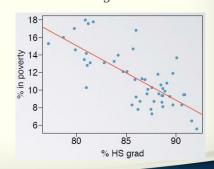


Example

According to the following linear model, what is the predicted % living in poverty in states where the HS graduation rate is 82%? % $\widehat{in\ poverty} = 64.68 - 0.62 \%$ $HS\ grad$

% in poverty =
$$64.68 - 0.62 \times 82$$

= 13.84%



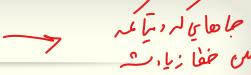


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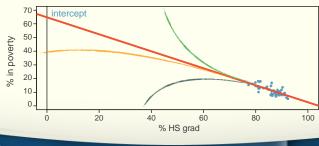
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Extrapolation



- ➤ Applying a model estimate to values outside of the realm of the original data is called extrapolation
- > Sometimes the intercept might be an extrapolation

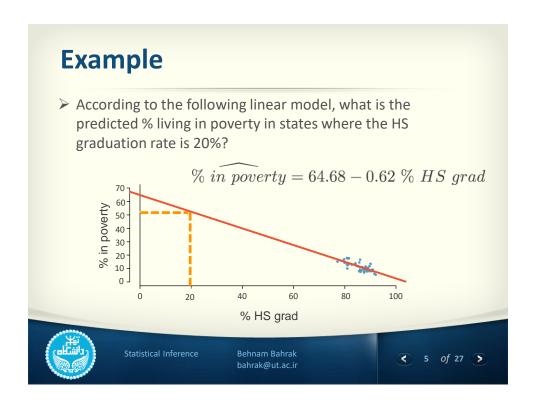




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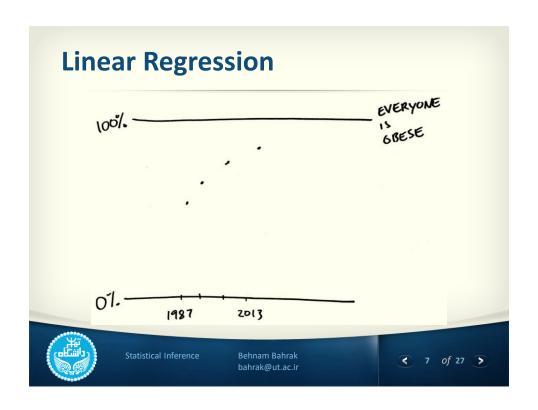


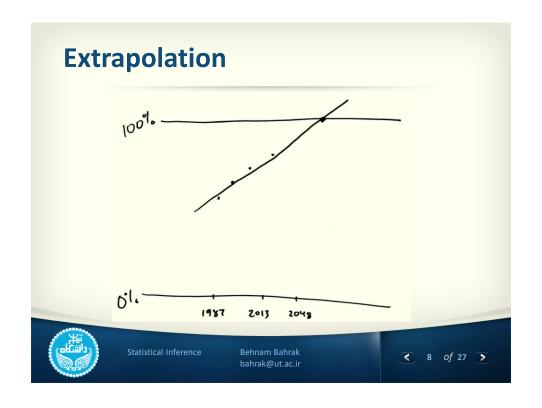
Will All Americans Become Overweight or Obese? Estimating the Progression and Cost of the US Obesity Epidemic

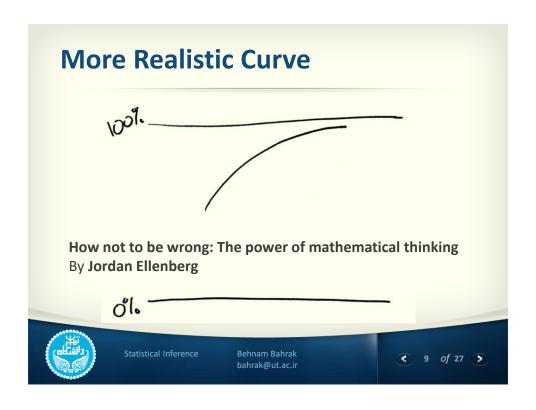
Youfa Wang¹, May A. Beydoun¹, Lan Liang², Benjamin Caballero¹ and Shiriki K. Kumanyika³

