

```
> with(DETools);with(plots);
```

```
[AreSimilar, Closure, DENormal, DEplot, DEplot3d, DEplot_polygon, DFactor,
DFactorLCLM, DFactorsols, Dchangevar, Desingularize, FunctionDecomposition, GCRD,
Gosper, Heunsols, Homomorphisms, IVPsol, IsHyperexponential, LCLM, MeijerGsols,
MultiplicativeDecomposition, ODEInvariants, PDEchangecoords, PolynomialNormalForm,
RationalCanonicalForm, ReduceHyperexp, RiemannPsols, Xchange, Xcommutator, Xgauge,
Zeilberger, abelsol, adjoint, autonomous, bernoullisol, buildsol, buildsym, canoni, caseplot,
casesplit, checkrank, chinisol, clairautsol, constcoeffsols, convertAlg, convertsys,
dalembertsol, dcoeffs, de2diffop, dfieldplot, diff_table, diffop2de, dperiodic_sols, dpolyform,
dsubs, eigenring, endomorphism_charpoly, equinv, eta_k, eulersols, exactsol, expsols,
exterior_power, firint, firtest, formal_sol, gen_exp, generate_ic, genhomosol, gensys,
hamilton_eqs, hypergeomsols, hyperode, indicialeq, infgen, initialdata, integrate_sols,
intfactor, invariants, kovacicols, leftdivision, liesol, line_int, linearsol, matrixDE,
matrix_riccati, maxdimsystems, moser_reduce, muchange, mult, mutest, newton_polygon,
normalG2, ode_int_y, ode_y1, odeadvisor, odepde, parametricsol, particularsol,
phaseportrait, poincare, polysols, power_equivalent, rational_equivalent, ratsols, redode,
reduceOrder, reduce_order, regular_parts, regularsp, remove_RootOf, riccati_system,
riccatisol, rifread, rifsimp, rightdivision, rtaylor, separablesol, singularities, solve_group,
super_reduce, symgen, symmetric_power, symmetric_product, symtest, transinv, translate,
untranslate, varparam, zoom]
```

```
[animate, animate3d, animatecurve, arrow, changecoords, complexplot, complexplot3d,
conformal, conformal3d, contourplot, contourplot3d, coordplot, coordplot3d, densityplot,
display, dualaxisplot, fieldplot, fieldplot3d, gradplot, gradplot3d, implicitplot,
implicitplot3d, inequal, interactive, interactiveparams, intersectplot, listcontplot,
listcontplot3d, listdensityplot, listplot, listplot3d, loglogplot, logplot, matrixplot, multiple,
odeplot, pareto, plotcompare, pointplot, pointplot3d, polarplot, polygonplot, polygonplot3d,
polyhedra_supported, polyhedraplot, rootlocus, semilogplot, setcolors, setoptions,
setoptions3d, spacecurve, sparsematrixplot, surfdata, textplot, textplot3d, tubeplot]
```

(1)

```
> ec:=diff(y(x),x)=1/cos(x)-y(x)*tan(x);#ex1
```

$$ec := \frac{d}{dx} y(x) = \frac{1}{\cos(x)} - y(x) \tan(x)$$

(2)

```
> sol:=dsolve(ec,y(x));
```

$$sol := y(x) = \cos(x) \tan(x) + \cos(x) _C1$$

(3)

```
> cond:=y(Pi)=1;
```

$$cond := y(\pi) = 1$$

(4)

```
> sol2:=dsolve({ec,cond},y(x));
```

$$sol2 := y(x) = \cos(x) \tan(x) - \cos(x)$$

(5)

```
> ec2:=(1+x^2)*diff(y(x),x,x)+4*x*diff(y(x),x)+2*y(x)-sin(x)=0;#ex2
```

$$ec2 := (1 + x^2) \left(\frac{d^2}{dx^2} y(x) \right) + 4x \left(\frac{d}{dx} y(x) \right) + 2y(x) - \sin(x) = 0$$

(6)

```
> sol3:=dsolve(ec2,y(x));
```

$$sol3 := y(x) = \frac{C2}{1 + x^2} + \frac{C1 x}{1 + x^2} - \frac{\sin(x)}{1 + x^2}$$

