

Transport Infrastructure and Spatial Sorting: Evidence from Buenos Aires

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- ▶ Cities spend a lot of money on new public transport infrastructure.
- ▶ Existing quantitative spatial models used to measure welfare gains are **static** → “immediate” response + spatial eq. (in expectation)
- ▶ However: residential and work mobility is costly → takes time.
- ▶ Accounting for these dynamics matters when evaluating effects of new transport infrastructure.
- ▶ **Research Questions:**
 - ▶ **How do improvements in the urban transport infrastructure affect the dynamics of spatial sorting?**
 - ▶ **Welfare consequences for high- and low- skilled residents when considering these dynamics?**

- ▶ Study effects of new BRT lines on (residential) spatial sorting in Buenos Aires, Argentina.
- ▶ Use novel individual-level panel data → track residents as they move.
 1. Reduced form analysis: causal impact of new transport infrastructure on sorting by skill-type.
 2. **Dynamic** QSM of a city. Explicitly model within-city migration (sorting).
 - ▶ Measure welfare gains for high- and low-skilled by initial place of residence.
 - ▶ Study spatial heterogeneity of welfare gains within city.
 - ▶ Evaluate importance of dynamic adjustment costs: difference in welfare between *static* model and *dynamic* model.

Preview of Main Findings (today)

- ▶ Similar **average** gains for high-skilled (college educated) and low-skilled ($\sim 1\%$).
- ▶ But conditioning on *initial location* (before BRT) matters for welfare gains.
- ▶ Pro-poor (**spatially**): residents starting in initially poorer neighborhoods see highest welfare gains.
- ▶ Accounting for *dynamic transition* reduces welfare gains by 35% for HS and 31% for LS residents on avg. (compared to “static-model-style” estimation).
- ▶ Large spatial heterogeneity in dynamic adjustment costs.

Setting

Buenos Aires 2011-2017 - New BRT System: Metrobus

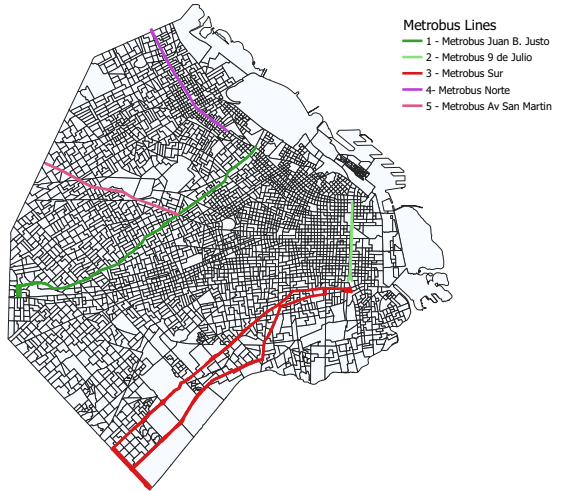
Bus Rapid Transit System (BRT):

- ▶ Bus-based public transport system
- ▶ **Dedicated bus lanes.**
- ▶ **Platform level boarding.**
- ▶ Ideally similar speed gains to subways but cheaper to build.

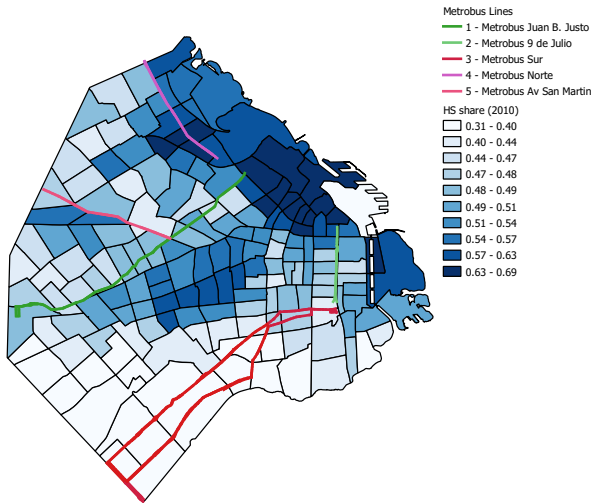


Buenos Aires 2011-2017 - New BRT System: Metrobus

- ▶ 2011: Juan B Justo
- ▶ 2013: 9 de Julio and Sur
- ▶ 2015: Norte
- ▶ 2016: San Martin
- ▶ \uparrow speed of buses $\approx 30\%$ on average.
- ▶ For average commute time
 \Rightarrow 110 hours saved in a year.



High-Skill Share in 2010 and Metrobus Lines



- ▶ Election registers for 2011, 2013, 2015, and 2017. Contains all citizens of voting age ($>2.5m$). Includes: *National ID number*, *address*, and *occupation*. → Track intra-city migration, update population every 2 years. [Description](#)
- ▶ Annual Household Survey (2010-2018) for the City of Buenos Aires → employment population by skill level.
- ▶ Commuting Survey for the city in 2010.
- ▶ Housing prices from online listings.
- ▶ Census data from 2010.

