FYS 2021 Assigment 1

A Study on Music Genre Classification using Logistic Regression

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Github repository: https://github.com/pettermad/FYS-2021-Machine-Learning/tree/ac93526806ee966c57759be05afa093a20bdf006/oblig%201

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from sklearn.metrics import confusion_matrix
```

Problem 1

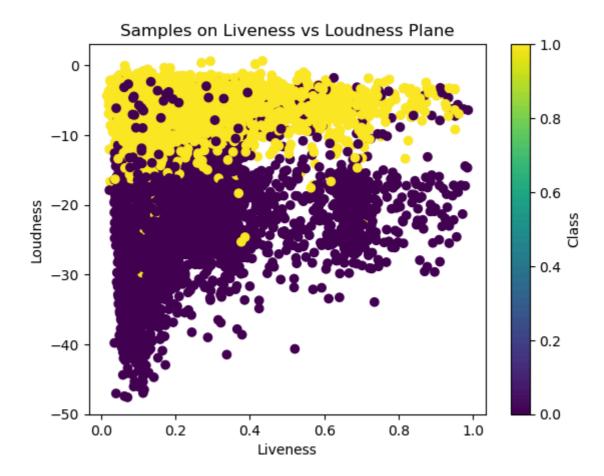
print(Y)

```
In [ ]: #1a
        SP = pd.read_csv("SpotifyFeatures.csv")
                                                                    # Reads .csv file
        #print(SP)
        print(f"Songs: {len(SP.axes[0])}, song properties {len(SP.axes[1])}") # Prints
        Songs: 232725, song properties 18
        a) There are 232725 samples with 18 features in the dataset.
        #1b
In [ ]:
        SP2 = pd.read_csv("SpotifyFeatures.csv",usecols = ["genre","liveness","loudness"])
        SP2 = SP2.loc[(SP2['genre'] == 'Pop') | (SP2['genre'] == 'Classical')] # Filters of
        SP2 = SP2.replace({'Pop':1, 'Classical':0})
                                                         # Renames Pop to value 1, and Cla
        len_classical = len(SP2.loc[SP2['genre'] == 0]) # Counts how many songs are classi
        len pop = len(SP2.loc[SP2['genre'] == 1])
        print(f"Classical songs: {len_classical}, Pop songs: {len_pop}")
        Classical songs: 9256, Pop songs: 9386
        b) There are 9256 classical songs, and 9386 pop songs.
In [ ]: # Create the input matrix
        X = SP2[['liveness', 'loudness']].values
        # Create the target vector
        Y = SP2['genre'].values
        print(X)
```

```
[[ 0.0762 -21.356 ]
         [ 0.106 -34.255 ]
         [ 0.0916 -28.215 ]
         [ 0.0816 -25.843 ]
         [ 0.105 -20.238 ]
         [ 0.0953 -29.223 ]]
        [0 0 0 ... 0 0 0]
In [ ]: # Split the data into training and test sets
        X_train, X_test, y_train, y_test = train_test_split(X, Y, test_size=0.2, shuffle=Tr
        #stratify makes sure that the training and test sets have the same proportion of cl
        print(X_train)
        print(y_train)
        [[ 0.101 -18.663 ]
         [ 0.211 -14.334 ]
         [ 0.0759 -18.204 ]
         [ 0.111 -7.213 ]
         [ 0.121 -21.863 ]
         [ 0.0521 -4.328 ]]
        [0 0 0 ... 1 0 1]
        c) The two generated arrays are looking like expected.
In [ ]: #1d
        plt.scatter(X[:, 0], X[:, 1], c=Y, cmap='viridis') # c is the color of the dots, cn
        plt.xlabel('Liveness')
        plt.ylabel('Loudness')
        plt.title('Samples on Liveness vs Loudness Plane')
        # Add a colorbar legend
```

plt.colorbar(label='Class')

plt.show()



d) We see from the plot that fair performing classification should be possible. Specially along the loudness axis there seem to be defined separation between the classes.

Problem 2