(7)

```
> cond:=y(0)=3, D(y)(0)=2;
```

$$cond := y(0) = 3, D(y)(0) = 2$$

(8)

```
> sol4:=dsolve({ec2,cond}, y(x));
```

$$sol4 := y(x) = \frac{3}{1+x^2} + \frac{3x}{1+x^2} - \frac{\sin(x)}{1+x^2}$$

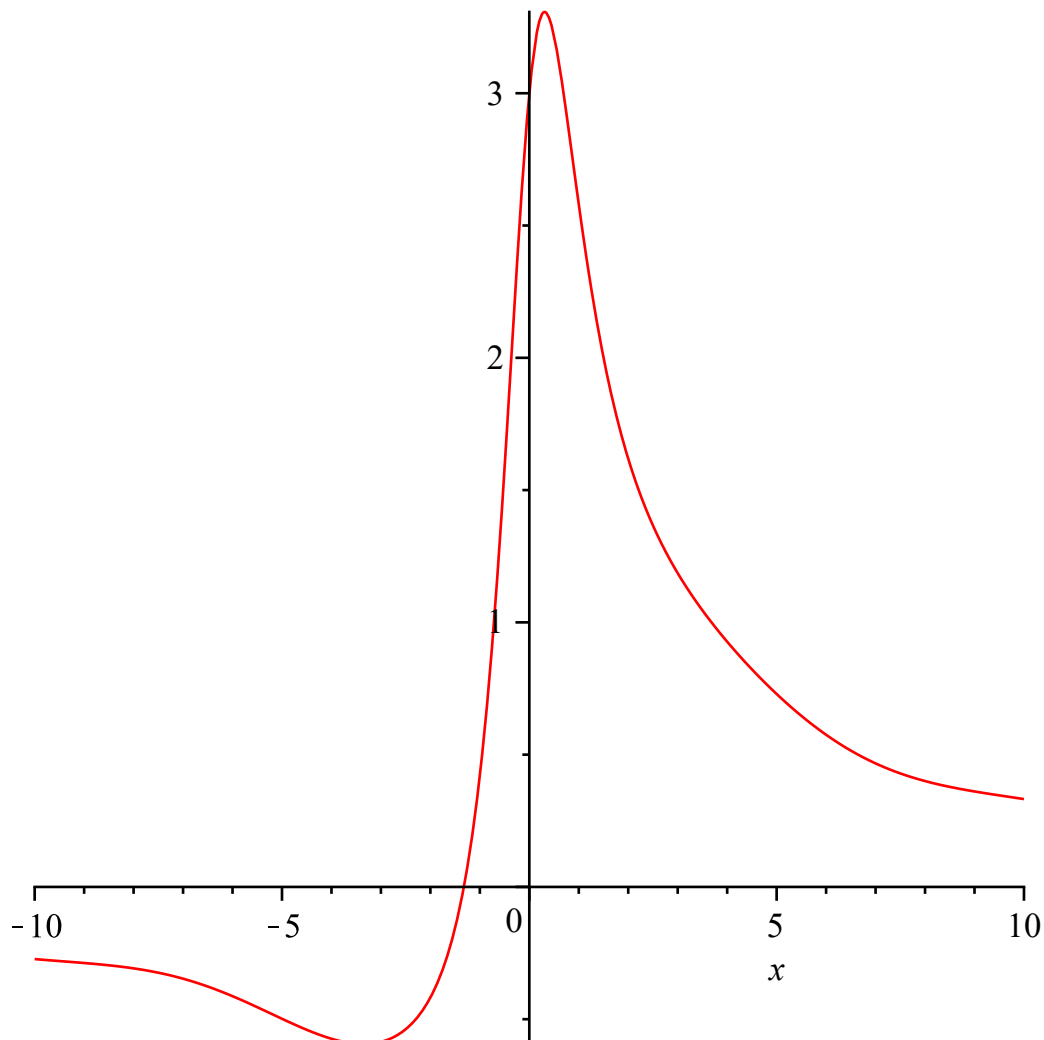
(9)

```
> ap:=unapply(rhs(sol4), x);
```

$$ap := x \rightarrow \frac{3}{1+x^2} + \frac{3x}{1+x^2} - \frac{\sin(x)}{1+x^2}$$

(10)

```
> plot(ap(x), x=-10..10);
```



```
> ec1:=diff(x(t), t)=x(t); #ex3
```

$$ec1 := \frac{d}{dt} x(t) = x(t)$$

(11)

```
> ec2:=diff(y(t), t)=x(t)+2*y(t);
```

$$ec2 := \frac{d}{dt} y(t) = x(t) + 2y(t)$$

(12)

```
> sist:=ec1, ec2;
```

$$sist := \frac{d}{dt} x(t) = x(t), \frac{d}{dt} y(t) = x(t) + 2y(t)$$

(13)

```
> sol:=dsolve({sist},{x(t),y(t)});
```

$$sol := \{x(t) = _C2 e^t, y(t) = -_C2 e^t + e^{2t} _C1\}$$
(14)

```
> cond:=x(0)=1,y(0)=4;
```

$$cond := x(0) = 1, y(0) = 4$$
(15)

```
> sol2:=dsolve({sist,cond},{x(t),y(t)});
```

$$sol2 := \{x(t) = e^t, y(t) = -e^t + 5 e^{2t}\}$$
(16)