A Dynamic Quantitative Spatial Model of a City

- ▶ Combines:
 - ▶ *migration/dynamics* from Caliendo, et al. (2019) and Artuç et al. (2010) with
 - ▶ *commuting* from Ahlfeldt, et al. (2015)
- ▶ Closed city: I residence locations and J work locations.
- ▶ Two types of infinitely lived residents/workers: high-skilled and low-skilled.
- ▶ Two types of goods: housing and consumption good. Cobb-Douglas preferences.
- ▶ Assume rational expectations.

Model in a Nutshell

- ▶ Consumers/Workers are forward looking and choose where to work and live each period taking into account:
 - ▶ Commute costs
 - ▶ Wages
 - ▶ Moving/migration costs
 - ▶ Housing prices (rents)
 - ▶ Idiosyncratic shocks for residential location and workplace location.
- ▶ **Goods market:** Armington-style production using mix of high- and low-skilled labor.
- ▶ **Labor market:** labor demand depends on commuting costs and pop. distribution. Wages adjust to clear market.
- ▶ **Housing market:** Housing supply is fixed. Housing prices adjust every period to clear market.

Resident's Problem - Static Problem

- ▶ Cobb-Douglas on consumption (c_i^g) and floor space ($H_{R,ij}^g$).
- ▶ Income is effective wages ($w_j^g \varepsilon_j^g$) discounted by commute costs $d_{ij} = \exp(\kappa \tau_{ij})$.

$$\max_{\{c_i^g, H_{R,ij}^g\}} C_{ij}^g = \left(\frac{c_{ij}^g}{\alpha} \right)^\alpha \left(\frac{H_{R,ij}^g}{1-\alpha} \right)^{1-\alpha}$$

$$\text{subject to } c_{ij}^g + r_{Ri} H_{R,ij}^g = \frac{w_j^g \varepsilon_j^g}{d_{ij}}.$$

$$\Rightarrow C_{ij}^{g*} = \frac{w_j^g \varepsilon_j^g r_{Ri}^{\alpha-1}}{d_{ij}}.$$

Resident's Problem - Dynamic Problem

$$v_{n,t}^g = \max_{\{i,j\}} \left\{ \overbrace{C_{nj,t}^{g*}}^{\text{flow utility}} + \underbrace{\beta E_t[v_{i,t+1}^g]}_{\text{cont. value}} - \overbrace{\mu_{ni}^g}^{\text{mig. cost}} + \underbrace{\eta_{i,t}^g}_{\text{id. res. shock}} \right\}$$

Taking expectations w. r. t. the joint distribution of ε_j and η_i ,

$$V_{n,t}^g = \tilde{T}_g \Phi_{Rgn,t}^{\frac{1}{\theta_g}} r_{Rn}^{\alpha-1} + \nu_g \ln \sum_{i=1}^I \exp \left(\beta V_{i,t+1}^g - \mu_{i,n}^g \right)^{\frac{1}{\nu_g}}. \quad (1)$$

Where

$$\overbrace{\Phi_{Rgn,t}}^{\text{CMA}} = \sum_j \left(\frac{w_{j,t}^g}{d_{nj,t}} \right)^{\theta_g},$$

Transition Dynamics After New Transport Infrastructure

- ▶ Change in transport network \rightarrow commute times ($d_{ij,t}$).
- ▶ Impacts spatial dist. of expected utility ($V_{i,t}^g$).
- ▶ But adjustment in residential pop. is gradual:
- ▶ **Residents wait for a large enough idiosyncratic shock ($\eta_{i,t}^g$) to pay moving cost μ_{ni}^g to move to i .**
- ▶ \rightarrow Gradual changes in location characteristics and transition to SS.

- ▶ From Caliendo et al. (2019) → equilibrium in **first differences**. Extend dynamic exact-hat algebra to incorporate commuting.
- ▶ **Crucially**: use electoral register data to calculate residential migration matrices every two years (as well as migration elasticities).
- ▶ Calculate transport cost at time 0, $(d_{ij,0})$ (pre-BRT), add lines at times 1, 2 and 3, and calculate $d_{ij,t}$ for each period (2 years), then assume $d_{ij,t} = d_{ij,3}$ for all $t \geq 4$.