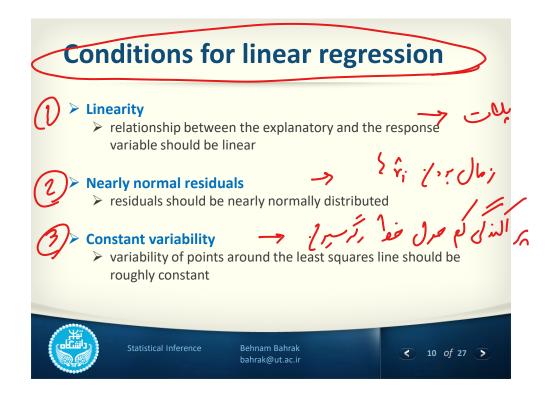
We projected future prevalence and BMI distribution based on national survey data (National Health and Nutrition Examination Study) collected between 1970s and 2004. Future obesity-related health-care costs for adults were estimated using projected prevalence, Census population projections, and published national estimates of per capita excess health-care costs of obesity/overweight. The objective was to illustrate potential burden of obesity prevalence and health-care costs of obesity and overweight in the United States that would occur if current trends continue. Overweight and obesity prevalence have increased steadily among all US population groups, but with notable differences between groups in annual increase rates. The increase (percentage points) in obesity and overweight in adults was faster than in children (0.77 vs. 0.46-0.49), and in women than in men (0.91 vs. 0.65). If these trends continue, by 2030, 86.3% adults will be overweight or obese; and 51.1%, obese. Black women (96.9%) and Mexican-American men (91.1%) would be the most affected. By 2048, all American adults would become overweight or obese, while black women will reach that state by 2034. In children, the prevalence of overweight (BMI ≥ 95th percentile, 30%) will nearly double by 2030. Total health-care costs attributable to obesity/overweight would double every decade to 860.7-956.9 billion US dollars by 2030, accounting for 16-18% of total US health-care costs. We continue to move away from the Healthy People 2010 objectives. Timely, dramatic, and effective development and implementation of corrective programs/policies are needed to avoid the otherwise inevitable health and societal consequences implied by our projections.