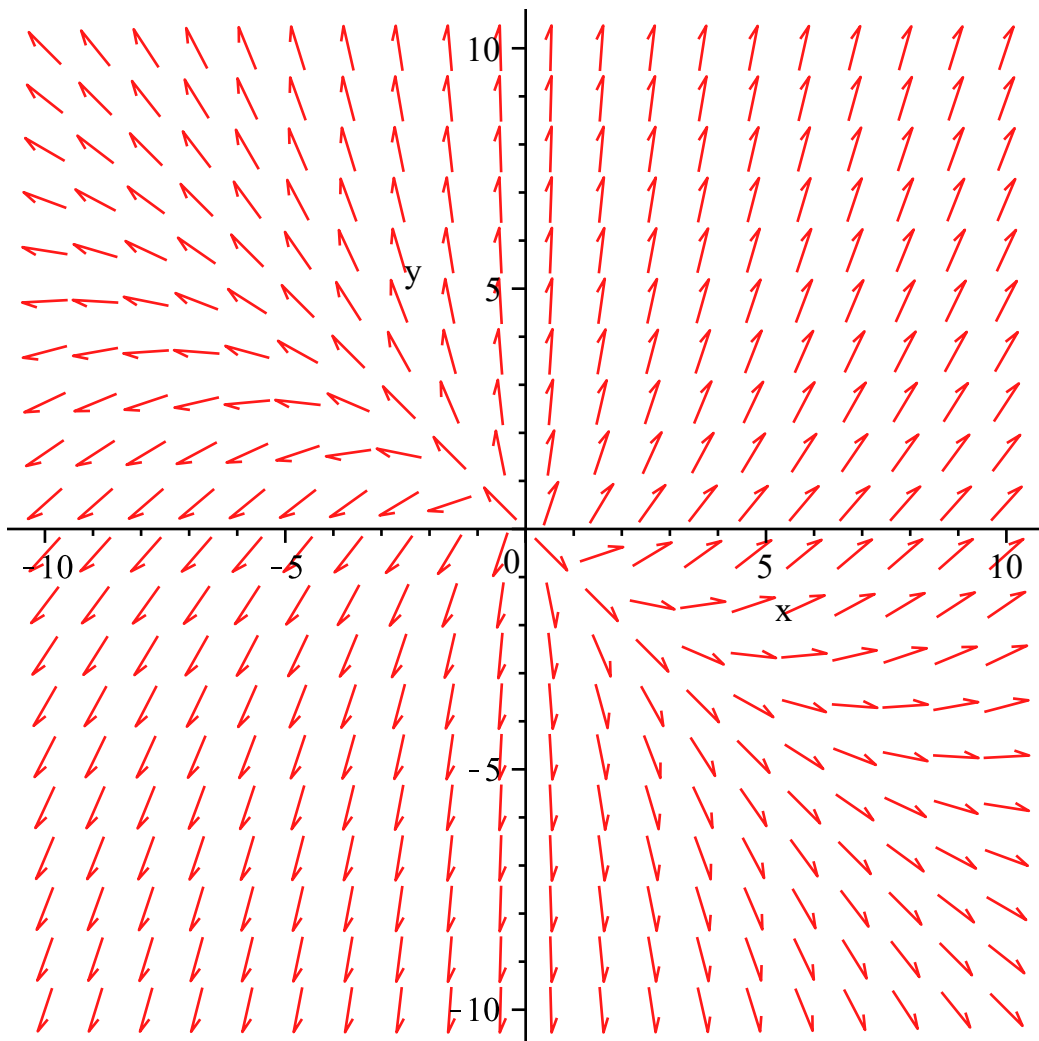
```
> #(0,0) e solutie pentru ambele functii => punct de echilibru
```

$$\frac{d}{dt} x(t)$$
(17)

```
> #pentru functia de x este puncti instabil, solutia derivatei cu 0  
da pozitiv
```

```
> #pentru functia de y este stabila, da negativ
```

```
> DEplot([sist], {x(t),y(t)}, t=-10..10, x=-10..10,y=-10..10);
```



```
> #nu deoarece se observa ca ssagetile ies din 0, insemnand ca  
functia tinde ori la -inf ori la +inf
```

$$\begin{aligned} &> \text{ec} := \text{diff}(N(t), t) = k * N(t); \# \text{ex4} \\ &ec := \frac{d}{dt} N(t) = k N(t) \end{aligned} \quad (18)$$