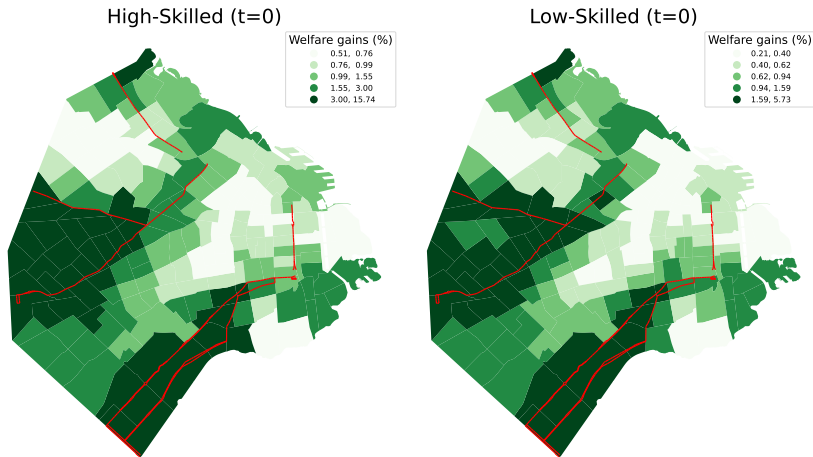
Estimation of model parameters

Welfare Gains for Residents at $t = 0$

- ▶ $V_{i,t}^g \rightarrow$ expected utility at time t in location i for resident of skill type g .
- ▶ $\hat{V}_{i,t}^g \rightarrow$ expected utility **without BRT**.
- ▶ Define $\delta_{n,t}^g$ as *consumption equivalent* compensating variation paid each period so that utility under counterfactual $\hat{V}_{i,t}^g$ (plus $\delta_{n,t}^g$) is equal to utility with new transport infrastructure ($V_{i,t}^g$).
- ▶ $\delta_{n,0}^g$ captures welfare gains for resident of skill level g living in n at time $t = 0$.

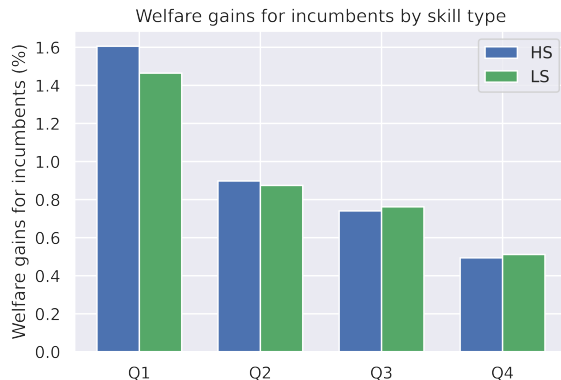
Welfare Gains: History Matters

Initial location (before BRT) matters for gains from new infrastructure.



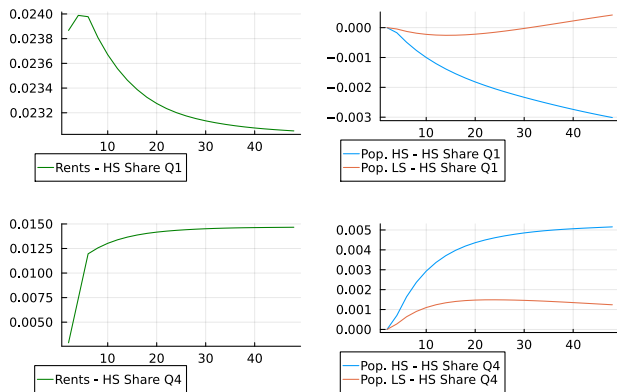
Welfare Gains for Incumbents By Quartile of HS share

- ▶ Avg. Welfare gains at $t = 0$ for locations < 1 km from line.
- ▶ On avg. welfare increased more in locations with lower initial HS share.
- ▶ BRT spatially “pro-poor” neighborhoods.



Short-run vs Long-Run: Dynamic Transitions Vary by Location

Evolution of housing prices (rents) and population relative to counterfactual (no BRT).



Location characteristics (rents, residential pop., etc.) adjust at different speeds and in different ways across locations.

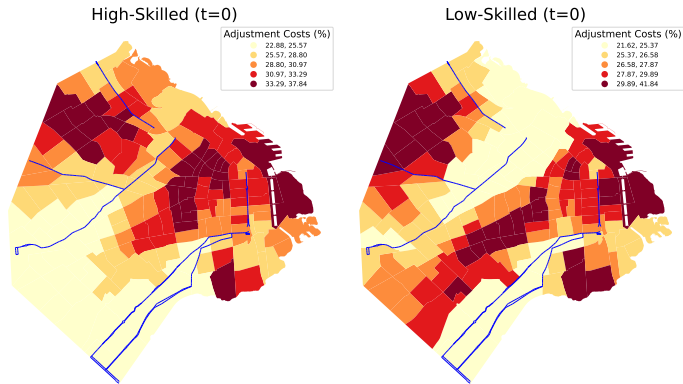
- ▶ Construct measure of adjustment cost that follows Davidson et al. (2010).

$$AC_{n,t}^g = \log \left(\frac{\delta_{n,SS}^g}{\delta_{n,t}^g} \right). \quad (2)$$

- ▶ Where $\delta_{n,t}^g$ is CD at time t , and $\delta_{n,SS}^g$ is the consumption equivalent compensating differential calculated starting from the steady state.
- ▶ **Intuition:** How much higher (or lower) would welfare be in location n if you could “jump” to new SS (as in static QSM models).