```
In [ ]: #2a
        # Define the logistic function
        def sigmoid(x):
            return 1 / (1 + np.exp(-x))
In [ ]: def logistic_regression(X, y, learning_rate, n_epochs):
            # Initialize the weights and bias
            n_features = X.shape[1]
            weights = np.zeros(n_features)
            bias = 0
            # Initialize lists to store training error and accuracy
            training_error = []
            training_accuracy = []
            # Iterate through each epoch
            for epoch in range(n_epochs):
                 # Iterate through each training sample
                for i in range(len(X)):
                    # Compute the predicted class probabilities
                    z = (X[i] @ weights) + bias
                    y_pred = sigmoid(z)
                    # Update the weights and bias using gradient descent
                    error = y_pred - y[i]
```

```
weights = weights - learning_rate * error * X[i]
bias = bias - learning_rate * error

# Calculate the training error and accuracy
y_pred = sigmoid((X @ weights) + bias)
training_error.append(np.mean(np.abs(y_pred - y)))
training_accuracy.append(np.mean((y_pred >= 0.5) == y))

return weights, bias, training_error, training_accuracy
```

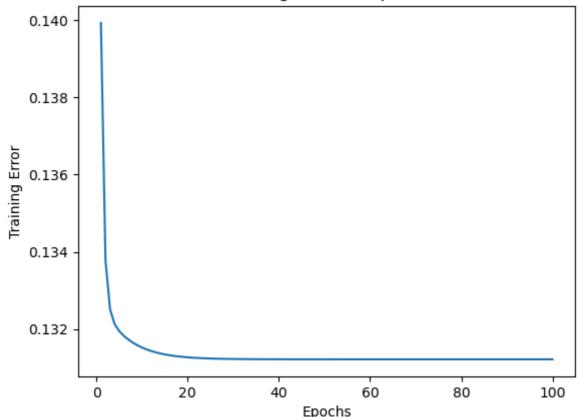
```
In []: # Set the Learning rate and number of epochs
    learning_rate = 0.01
    n_epochs = 100

# Train the Logistic regression classifier
    weights, bias, training_error, training_accuracy = logistic_regression(X_train, y_t

# Plot the training error as a function of epochs
    plt.plot(range(1, n_epochs+1), np.array(training_error))
    plt.xlabel('Epochs')
    plt.ylabel('Training Error')
    plt.title('Training Error vs. Epochs')
    plt.show()

print("weights =", weights)
    print("bias =", bias)
```

Training Error vs. Epochs



```
weights = [-1.65160436 0.53076298]
bias = 5.883908437897808
```

a) The training error is rapidly decreasing as number of epochs is increasing, as excepcted. At around 20 epochs the error seems to have stabilized.

```
In [ ]: accuracy = training_accuracy[-1]
    print('Accuracy on the training set:', accuracy)
```

Accuracy on the training set: 0.9183933480855629

This is an acceptable accuracy.

```
In [ ]: learning_rates = [0.001, 0.01, 0.1, 1.0] # Different Learning rates to try
        # Initialize empty lists to store training accuracies for each learning rate
        training_accuracies = []
        # Iterate through each learning rate
        for learning_rate in learning_rates:
            # Train the Logistic regression classifier
            weights, bias, training_error, training_accuracy = logistic_regression(X_train,
            # Append the training accuracy to the list
            training_accuracies.append(training_accuracy[-1])
        # Print the results
        for i in range(len(learning_rates)):
            print(f"Learning Rate: {learning_rates[i]}, Training Accuracy: {training_accura
        C:\Users\pette\AppData\Local\Temp\ipykernel_22828\3092525962.py:5: RuntimeWarning:
        overflow encountered in exp
          return 1 / (1 + np.exp(-x))
        Learning Rate: 0.001, Training Accuracy: 0.9224837390196473
        Learning Rate: 0.01, Training Accuracy: 0.9183933480855629
        Learning Rate: 0.1, Training Accuracy: 0.9152417353986455
        Learning Rate: 1.0, Training Accuracy: 0.9212096828270636
```

The difference in accuracy for the different learning rates are relatively small. The best accuracy is found with a learning rate of 0.001.

The training accuracy can vary for different learning rates because the learning rate determines the step size taken during the gradient descent optimization process.

When the learning rate is too small, the algorithm takes small steps towards the optimal solution. This can result in slow convergence and the model may require more epochs to reach a good accuracy. On the other hand, if the learning rate is too large, the algorithm may overshoot the optimal solution and fail to converge. This can lead to unstable training and lower accuracy.