$$\begin{aligned} &> \text{cond} := N(0) = \text{nz}; \\ &cond := N(0) = \text{nz} \end{aligned} \quad (19)$$

$$\begin{aligned} &> \text{nz} := 500; \\ &\text{nz} := 500 \end{aligned} \quad (20)$$

$$\begin{aligned} &> k := 2.5; \\ &k := 2.5 \end{aligned} \quad (21)$$

$$\begin{aligned} &> \text{sol} := \text{dsolve}(\{\text{ec}, \text{cond}\}, N(t)); \\ &\text{sol} := N(t) = 500 e^{\frac{5}{2} t} \end{aligned} \quad (22)$$

$$\begin{aligned} &> k := 1.5; \\ &k := 1.5 \end{aligned} \quad (23)$$

$$\begin{aligned} &> \text{nz} := 10; \\ &\text{nz} := 10 \end{aligned} \quad (24)$$

$$\begin{aligned} &> \# \text{atunci } N(t) = 20 \text{ populatia curenta este dublata} \\ &> \text{sol2} := \text{dsolve}(\{\text{ec}, \text{cond}\}, N(t)); \\ &\text{sol2} := N(t) = 10 e^{\frac{3}{2} t} \end{aligned} \quad (25)$$

$$\begin{aligned} &> t := \text{solve}(\text{rhs}(\text{sol2}) = 20, t); \\ &t := \frac{2}{3} \ln(2) \end{aligned} \quad (26)$$

$$\begin{aligned} &> t := 't'; \# \text{ex5} \\ &t := t \end{aligned} \quad (27)$$

$$\begin{aligned} &> f1 := (x, y) \rightarrow y * x^2 + x * y^2; \\ &f1 := (x, y) \rightarrow y x^2 + x y^2 \end{aligned} \quad (28)$$

$$\begin{aligned} &> f2 := (x, y) \rightarrow x - y^2 - x * y + 1; \\ &f2 := (x, y) \rightarrow x - y^2 - x y + 1 \end{aligned} \quad (29)$$

$$\begin{aligned} &> \text{ec1} := \text{diff}(x(t), t) = f1(x(t), y(t)); \\ &ec1 := \frac{d}{dt} x(t) = y(t) x(t)^2 + x(t) y(t)^2 \end{aligned} \quad (30)$$

$$\begin{aligned} &> \text{ec2} := \text{diff}(y(t), t) = f2(x(t), y(t)); \\ &ec2 := \frac{d}{dt} y(t) = x(t) - y(t)^2 - x(t) y(t) + 1 \end{aligned} \quad (31)$$

$$\begin{aligned} &> \text{sist} := \text{ec1}, \text{ec2}; \\ &\text{sist} := \frac{d}{dt} x(t) = y(t) x(t)^2 + x(t) y(t)^2, \frac{d}{dt} y(t) = x(t) - y(t)^2 - x(t) y(t) + 1 \end{aligned} \quad (32)$$

$$\begin{aligned} &> p := \text{solve}(\{f1(x, y) = 0, f2(x, y) = 0\}, \{x, y\}); \\ &p := \{x = -1, y = 0\}, \{x = 0, y = 1\}, \{x = 0, y = -1\}, \{x = -1, y = 1\} \end{aligned} \quad (33)$$

$$\begin{aligned} &> \text{with}(\text{linalg}); \\ &[\text{BlockDiagonal}, \text{GramSchmidt}, \text{JordanBlock}, \text{LUdecomp}, \text{QRdecomp}, \text{Wronskian}, \text{addcol}, \\ &\text{addrow}, \text{adj}, \text{adjoint}, \text{angle}, \text{augment}, \text{backsub}, \text{band}, \text{basis}, \text{bezout}, \text{blockmatrix}, \text{charmat}, \end{aligned} \quad (34)$$

charpoly, cholesky, col, coldim, colspace, colspan, companion, concat, cond, copyinto, crossprod, curl, definite, delcols, delrows, det, diag, diverge, dotprod, eigenvals, eigenvalues, eigenvectors, eigenvects, entermatrix, equal, exponential, extend, ffgausselim, fibonacci, forwardsub, frobenius, gausselim, gaussjordan, geneqns, genmatrix, grad, hadamard, hermite, hessian, hilbert, htranspose, ihermite, indexfunc, innerprod, intbasis, inverse, ismith, issimilar, iszero, jacobian, jordan, kernel, laplacian, leastsqrs, linsolve, matadd, matrix, minor, minpoly, mulcol, mulrow, multiply, norm, normalize, nullspace, orthog, permanent, pivot, potential, randmatrix, randvector, rank, ratform, row, rowdim, rowspace, rowspan, rref, scalarmul, singularvals, smith, stackmatrix, submatrix, subvector, sumbasis, swapcol, swaprow, sylveste, toeplitz, trace, transpose, vandermonde, vecpotent, vectdim, vector, wronskian]

```
> j:=jacobian([f1(x,y), f2(x,y)], [x,y]);
```