Dynamic Adjustment Costs at $t=0$

Larger AC further away from new BRT, where indirect gains require population changes.



Avg. $AC_h = 35\%$, Avg. $AC_l = 31\%$.

- ▶ Existing **static** models (Heblich et al. 2020; Tsivanidis, 2023; Severen 2023; etc.) assume: **spatial eq.** + “**jump to SS**”.
- ▶ Accounting for dynamics matters because:
 - ▶ **Initial exposure matters**: large spatial heterogeneity in welfare gains conditional on initial location.
 - ▶ **Dynamic transition matter**: not accounting for transition overestimates gains by 35% for HS and 31% for LS residents.
 - ▶ Large spatial heterogeneity in dynamic adjustment costs.

Thank you!

Appendix

Neighborhood Migration Flows and Residential Population

$m_{in,t}$: fraction of agents that are residing in location n at the beginning of period t , and move to location i by the end of period t . From distribution of idiosyncratic preferences $\eta_{n,t}$ we obtain:

$$m_{in,t}^g = \frac{\left[\exp(\beta V_{i,t+1}^g - \mu_{in}^g) \right]^{\frac{1}{\nu_g}}}{\sum_{m=1}^N \left[\exp(\beta V_{m,t+1}^g - \mu_{mn}^g) \right]^{\frac{1}{\nu_g}}} \quad (3)$$

It follows that:

$$L_{Ri,t}^g = \sum_{n=1}^I \underbrace{m_{in,t}^g L_{Rn,t-1}^g}_{\text{Num. movers } n \text{ to } i} \quad (4)$$

Given idiosyncratic productivity shocks ε_j^g , the probability that a worker that lives in i at time t decides to work in location j is:

$$\Pi_{j|tig} = \frac{(w_{j,t}^g/d_{ij,t})^{\theta_g}}{\sum_s \left(\frac{w_{s,t}^g}{d_{is,t}}\right)^{\theta_g}} = \frac{(w_{j,t}^g/d_{ij,t})^{\theta_g}}{\Phi_{Rgi,t}}. \quad (5)$$

Therefore, labor supply at time t for workplace location j will be

$$L_{Fj,t}^g = \sum_{i=1}^I \Pi_{j|tig} L_{Ri,t}^g, \quad (6)$$

Equilibrium Definitions

- ▶ Given $\{L_{Ri,t}^g\}$ and $\{d_{ij,t}\}$ at time t , and $\{A_j\}$, a **temporary equilibrium**: as a vector of wages $\{w_j^g\}$ and floorspace prices $\{r_{Ri}\}$ that solve labor market clearing and floorspace market clearing at time t .
- ▶ Given $L_{R0}^g, L_{F0}^g, \{m_{in,0}^g\}$ and $\{d_{ij,t}\}$, **sequential competitive equilibrium**: sequence of $\{L_{Rt}^g, L_{Ft}^g, m_t^g, w_t^g, r_{Rt}, V_t^g\}_{t=0}^\infty$ that solves residents' dynamic optimization problem, and temporary equilibrium at each time t .
- ▶ **Stationary equilibrium**: sequential competitive equilibrium such that all the elements of the vector $\{L_{Rt}^g, L_{Ft}^g, m_t^g, w_t^g, r_{Rt}, V_t^g\}_{t=0}^\infty$ are constant for all t .

Labor Market clearing

Housing Market clearing

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Parameter Estimation

Parameters	Values	Source
Commute cost parameter	$\kappa = 0.01$	From Ahlfeldt et al. (2015)
Discount factor	$\beta = 0.92$	Based on Caliendo et al. (2019)
Non-housing consump. share	$\alpha = 0.7$	From hh. consumption survey 2010
Semi-elast. of commuting	$\theta_h = 3.7, \theta_l = 4.7$	Estimated as in Ahlfeldt et al. (2015) using commuting survey data
Inverse migration elast.	$\nu_h = 1.4, \nu_l = 1.8$	Estimated with intra-city migration data (following Artuç et al. 2010)

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- ▶ Consumers/workers consume **consumption good** and **housing** (floorspace). They:
- ▶ Start period in residence location i .
- ▶ Observe idiosyncratic match productivities for each workplace location j (ε_j^g , Frechet).
- ▶ Choose a workplace location j to maximize wage income discounted by **commuting costs**. → **Labor supply**.
- ▶ Consume housing and consumption good. → **Housing demand and consumption demand**.
- ▶ Observe idiosyncratic preference shocks for each residence location next period (η_n^g , Gumbel).
- ▶ Choose residential location for next period. → **Migration probabilities**.

