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AI1110 assignment 2 ICSE 12 2017

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Question: 1(iii) prove that

$$\frac{1}{2}\cos^{-1}\left(\frac{1-x}{1+x}\right) = \tan^{-1}\sqrt{x}$$

Solution: let

$$x = tan^2(y)$$

$$\Rightarrow \frac{1}{2}\cos^{-1}\left(\frac{1-x}{1+x}\right)$$

$$\Rightarrow \frac{1}{2}\cos^{-1}\left(\frac{1-tan^2(y)}{1+tan^2(y)}\right)$$

$$\Rightarrow \frac{1}{2}\cos^{-1}(\cos 2y)$$

$$\Rightarrow \frac{1}{2}2y$$

$$\Rightarrow y$$

$$\Rightarrow tan^{-1}\sqrt{x}$$

$$\therefore \frac{1}{2}\cos^{-1}\left(\frac{1-x}{1+x}\right) = \tan^{-1}\sqrt{x}$$