$$j := \begin{bmatrix} 2xy + y^2 & x^2 + 2xy \\ -y + 1 & -2y - x \end{bmatrix} \quad (35)$$

```
> A1:=subs(p[1,1],p[1,2], eval(j));
```

$$A1 := \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix} \quad (36)$$

```
> eigenvals(A1);
```

$$\frac{1}{2} + \frac{1}{2}\sqrt{5}, \frac{1}{2} - \frac{1}{2}\sqrt{5} \quad (37)$$

```
> #focus instabil
```

```
> A2:=subs(p[2,1],p[2,2], eval(j));
```

$$A2 := \begin{bmatrix} 1 & 0 \\ 0 & -2 \end{bmatrix} \quad (38)$$

```
> eigenvals(A2);
```

$$1, -2 \quad (39)$$

```
> #sa instabil
```

```
> A3:=subs(p[3,1],p[3,2], eval(j));
```

$$A3 := \begin{bmatrix} 1 & 0 \\ 2 & 2 \end{bmatrix} \quad (40)$$

```
> eigenvals(A3);
```

$$1, 2 \quad (41)$$

```
> #tip nod instabil
```

```
> A4:=subs(p[4,1],p[4,2], eval(j));
```

$$A4 := \begin{bmatrix} -1 & -1 \\ 0 & -1 \end{bmatrix} \quad (42)$$

```
> eigenvals(A4);
```

$$-1, -1 \quad (43)$$

```
> #tip nod stabil
```

```
> cond_in:= [x(0)=-2,y(0)=-2], [x(0)=0,y(0)=0], [x(0)=-0.75,y(0)=
```

```
-0.75], [x(0)=0,y(0)=1],[x(0)=2,y(0)=3],[x(0)=0.75,y(0)=1.75],[x
(0)=0,y(0)=-3],[x(0)=2,y(0)=-1],[x(0)=0.75,y(0)=-2.75],[x(0)=0,y
(0)=i]$i=1..5, [x(0)=0,y(0)=-i]$i=1..5, [x(0)=i,y(0)=0]$i=1..5,
[x(0)=-i,y(0)=0]$i=1..5;
```

```
cond_in := [x(0) = -2, y(0) = -2], [x(0) = 0, y(0) = 0], [x(0) = -0.75, y(0) = -0.75], [x(0) = 0, y(0) = 1], [x(0) = 2, y(0) = 3], [x(0) = 0.75, y(0) = 1.75], [x(0) = 0, y(0) = -3], [x(0) = 2, y(0) = -1], [x(0) = 0.75, y(0) = -2.75], [x(0) = 0, y(0) = 1], [x(0) = 0, y(0) = 2], [x(0) = 0, y(0) = 3], [x(0) = 0, y(0) = 4], [x(0) = 0, y(0) = 5], [x(0) = 0, y(0) = -1], [x(0) = 0, y(0) = -2], [x(0) = 0, y(0) = -3], [x(0) = 0, y(0) = -4], [x(0) = 0, y(0) = -5], [x(0) = 1, y(0) = 0], [x(0) = 2, y(0) = 0], [x(0) = 3, y(0) = 0], [x(0) = 4, y(0) = 0], [x(0) = 5, y(0) = 0], [x(0) = -1, y(0) = 0], [x(0) = -2, y(0) = 0], [x(0) = -3, y(0) = 0], [x(0) = -4, y(0) = 0], [x(0) = -5, y(0) = 0]
```

```
> DEplot([sist],[x(t),y(t)], t=-5..5,x=-6..6,y=-6..6, [cond_in],
arrows=medium,linecolor=blue);
```

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further right of .10419528, probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further right of .50368102, probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further right of .15555323, probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further right of .58322720, probably a singularity

cannot evaluate the solution further left of -.61184774, maxfun limit exceeded (see ?dsolve,maxfun for details)

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further left of -.20273255, probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further right of .20273255, probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further left of -.61588178, probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further left of -.35613782, probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further left of -.20422238, probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further right of .56235807,
probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further right of .35049695,
probably a singularity

Warning, plot may be incomplete, the following errors(s) were issued:

cannot evaluate the solution further right of .20363630,
probably a singularity

