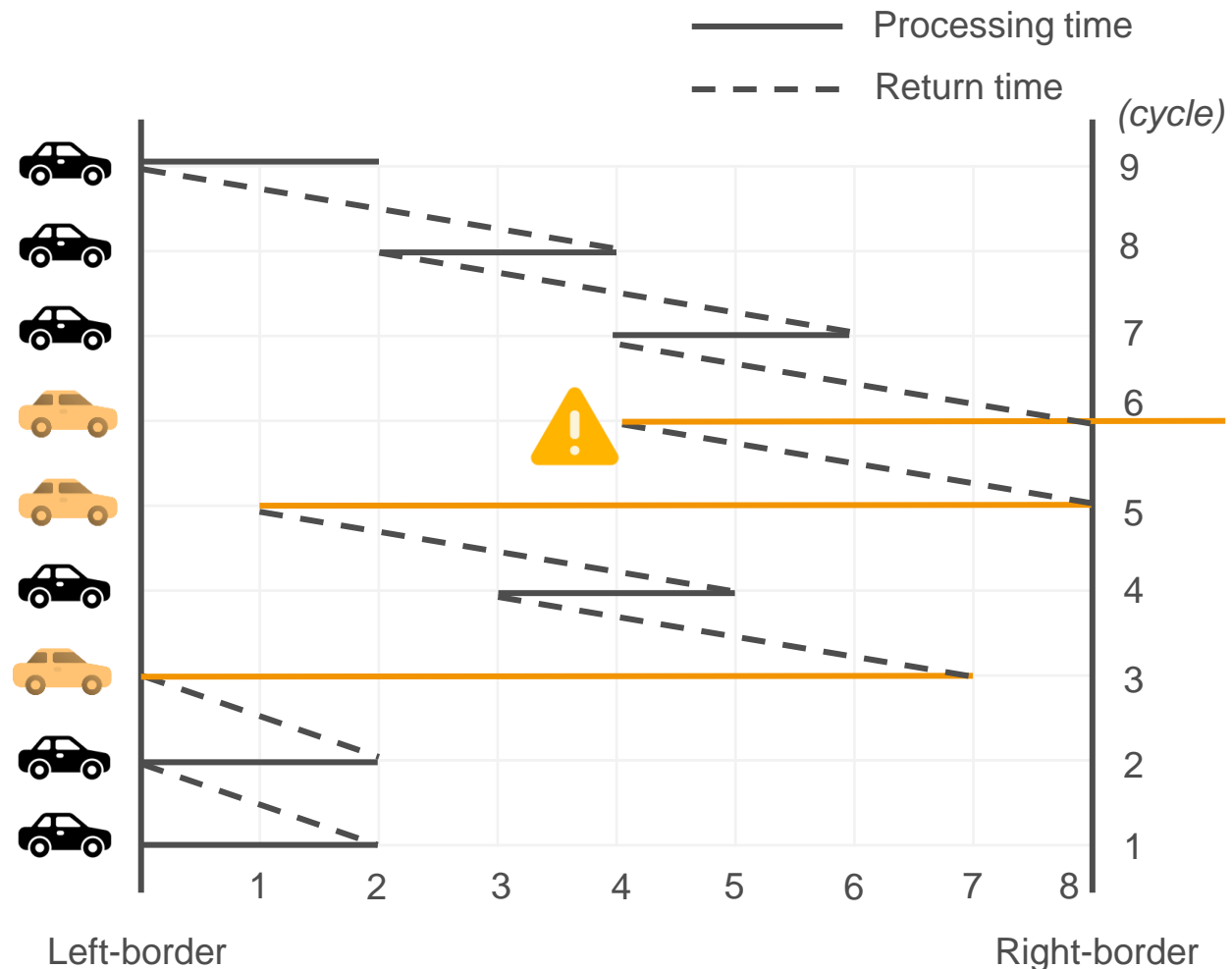
## Problem formulation

- A feasible sequence
  - B – B – O – B – O – O – B – B – B is not feasible as work overload incurs
  - 2 orange models should not enter the line consecutively
- Car sequencing rule  $H_o : N_o$ 
  - $H_o$  restricts the number of models with option O that could be processed consecutively without generating work overload
  - $N_o$  is  $H_o$  plus other models (w/o O) to get the operators back to left-border station