```
# Calculate the predicted class probabilities for the test set
y_pred_test = sigmoid((X_test @ weights) + bias)

# Convert the predicted probabilities to binary predictions
y_pred_test_class = (y_pred_test >= 0.5).astype(int)

# Calculate the accuracy on the test set
accuracy_test = np.mean(y_pred_test_class == y_test)

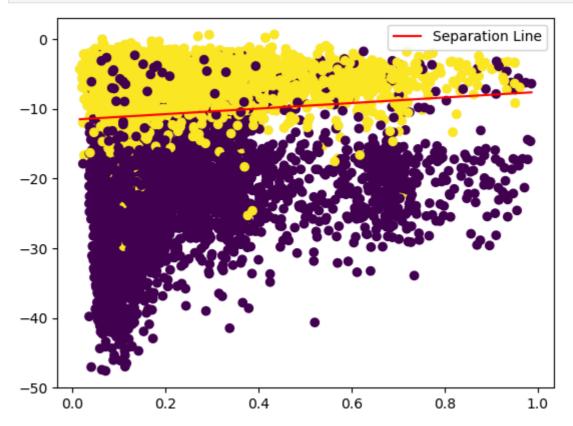
# Print the accuracy on the test set
print('Accuracy on the test set:', accuracy_test)
```

Accuracy on the test set: 0.9203539823008849

b) Accuracy on the test set is on par with the train set. So we are happy with our classifier.

If there is a significant difference between the accuracy on the training and test set can be attributed to a phenomenon called overfitting. Overfitting occurs when a machine learning model performs extremely well on the training data but fails to generalize well to new, unseen data.

```
In [ ]:
        #2c
        # Calculate the slope and y-intercept of the decision boundary line (ax+b)
        slope = -weights[0] / weights[1]
        intercept = -bias / weights[1]
        # Generate x values for the decision boundary line
        x_{values} = np.linspace(np.min(X[:, 0]), np.max(X[:, 0]), 100)
        # Calculate corresponding y values for the decision boundary line
        y_values = slope * x_values + intercept
        # Plot the decision boundary line
        plt.plot(x_values, y_values, color='red', linestyle='-', label='Separation Line')
        # Plot the data points
        plt.scatter(X[:, 0], X[:, 1], c=Y, cmap='viridis')
        # Add Legend to the plot
        plt.legend()
        # Show the plot
        plt.show()
```



c) The separation line make a good job of separating the classes. But as we see from the plot a linear line will not perfectly separate between the two classes. Perfect accuracy is not achievable here.

- b) The confusion matrix provides more detailed information about the performance of the classifier on the test set compared to the accuracy score. It yields the number of true positives, true negatives, false positives, and false negatives.
 - True Positives (TP): The number of positive instances correctly predicted as positive.
 - True Negatives (TN): The number of negative instances correctly predicted as negative.
 - False Positives (FP): The number of negative instances incorrectly predicted as positive.
 - False Negatives (FN): The number of positive instances incorrectly predicted as negative.

From these we can calculate both precision and recall. Precision measures the proportion of correctly predicted positive instances out of all instances predicted as positive, while recall measures the proportion of correctly predicted positive instances out of all actual positive instances.

These can also be used to calculate an F1 score. This is usefull when class distribution is uneven and you need a measure that takes both false positive and false negative into account.