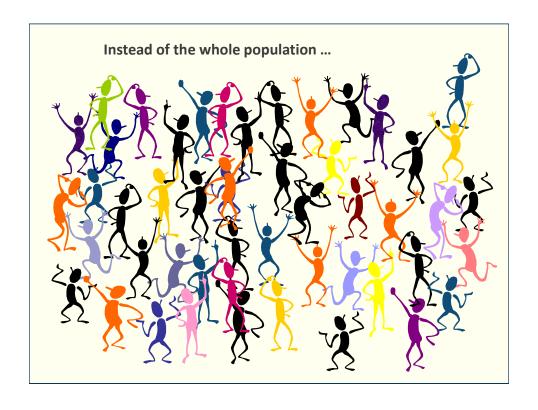
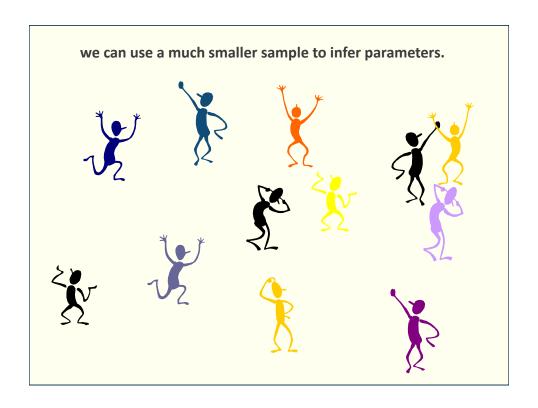


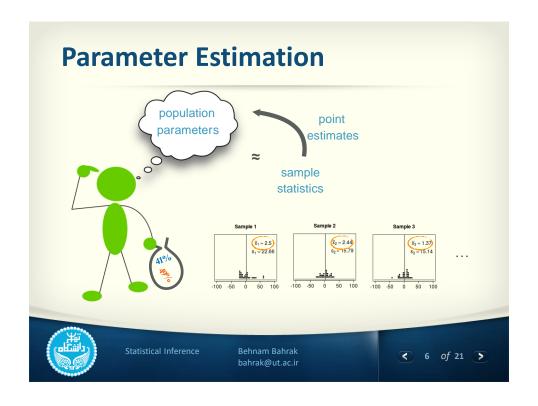
Results of the Survey

- ➤ The general public survey is based on telephone interviews conducted June 25-27, 1999, with a nationally representative sample of 1,016 adults ages 18 and older living in the continental United States.
- ➤ Margin of sampling error is plus or minus 3 percentage points for results at the 95% confidence level.
- ➤ 18% ± 3%: We are 95% confident that 15% to 21% of the adult Americans believe that the sun revolve around the earth.

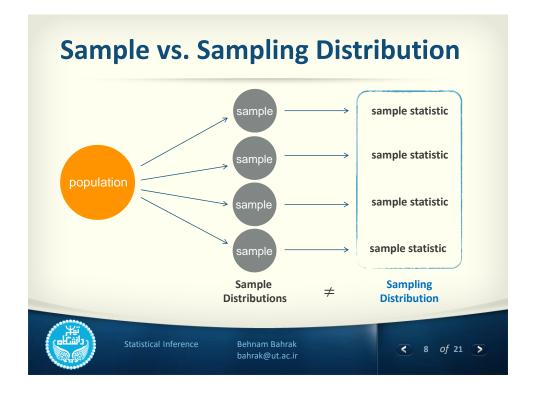


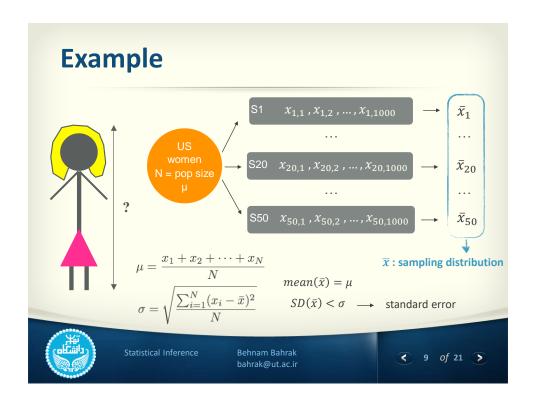






Parameter Estimation > We are often interested in population parameters. > Since complete populations are difficult (or impossible) to collect data on, we use sample statistics as point estimates for the unknown population parameters of interest. > Sample statistics vary from sample to sample. > Quantifying how sample statistics vary provides a way to estimate the margin of error associated with our point estimate.