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- ▶ J varieties of the consumption good, differentiated by location of production, and supplied in a competitive market.
- ▶ Consumers have CES preferences over each variety, with elasticity of substitution $\sigma > 1$.
- ▶ Firms solve static problem.
- ▶ Production function \rightarrow Cobb-Douglas combines high- and low-skilled labor.
- ▶ Using all these assumptions, determine effective **labor demand** by skill as function of wage vector $\mathbf{w}_t = \{\{\mathbf{w}_{jt}^h\}_{j=1}^J, \{\mathbf{w}_{jt}^l\}_{j=1}^J\}$.

- ▶ Fixed supply of housing (floorspace).
- ▶ Demand for floorspace by skill group comes from FOC of consumer problem.
- ▶ As population moves around, demand for housing changes \Rightarrow change in housing prices.

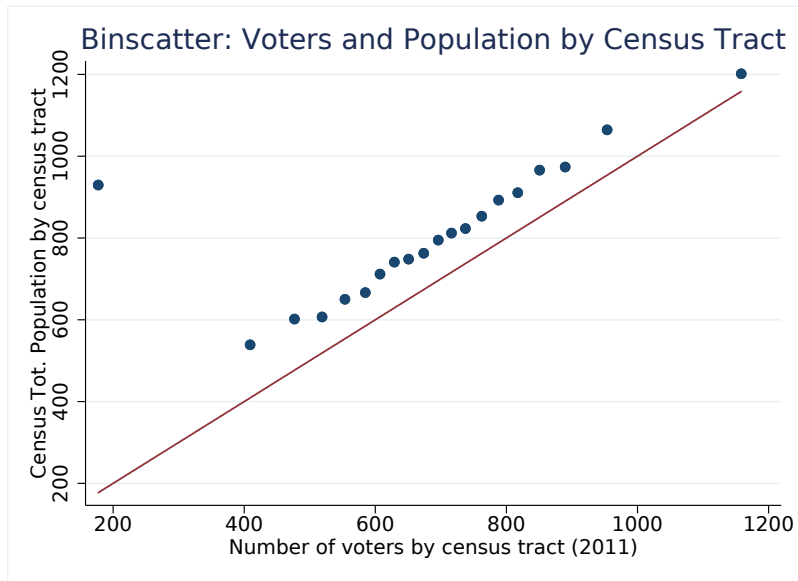
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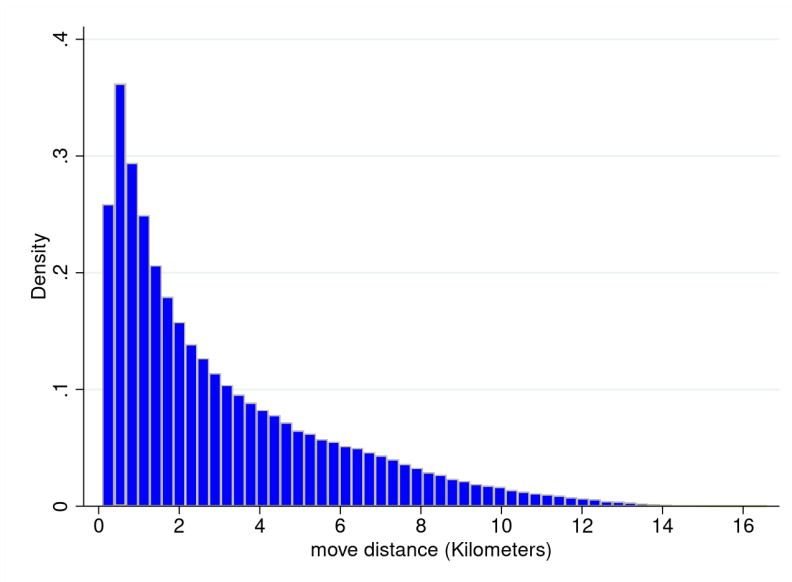
Floorspace Prices in 2010 and Metrobus Lines

metrobus_lines_and_floorspace_prices_0_with_arrow.pdf

Electoral Register Data

- ▶ Voting is compulsory for all Argentine citizens between 18 and 70.
- ▶ Your polling place is decided based on your residence.
- ▶ So the government keeps an “up to date” record of every person’s address, which it updates for each election.
- ▶ I have electoral registry for the entire country for 2011, 2013, 2015, and 2017.
- ▶ Includes: National ID number, name, sex at birth, birth year, *address* as free text, and *occupation* as free text.
- ▶ Cleaned and geotagged (assigned GPS coordinates) for almost all addresses in the city of Buenos Aires (aprox. 2.5 million people).
- ▶ Residence changes are self-reported. This might imply under-reporting of changes in residence.