## Assumptions of mathematical model

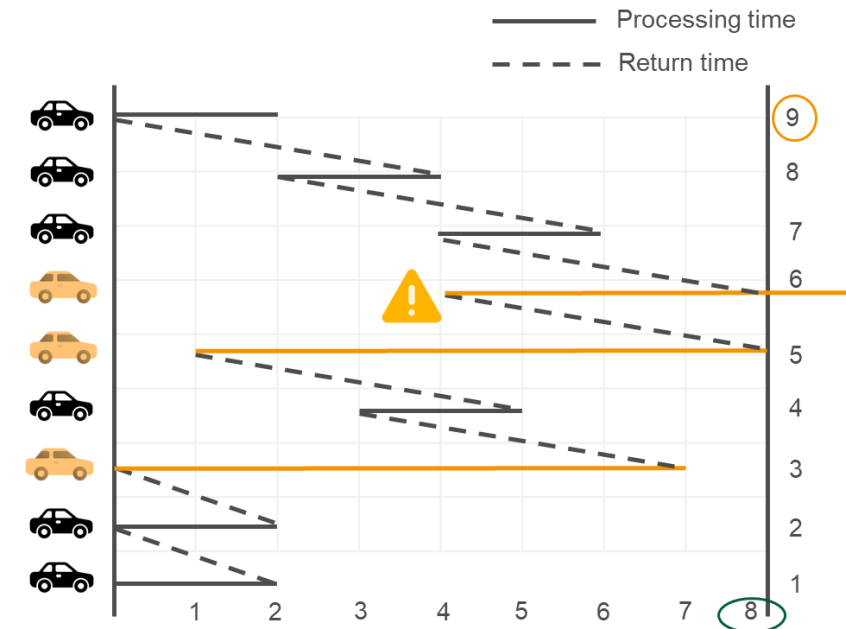
- Workflow is from left to right
- Operators can work only in their workstation
- Product models move at a constant speed
- All workstations are set up successively
- The products are processed as long as they meet the operators within the stations
- The operator has sufficient time to return to proceed next model
- **Demand** and **processing time** are **deterministic** and remain **constant**
- Work overload will be compensated and therefore **no line stoppage**



## Introduction to variables of the mathematical models

- Settings: consider a production line with K workstations (index k), T cycle (index t), M models (index m) cycle time c and 2 models with **2 processing time**
  - $p_o^+$ , **longer processing time**, for model with option O
  - $p_o^-$ , **shorter processing time**, for model w/o O
- The model is based on Golle et. al., (2014) and describes a car sequencing model with **multiple sequencing rules** (MSR) in which **each rule is assigned a weighting factor  $\lambda_0$**

$$\lambda_0 = p_o^+ - c$$



## Introduction to variables of the mathematical models

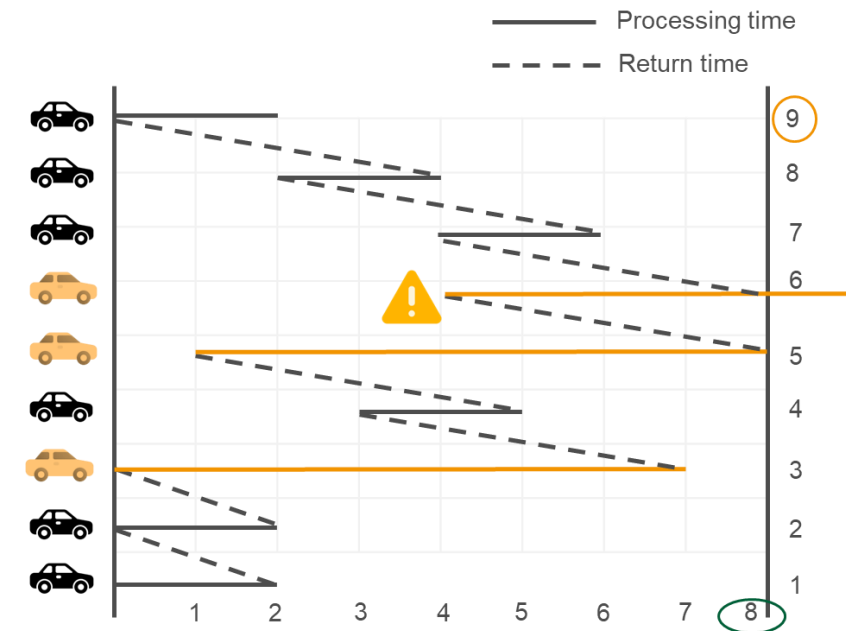
- $v_0$  calculates **the number of successive models with option O** in a sequence

$$v_0 = \sum_{t=1}^{T-N_o^q+1} \min \left\{ 1; \max \left\{ \sum_{t'=t}^{t+N_o^q-1} \sum_{m \in M} a_{om} \cdot x_{mt'} - H_o^q; 0 \right\} \right\}$$