Central Limit Theorem (CLT): The distribution of the sample mean is well approximated by a normal model:

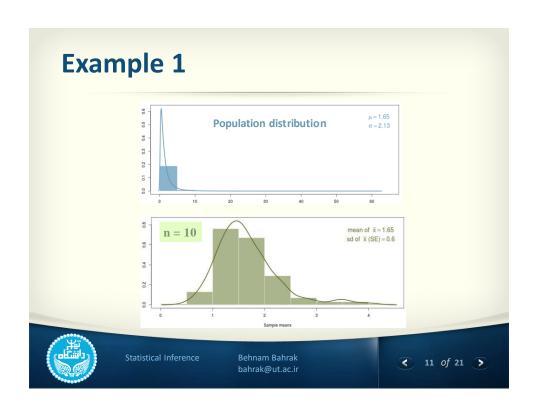
$$\bar{x} \sim N(mean = \mu, SE = \frac{\sigma}{\sqrt{n}})$$

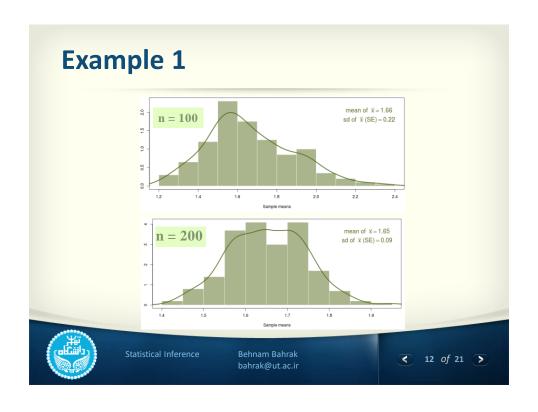
where SE represents standard error, which is defined as the standard deviation of the sampling distribution.

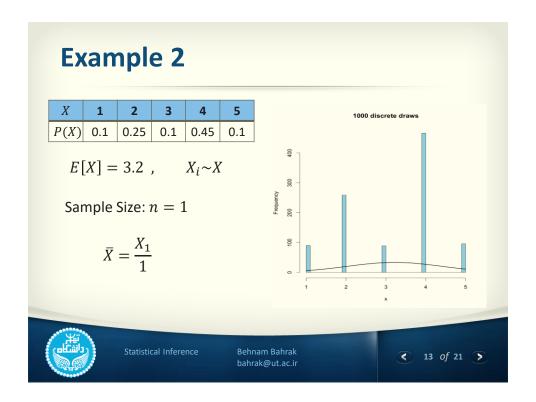
- \triangleright Note that as n increases SE decreases.
- \triangleright If σ is unknown, use s (the sample standard deviation).
 - > s: the standard deviation of one sample that we happen to have at hand