ISCO 1 Digit Classification

1	Managers	
2	Professionals	
3	Technicians and associate professionals	High-Skilled
4	Clerical support workers	
6	Skilled agricultural, forestry and fishery workers	
5	Service and sales workers	
7	Craft and related trades workers	
8	Plant and machine operators, and assemblers	Low-Skilled
9	Elementary occupations	
0	Armed forces occupations	

hs_by_occupation.pdf

High-skill Share by Census Tract: Census vs Constructed Measure

census_tract_hs_plot.pdf

CMA_1_0.pdf

Δ CMA for Low-Skilled 2011-2017

change_CMA_1_8_census_tracts.pdf

- ▶ Classify occupation descriptions using International Standard Classification of Occupations. [Classification](#)
- ▶ Divide Occupations by share of college educated workers into high-skilled and low-skilled: [Graph](#)
- ▶ Assign each person in electoral registry to high-skill/low-skill according to coded occupation.

[Comparison with Census Data](#)

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Definition of Commuter Market Access (CMA)

$$CMA_{gn,t} = \sum_j \left(\frac{w_{j,t}^g}{d_{nj,t}} \right)^{\theta_g}$$

- ▶ g : High-Skilled (h) or Low-Skilled (l).
- ▶ n : residential location.
- ▶ j : workplace location.
- ▶ Commute costs: $d_{nj,t} = \exp(\kappa\tau_{ij})$, with τ_{ij} being commute time from i to j .
- ▶ $w_{j,t}^g$: model-consistent wages for type g at time t , calculated with residential and employment population.
- ▶ θ_g : semi-elasticity of commute shares with respect to commute times for skill type g .

CMA for High-Skilled in 2011

Pre BRT: market access higher near subway lines and near Central Business District (CBD).

CMA_h_0.pdf

Δ CMA for High-Skilled 2011-2017

Δ CMA larger near new BRT lines and further from Central Business District (CBD).

change_CMA_h_0_census_tracts.pdf

Identification: Historical IV

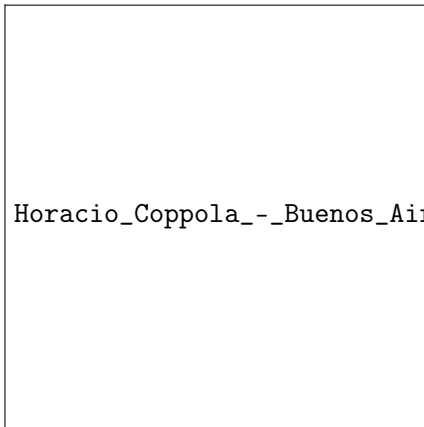
- ▶ Large tramway system dismantled in 1963.
- ▶ Buses competed directly with trams, and kept same routes.
- ▶ Metrobus lines follow existing bus routes along large two-way avenues.
- ▶ Use subset of tramway system built by 1938 that ran through two-way avenues to instrument for placement of Metrobus lines.
- ▶ IV: predicted Δ CMA if BRT placement followed tramway lines. [Details](#)
- ▶ Identifying assumption: placement decided before 1938 of tramway not correlated with contemporary changes in unobservables.

[Photo](#)[Map](#)[Back](#)

Tramway in 1938 and Metrobus System

tramway_lines_and_metrobus.pdf

Tramway and Buses Competing in 1936



Horacio_Coppola_-_Buenos_Aires_1936_-_Sarmiento_y_Diag

$$CMA_{gn,t} = \sum_j \left(\frac{w_{j,t}^g}{d_{nj,t}} \right)^{\theta_g}$$

- ▶ $d_{nj,t} = \exp \kappa \tau_{nj}$.
- ▶ Where τ_{nj} are calculated using a model of the city's transportation network.
- ▶ ΔCMA comes from calculating τ_{nj} before and after the BRT.
- ▶ For IV, replace τ_{nj} after BRT with $\hat{\tau}_{nj}$, assuming BRT runs through tramway lines.