$H_o^q : N_o^q$  is the rule in sequencing rule  $q^{\text{th}}$

$a_{om}$  is a binary variable. 1 if model contains option o, 0 otherwise

$x_{mt'}$  is a binary variable. 1 if model is produced in slot t, 0 otherwise



## Introduction to variables of the mathematical models

- Define the number of rules (Q)

$Q_o$  amounts to  $q_o^{max} - q_o^{min} + 1$  with

$$q_o^{min} = \left\lfloor \frac{l_o - c}{p_o^+ - c} \right\rfloor \forall o \in O \quad (1)$$

$$q_o^{max} = \left\lfloor \frac{T(c - p_o^-) + (l_o - c)}{p_o^+ - p_o^-} \right\rfloor \forall o \in O \quad (2)$$

Then,  $\forall q_o \in [q_o^{min}, q_o^{max}]$ , MSR generates a rule  $H_o^{q_o - q_o^{min} + 1} : N_o^{q_o - q_o^{min} + 1}$  with

$$H_o^{q_o - q_o^{min} + 1} = q_o \quad \forall o \in O \quad (3)$$

$$N_o^{q_o - q_o^{min} + 1} = H_o^{q_o - q_o^{min} + 1} + \left\lfloor \frac{q_o \cdot (p_o^+ - c) + (l_o - p_o^+)}{c - p_o^-} \right\rfloor \forall o \in O \quad (4)$$

$q_o^{min}$  Maximum number of successive models containing option  $o$  without inducing work overload, equals  $H_o$   
 $q_o^{max}$  Maximum number of models with option  $o$  that can occur in a sequence of length  $T$  without work overload

- Numerical example:

Assume that  $l_o = 20$  and there are two car models, with two processing time  $p_o^+ = 15$  and  $p_o^- = 5$  respectively. The cycle time is 10 and we assume that the length of the sequence  $T = 12$

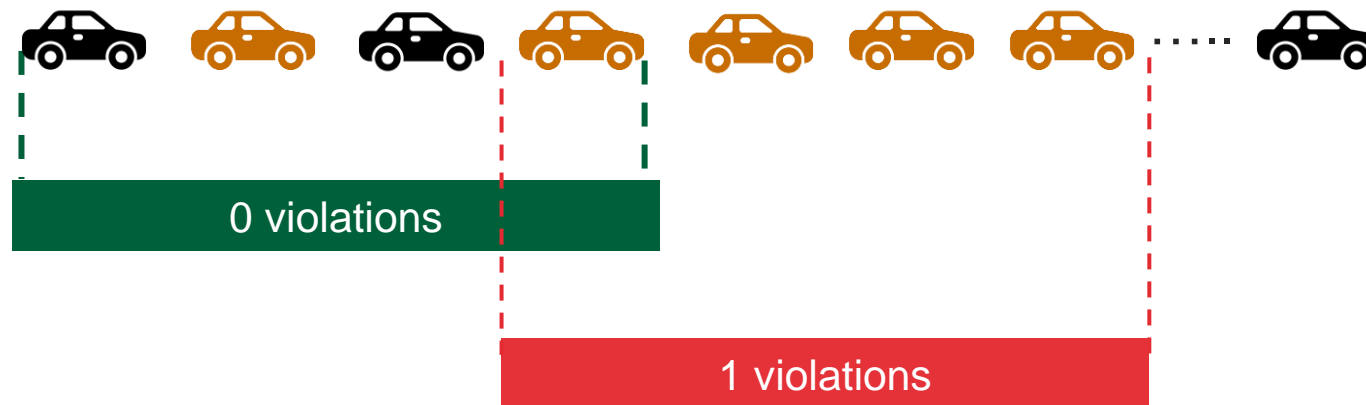
From (1) and (2) we derive  $q_o^{min} = 2$  and  $q_o^{max} = 7$ , which indicates that we would have 6 sequencing rules

From (3) and (4), we get  $H_o^1 : N_o^1 = 2 : 3$ ,  $H_o^2 : N_o^2 = 3 : 4$ ,  $H_o^3 : N_o^3 = 4 : 5$ ,  $H_o^4 : N_o^4 = 5 : 6$ ,  $H_o^5 : N_o^5 = 6 : 7$  and  $H_o^6 : N_o^6 = 7 : 8$

## Introduction to variables of the mathematical models

- How does multiple sequencing rules per station work?