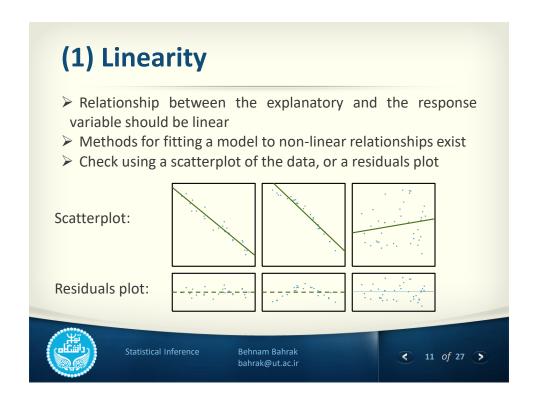


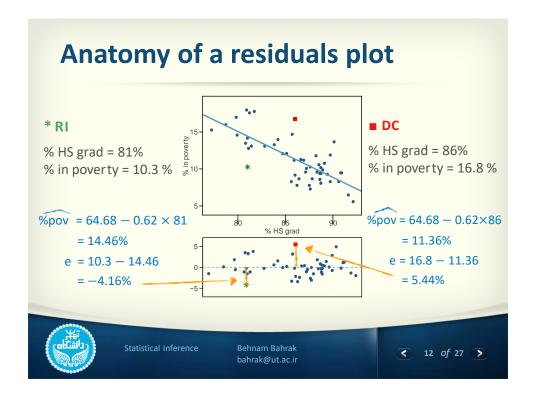


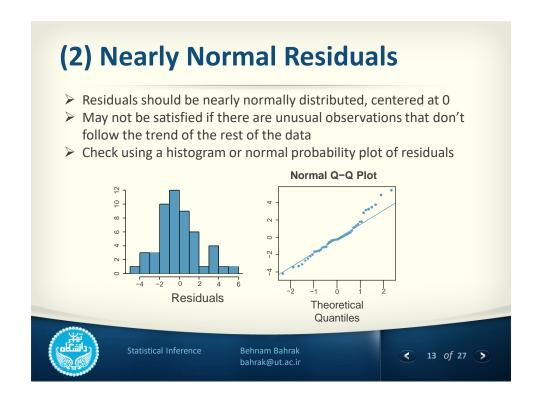


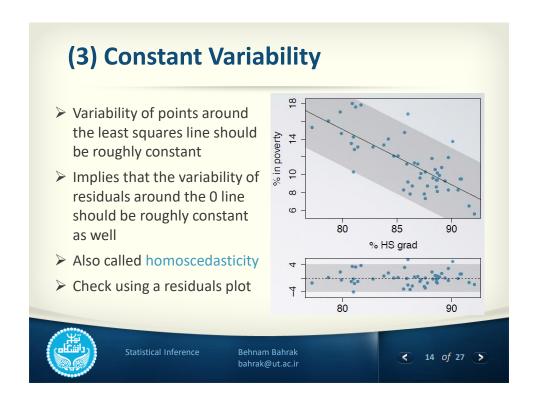












ترہنے مل میل حبہ مقداری از تعنیرات ارتغیریا سے دمل R^2

- > Strength of the fit of a linear model is most commonly evaluated using R^2
- Calculated as the square of the correlation coefficient
- Tells us what percent of variability in the response variable is explained by the model
- The remainder of the variability is explained by variables not included in the model
- ➤ Always between 0 and 1

$$R^2 = \frac{\left(\operatorname{Cov}(x, y)\right)^2}{\sigma_x^2 \sigma_y^2}$$



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Example

- Which of the following is the correct interpretation of the R^2 for this model for predicting % living in poverty from % HS graduation rate? ($R^2 = 0.5625$)
 - (a) 56.25% of the time % HS graduates predict % living in poverty correctly.
 - (b) 43.75% of the variability in the % of residents living in poverty among the states is explained by the model.
 - (c) 56.25% of the variability in the % of HS graduates among the states is explained by the model.
 - (d) \$6.25% of the variability in the % of residents living in poverty among the states is explained by the model.



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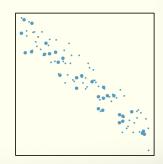
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Example

 \triangleright The \mathbb{R}^2 for the relationship displayed in the scatterplot is 92.16%. What is the correlation coefficient?

$$|R| = \sqrt{R^2} = \sqrt{0.9216} = 0.96$$

$$\Rightarrow R = -0.96$$





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Regression with categorical explanatory variable

Poverty vs. Region explanatory variable: region 0: east 1: west



$$\widehat{poverty} = 11.17 + 0.38 \ region : west$$

for eastern states plug in 0 for x

for western states plug in 1 for x

$$\widehat{poverty} = 11.17 + 0.38 \times 0 = 11.17$$
 $\widehat{poverty} = 11.17 + 0.38 \times 1 = 11.55$

In regression models, with explanatory categorical variables, reference level: we always code one of the levels of that categorical variable to be what we call the reference level. This is the level that we plug in zero for.



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 $\widehat{poverty} = 11.17 + 0.38 \ region : west$

- ➤ Intercept: The model predicts an 11.17% average poverty percentage in eastern states.
- ➤ This is the value we get if we plug in 0 for the explanatory variable
- Slope: The model predicts that the average poverty percentage in western states is 0.38% higher than in the eastern states.

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Example

Next, we use a new region variable (region4) with four levels: northeast, midwest, west, south. Write the linear regression model based on the regression output below.

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	9.50	0.87	10.94	0.00
region4:midwest	0.03	1.15	0.02	0.98
region4:west	1.79	1.13	1.59	0.12
region4:south	4.16	1.07	3.87	0.00

% in poverty = 9.50 + 0.03 reg4:mw+ 1.79 reg4:w + 4.16 reg4:s

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