Output of the final good in location j at time t :

$$q_{jt} = A_j (\tilde{L}_{jt}^l)^{\rho_j} (\tilde{L}_{jt}^h)^{(1-\rho_j)}.$$

Solving producer's problem we obtain

$$w_{j,t}^h \tilde{L}_{Fj,t}^h = (1 - \rho_j) X_{jt}, \quad (7)$$

$$w_{j,t}^l \tilde{L}_{Fj,t}^l = \rho_j X_{jt}. \quad (8)$$

Production - Details on Labor Demand

- ▶ From CES demand we know that $X_{jt} = p_{jt}^{1-\sigma} X$, where
 - ▶ $X = \sum_{i=1}^I \alpha \sum_{g \in \{h,l\}} \bar{y}_{igt}$ is total city exp. on consumption.
 - ▶ \bar{y}_{igt} is mean income for worker of type g in location i at time t .
- ▶ Perfect competition implies price equals marginal cost:

$$p_{jt} = A_j^{-1} (w_{jt}^l)^{\rho_j} (w_{jt}^h)^{(1-\rho_j)}.$$

- ▶ Combining previous results we obtain labor demand at each location j at time t for each skill type g as a function of the wage vector $\mathbf{w}_t = \{\{w_{jt}^h\}_{j=1}^J, \{w_{jt}^l\}_{j=1}^J\}$:

$$\tilde{L}_{Fj,t}^g = f_{jgt}(\mathbf{w}_t) \quad (9)$$

Labor Market Clearing

$$\underbrace{L_{Fjt}^g = \frac{f_{jgt}(\mathbf{w}_t)}{\bar{\epsilon}_{jt}^g}}_{\text{labor demand}} = \underbrace{\sum_{i=1}^I \frac{(w_{j,t}^g/d_{ij,t})^\theta}{\sum_j \left(\frac{w_{j,t}^g}{d_{ij,t}}\right)^\theta}}_{\text{labor supply}} L_{Ri,t}^g. \quad (10)$$

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Floorspace Market Clearing

- ▶ Assume fixed supply of floorspace \bar{H}_{Ri} .
- ▶ Demand for floorspace by skill group comes from FOC of consumer problem.
- ▶ Implies floorspace market clearing condition:

$$r_{Ri,t} = \frac{\overbrace{\sum_{g \in \{h,l\}} L_{Ri,t}^g \tilde{T}_g \phi_{Rgi,t}^{\frac{1}{\theta_g}} (1 - \alpha)}^{\text{total income by } g}}{\bar{H}_{Ri}}. \quad (11)$$

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Share of employment by commune for each skill level

workers_by_commune.pdf

Reduced Form vs. Model (Districts)

Reduced Form (IV)		Model	
$\Delta \log(\text{hs share})$		$\Delta \log(\text{hs share}_{BRT}) - \Delta \log(\text{hs share}_{CF})$	
$\Delta \log(CMA)$	-2.31 (0.52)***	$\Delta \log(CMA_{BRT}) - \Delta \log(CMA_{CF})$	-2.20 (0.62)***
hs share ₀	0.11 (0.05)**	hs share ₀	-0.03 (0.04)
$\Delta \log(CMA) \times \text{hs sh. avg.}_0$	4.14 (0.85)***	$\Delta \log(CMA_{BRT}) - \Delta \log(CMA_{CF}) \times \text{hs share}_0$	6.17 (1.65)***
cons	-0.42 (0.04)***	cons	-0.01 (0.02)
N	2,282	N	167

Welfare Gains With Only Medium HS Share Lines Built

Gains are largest close to BRT line.

welfare_t_0_cf_med.png

Gains are almost the same than with full BRT system.

welfare_t_0_cf_med_comp.png

Welfare Gains With Only High HS Share Line Built

Gains are largest close to BRT line.

welfare_t_0_cf_high.png

Compared to full BRT system, gains are slightly smaller close to BRT line.

welfare_t_0_cf_high_comp.png

Reduced Form Results: Increase in Segregation by Skill Type

► Using IV specification:

- $\frac{\Delta \log(\text{HS share})}{\Delta \log(\text{CMA})}$ for census tract at **20th** percent. of HS share: **0.1**
- $\frac{\Delta \log(\text{HS share})}{\Delta \log(\text{CMA})}$ for census tract at **80th** percent. of HS share: **0.6**

	$\Delta \log(\text{hs share})$				
	OLS	IV	OLS	IV	IV
$\Delta \log(\text{CMA})$	-0.122 (0.087)	0.202 (0.096)**	-2.797 (0.564)***	-2.308 (0.522)***	-2.609 (1.197)**
hs share ₀	0.192 (0.038)***	0.296 (0.044)***	0.153 (0.078)**	0.113 (0.052)**	0.191 (0.097)**
$\Delta \log(\text{CMA}) \times \text{hs sh. avg.}_0$			4.629 (0.895)***	4.143 (0.847)***	3.489 (1.925)*
cons	-0.457 (0.026)***	-0.538 (0.031)***	-0.445 (0.053)***	-0.419 (0.036)***	-0.404 (0.063)***
Neigh. FE	NO	NO	NO	NO	YES
F first	-	410	-	403	135
N	2,282	2,282	2,282	2,282	2,282

* $p < 0.1$; ** $p < 0.05$; *** $p < 0.01$

Reduced Form Results: Housing Prices Increase more in Richer Neighborhoods

- ▶ Using IV specification:

- ▶ $\frac{\Delta \log(\text{floorspace price})}{\Delta \log(\text{CMA})}$ at **20th** percent. of HS share: **0.3**
- ▶ $\frac{\Delta \log(\text{floorspace price})}{\Delta \log(\text{CMA})}$ at **80th** percent. of HS share: **1**

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Why a Dynamic Model?