It follows sliding window. Assume we have a sequence of total 8 cars as and examine the rule of  $H_o^2 : N_o^2 = 3 : 4$  (*under a subsequence of 4 cars, there are maximum of 3 orange cars that can be processed consecutively to avoid work overload*)



- Numerical example:

Assume that  $l_o = 20$  and there are two car models, with two processing time  $p_o^+ = 15$  and  $p_o^- = 5$  respectively. The cycle time is 10 and we assume that the length of the sequence  $T = 12$

From (1) and (2) we derive  $q_o^{min} = 2$  and  $q_o^{max} = 7$ , which indicates that we would have 6 sequencing rules

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## Introduction to model objective functions

- Objective functions

$$\text{minimize } obj^w = \sum_{o \in O} \lambda_o \frac{1}{Q_o} \sum_{q \in Q_o} v_{oq}$$

(minimize total number of violations with weighting factors)

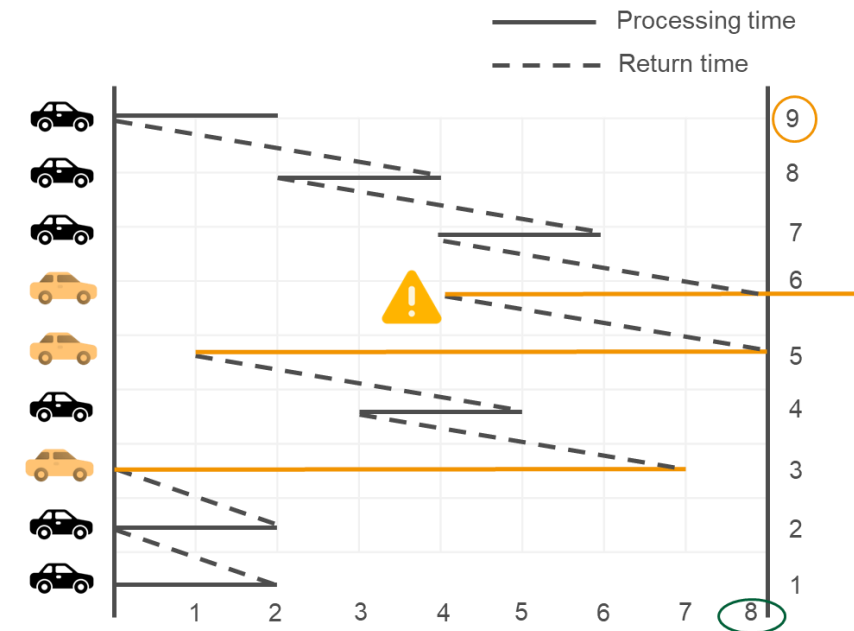
subject to

$$\sum_{t=1}^T x_{mt} = d_m$$

( $d_m$  demand, total production output needs to meet demand)

$$\sum_{m \in M} x_{mt} = 1 \quad \forall t = 1, \dots, T$$

(each slot in the sequence contains exactly 1 model)



## Advantages of car sequencing compared to mixed-model sequencing

- Based on Golle et. al., 2014 and Louis et. al., 2023 car sequencing are considered
  - **Easy** to apply and execute in practice
  - **Less effort** in constructing the mathematical model and data collection process
  - The evaluation of sequence is **faster**
- However, all previous studies shown that
  - **MMS generates less overload** than CS for assembly workers (using both real-case industry data and random instances)