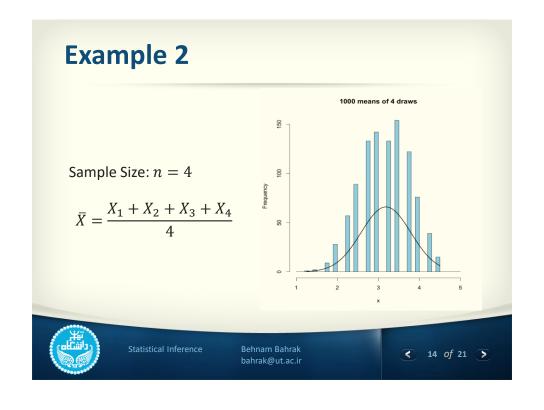


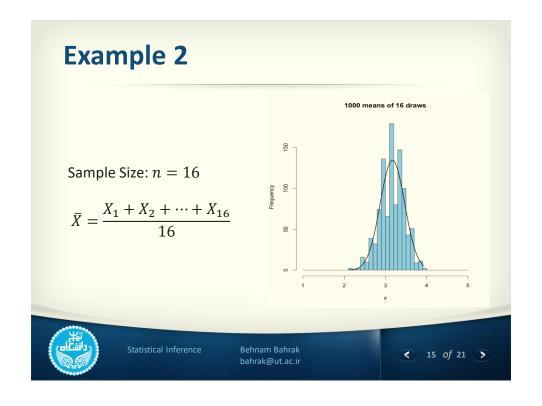
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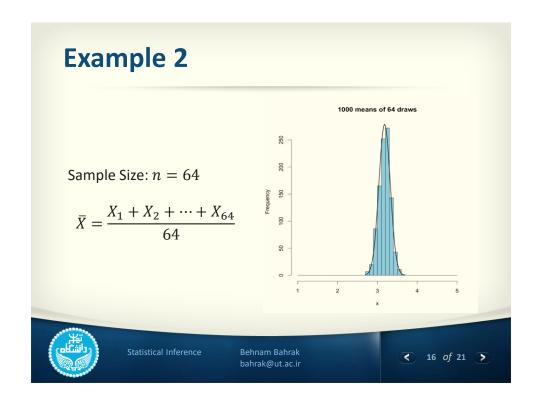












CLT Conditions

رزات مر رکزی

Certain conditions must be met for the CLT to apply:

مقلاك

1. Independence: Sampled observations must be independent. This is difficult to verify, but is more likely if:

random sampling/assignment is used, and



 \nearrow if sampling without replacement, n < 10% of the population.

- 2. Sample size/skew: Either the population distribution is normal, or if the population distribution is skewed, the sample size is large.
 - the more skewed the population distribution, the larger sample size we need for the CLT to apply
 - \triangleright for moderately skewed distributions n > 30 is a widely used rule of thumb



Statistical Inference

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Justification for the Conditions

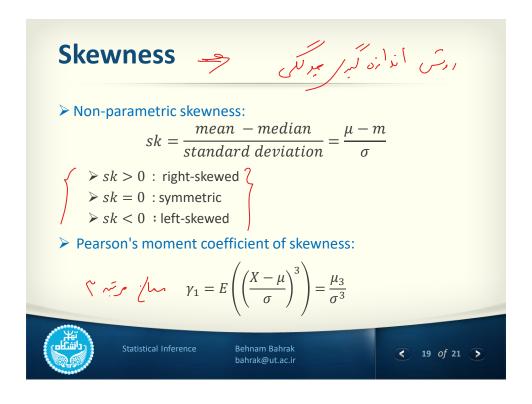
- \triangleright If sampling without replacement, n needs to be less than 10% of the population. Why is this the case?
 - if we grab a very big portion of the population to be in our sample, its going to be very difficult to make sure that the sampled individuals are independent of each other.
- The more skewed the population distribution, the larger sample size we need for the CLT to apply. Why?
 - ➤ When the sample size is small, the sample means will be quite variable, and the shape of their distribution will mimic the population distribution.

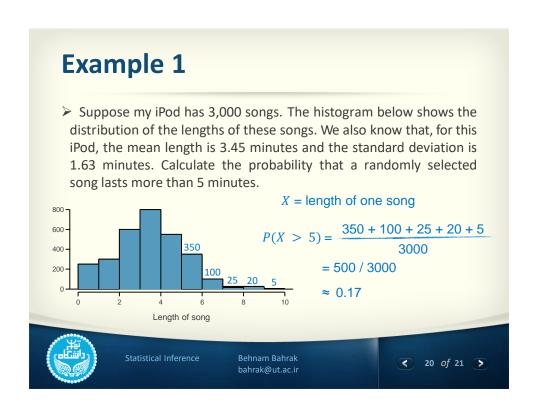


Statistical Inference

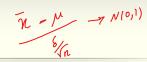
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Example 2



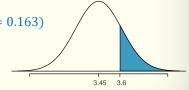
➤ I'm about to take a trip to visit my parents and the drive is 6 hours. I make a random playlist of 100 songs. What is the probability that my playlist lasts the entire drive?

$$P\{X_1 + X_2 + ... + X_{100} \ge 360 \text{ min}\} = ? \Rightarrow P\{\bar{X} \ge 3.6\} = ?$$

$$\bar{X} \sim N(mean = \mu = 3.45, SE = \frac{\sigma}{\sqrt{n}} = \frac{1.63}{\sqrt{100}} = 0.163)$$

$$Z = \frac{3.6 - 3.45}{0.163} = 0.92$$

$$P(Z > 0.92) = 0.179$$





Statistical Inference

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