- ▶ Previous literature (Tsivanidis 2019, Ahlfeldt, et al. 2015, etc.) rely on comparative statics after the policy for welfare analysis.
- ▶ This tells us welfare gains in location for residents living there **after** changes (new equilibrium).
- ▶ But people can move around.
- ▶ Policy maker interested in welfare gains for residents living there **before** changes (**incumbents**).
- ▶ Must model explicitly migration \Rightarrow forward-looking agents.

Transport Use by Mode of Transport

81% of low-skilled and 73% of high-skilled commute by public transport or walking within the city.

Mode of Transport	Low-Skilled	High-Skilled	Total
Car / motorcycle	16.5%	22.9%	19.3%
Taxi	2.1%	3.7%	2.8%
Bus	37.1%	39.3%	38.1%
Subway	4.4%	14.5%	8.8%
Train	1.6%	3.2%	2.3%
Walking / bicycle	38.1%	16.3%	28.5%
Other	0.2%	0.0%	0.1%

Table: Percentage of trips made by mode of transport by skill type. Source: 2010 mobility survey.

Resident's Problem - Static Problem

- ▶ Cobb-Douglas on CES bundle of consumption varieties (c) and floor space (H^R).
- ▶ Income is effective wages ($w_j^g \varepsilon_j^g$) discounted by commute costs $d_{ij} = \exp(\kappa \tau_{ij})$.
- ▶ Implies indirect utility:

$$\Rightarrow C_{ij}^{g*} = \frac{w_j^g \varepsilon_j^g r_{Ri}^{\alpha-1}}{d_{ij}}.$$

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Resident's Problem - Dynamic Problem

$$v_{n,t}^g = \max_{\{i,j\}} \left\{ \underbrace{C_{nj,t}^{g*}}_{\text{flow utility}} + \underbrace{\beta E_t[v_{i,t+1}^g]}_{\text{cont. value}} - \underbrace{\mu_{ni}^g}_{\text{mig. cost}} + \underbrace{\eta_{i,t}^g}_{\text{id. res. shock}} \right\}$$

Taking expectations w. r. t. the joint distribution of ε_j and η_i ,

$$V_{n,t}^g = \tilde{T}_g \Phi_{Rgn,t}^{\frac{1}{\theta_g}} r_{Rn}^{\alpha-1} + \nu_g \ln \sum_{i=1}^I \exp \left(\beta V_{i,t+1}^g - \mu_{i,n}^g \right)^{\frac{1}{\nu_g}}. \quad (12)$$

Where

$$\underbrace{\Phi_{Rgn,t}}_{\text{CMA}} = \sum_j \left(\frac{w_{j,t}^g}{d_{nj,t}} \right)^{\theta_g},$$

and $\tilde{T}_g = T_g \times \Gamma(1 - 1/\theta_g)$, with T_g the scale parameter of the e.v. type II distribution for type g .

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“Neighborhood” Migration Flows and Residential Population

$m_{in,t}$: fraction of agents that are residing in location n at the beginning of period t , and move to location i by the end of period t . From distribution of idiosyncratic preferences $\eta_{n,t}$ we obtain:

$$m_{in,t}^g = \frac{\left[\exp(\beta V_{i,t+1}^g - \mu_{in}^g) \right]^{\frac{1}{\nu_g}}}{\sum_{m=1}^N \left[\exp(\beta V_{m,t+1}^g - \mu_{mn}^g) \right]^{\frac{1}{\nu_g}}} \quad (13)$$

It follows that:

$$L_{Ri,t}^g = \sum_{n=1}^I \underbrace{m_{in,t}^g L_{Rn,t-1}^g}_{\text{Num. movers } n \text{ to } i} \quad (14)$$

The probability that a worker that lives in i at time t decides to work in location j is:

$$\Pi_{j|tig} = \frac{(w_{j,t}^g/d_{ij,t})^{\theta_g}}{\sum_s \left(\frac{w_{s,t}^g}{d_{is,t}}\right)^{\theta_g}} = \frac{(w_{j,t}^g/d_{ij,t})^{\theta_g}}{\Phi_{Rgi,t}}. \quad (15)$$

Therefore, labor supply at time t for workplace location j will be

$$L_{Fj,t}^g = \sum_{i=1}^I \Pi_{j|tig} L_{Ri,t}^g, \quad (16)$$

Subway Lines in 2010

subway_2010_map.pdf