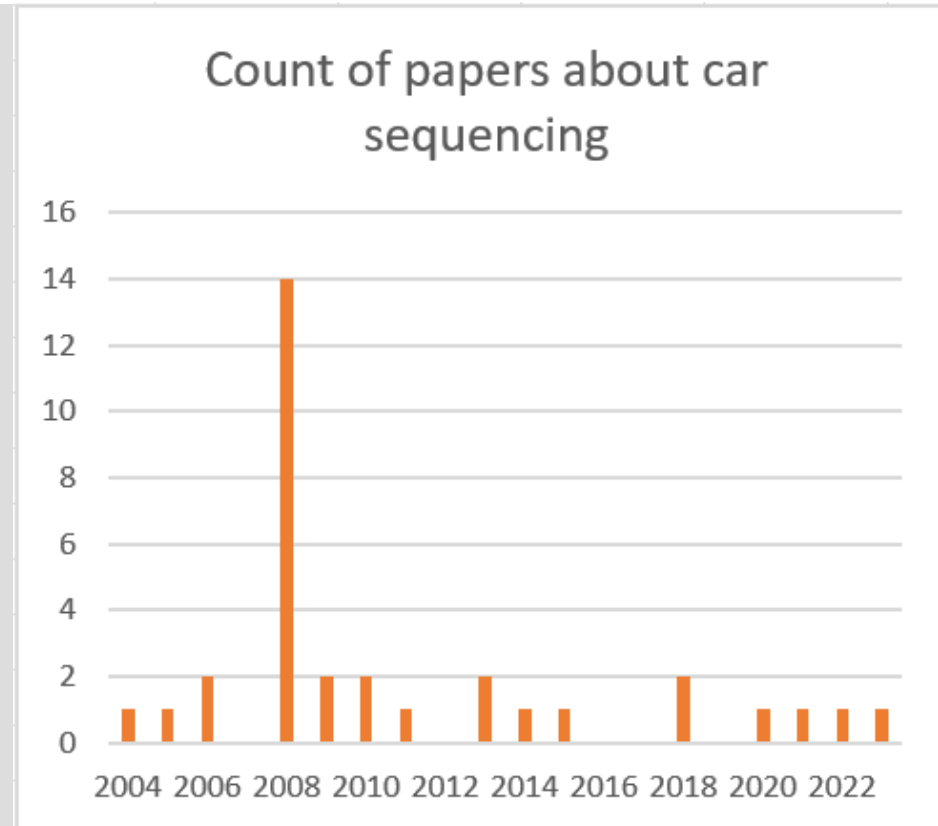
## Selection of sequencing rules

- Based on Golle et. al., 2014, there are 2 scenarios of misclassifying in CS
  - A sequence is **feasible in CS** but **not feasible in MMS**
    - Sequencing **rules are not strict** enough to eliminate circumstances where work overload would happen
    - **Additional costs** to deal with unforeseen work overload if it is incurred
  - A sequence is **infeasible in CS** but **feasible in MMS**
    - Car sequencing is **unnecessarily strict** that no sequence could fulfill
    - The elimination of feasible solutions would potentially lead to the removal of optimal solution or in the worst case, **no feasible sequences could be found**
- The quality of CS rules are based on the **percentage of misclassification**. The lower, the better

## Selection of sequencing rules

- There are **3 sequencing rules** that have been used for previous research studies
  - **One** sequencing rule (introduced by Golle et al., 2014)
  - **Multiple** sequencing rules (MSR) per station (introduced by Golle et al., 2014)
  - **Unique** sequencing ratio (USR) per station (introduced by Lesert, Alpan, and Frein 2011)
- Finding from Louis et. el., 2023 and Golle et al., 2014
  - **MMS always achieve the best results** compared to CS
  - With industry real-case data:
    - CS with MSR method **are as good as MMS when cars on one sequence are limited**
    - Otherwise, **MMS helps achieve better results** than CS
    - Among 3 sequencing rules, **USR gave the best results**

- SCOPUS database
- Journals with ranking from A+ to B according to VHB-JOURQUAL rating for operations research
- Period from 2004 to 2023 inclusively
- ROADEF'05 challenge in 2005 initiated by Renault company (mostly papers of 2008) => the period reduced to 2010-2023
- Excluding Estellon and Gardi (2013)
- **=> 12 highly rated papers**



Title		Problem formulation			Contribution					
Paper	Year	Problem type	Objective function	Options per station	Solution method	Algorithm type	Bounds improved	Comparison of CS and MMS	Sequencing rules creation	Instance space analysis
Giard and Jeunet	2010	CS with sequence-dependent setups and utility workers	minimize the cost function involving costs associated with additional utility workers and setup costs	2, colors	MIP solved with ILOG-Cplex 9.0	exact algorithm	-	-	-	-
Golle et al.	2010	CS	-	multiple	-	-	-	-	X	-
Lesert et al.	2011	CS	minimize the number of violations	multiple	sequencing tool of an automotive company	-	-	-	X	-
Yavuz	2013	combined CS and LS	minimize the sum of absolute differences between actual and ideal positions of variant copies	2	iterated beam search	both heuristic or exact algorithm	tight lower bounds, upper bounds	-	-	-



Title		Problem formulation			Contribution					
Paper	Year	Problem type	Objective function	Options per station	Solution method	Algorithm type	Bounds improved	Comparison of CS and MMS	Sequencing rules creation	Instance space analysis
Golle et al.	2014	CS	minimize the number of (weighted) violations with 3 objective functions: 1) sliding window (Gravel et al., 2005), 2) Fliedner and Boysen (2008) function, 3) Bolat and Yano (1992) function	2	MIP solved with CPLEX 12.2	exact algorithm	-	X CS is worse	-	-
Golle et al.	2015	CS	minimize the number of (weighted) violations with 3 objective functions: 1) sliding window (Gravel et al., 2005), 2) Fliedner and Boysen (2008) function	2	iterated beam search	both heuristic or exact algorithm	lower bounds improved	-	-	-
Jahren and Achá	2018	industrial CS	minimize the weighted sum of 2 objectives: ratio costs and paint changes	2, colors	column generation based algorithm	exact algorithm	lower, upper bounds improved	-	-	-

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Yavuz and Ergin	2018	combined CS and LS	minimize sum of absolute differences between actual and ideal positions of variant copies	2	constraint propagation, branch-and-bound	heuristic	-	-	-	-
Thiruvady et al.	2020	CS	min the sum of upper over- and under-assignments (see Bautista et al., 2008)	2	large neighborhood search	heuristic	-	-	-	-
Hottenrott et al.	2021	CS, robust against short-term sequence alterations	minimize the expected number of violations	2, colors	1) branch-and-bound for small instances, 2) a sampling-based adaptive large neighborhood search heuristic for large instances	1) exact algorithm 2) heuristic	lower bounds improved	-	-	-

Title		Problem formulation			Contribution					
Paper	Year	Problem type	Objective function	Options per station	Solution method	Algorithm type	Bounds improved	Comparison of CS and MMS	Sequencing rules creation	Instance space analysis
Sun et al.	2022	CS	minimize the sum of upper over- and under-assignments (see Bautista et al. 2008)	2	adaptive large neighborhood search, MIP with lazy constraints solved with Gurobi	1) heuristic 2) exact algorithm	-	-	-	X
Louis et al.	2023	CS, industrial CS	minimize the number of violations	2 or multiple	-	-	-	X CS is worse	-	-

Trends	Future research
Modifications of CS	Incorporating uncertainty (e. g. robust CS)
Multiple options: the early 2010-s, then less interest	Revisiting the topic
Case studies in automotive industry	Applications in other industries
Development of well-performing algorithms (e. g. ROADEF'05)	Focus on other aspects
CS vs. MMS – MMS is better	Deployment of MMS in companies: cases
Sequencing rules generation – popularity in the early 2010-s, then less interest	Revisiting the topic
Instance space analysis	Further features of hard instances, new benchmark instances, improvement of existing algorithms

- Google Scholar and SCOPUS databases
- Keywords “mixed-model assembly”, “sequencing”, “case study”, excluding keywords “car”, “automotive”, “truck”, “motorbike”
- No restriction on journals and paper ratings







- Boiler manufacturing (Hwang and Katayama, 2010): E. g. various fan seals, fan motors, burners, air conditioners, etc.
- Food processing (Savsar et al., 2017): E. g. a salad line with different core and additional ingredients
- GPU cards (Wang et al., 2023)
- Hydraulic pumps (Rauf et al., 2020): E. g. different valves, levers
- Industrial air-dryers (Faccio et al., 2016)
- Industrial machines manufacturing (Rabbani et al., 2015)





- Off-Highways systems manufacturing (Tiacci and Mimmi, 2018): E. g. the presence/absence of the Power Take Off (PTO) and/or quick couplers
- Plastic bag manufacturing (Mamun et al., 2012): E. g. presence/absence of different prints, various U-panels, etc.
- Turbocharger assembly (Yadav et al., 2020)
- Wooden furniture (Nouri and Abdul-Nour, 2019): E. g. presence/absence of reclining sofa backs, cabinet handles, different colors, etc.



- Sequencing is the task of defining the optimal job orders to minimize costs and work overload
- Mixed-model and car sequencing are the two common methods
- Among all sequencing rules, unique sequencing ratio per station delivered optimal results
- Methodology of searching papers was proposed
- Literature was classified by problem formulation and contribution
- Literature trends and future research directions were identified
- Industries where sequencing can be applied were identified



*Thank you! Any questions?*

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