

Review

What purpose does a large sample serve?

- As long as observations are independent, and the population distribution is not extremely skewed, a large sample would ensure that...
 - > the sampling distribution of the mean is nearly normal
 - ightharpoonup the estimate of the standard error is reliable: $\frac{s}{\sqrt{n}}$

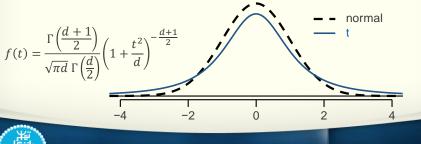


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Student's t-distribution

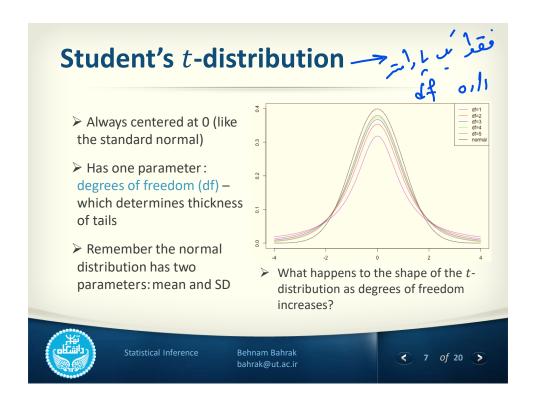
- \triangleright When σ is unknown (which is almost always), use the t-distribution to address the uncertainty of the standard error estimate
- > Bell shaped but thicker tails than the normal
 - ➤ Observations more likely to fall beyond 2 SDs from the mean
 - ➤ Extra thick tails helpful for mitigating the effect of a less reliable estimate for the standard error of the sampling distribution

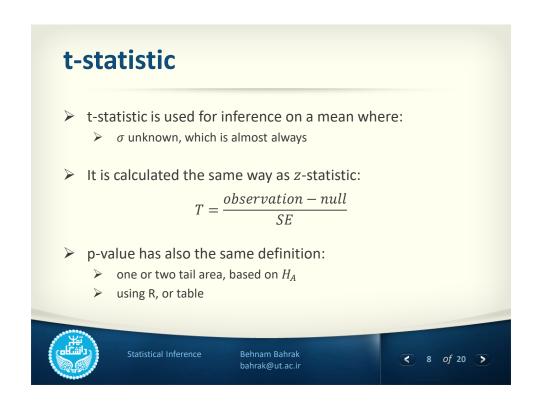


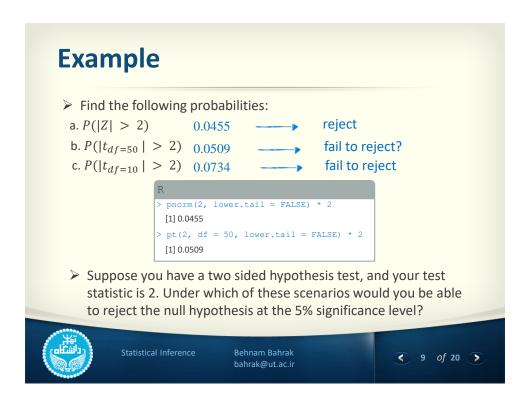


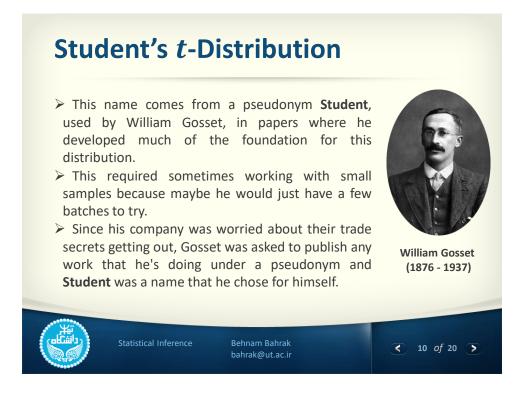
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PLAYING A COMPUTER GAME DURING LUNCH AFFECTS FULLNESS, MEMORY FOR LUNCH, AND LATER SNACK INTAKE

distraction and recall of food consumed and snacking

Biscuit intake

solitaire

No distraction

- > Sample: 44 patients: 22 men and 22 women
- > Study design:
 - randomized into two groups:
 - (1) play solitaire while eating -"win as many games as possible"
 - (2) eat lunch without distractions
 - both groups provided same amount of lunch
 - > offered biscuits to snack on after lunch



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 \overline{x}

52.1g

27.1g

s

45.1g

26.4g

n

22

Estimating the Mean

point estimate ± margin of error

$$\bar{x} \pm t_{df}^{\star} SE_{\bar{x}}$$

$$\bar{x} \pm t_{df}^{\star} \frac{s}{\sqrt{n}}$$

$$\bar{x} \pm t_{n-1}^{\star} \frac{s}{\sqrt{n}}$$

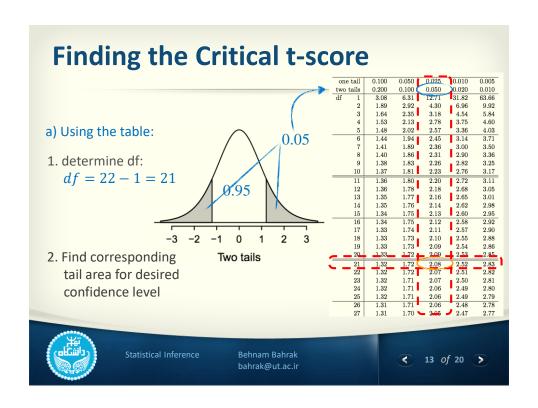
> Degrees of freedom for t statistic for inference on one sample mean: df = n - 1

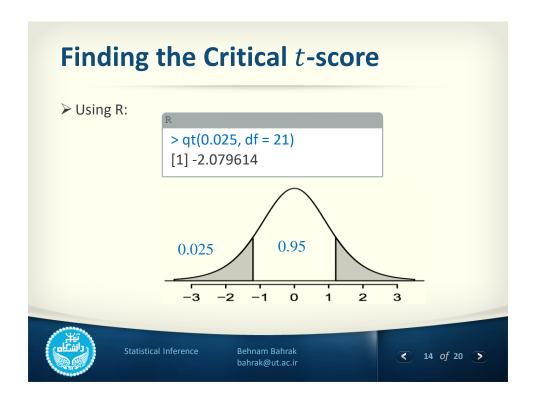


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Example

Estimate the average after-lunch snack consumption (in grams) of people who eat lunch distracted using a 95% confidence interval.

$$ar{x} = 52.1 \ g$$
 $s = 45.1 \ g$ $n = 22$ $z = 52.1 \pm 2.08 \times \frac{45.1}{\sqrt{22}}$ $z = 52.1 \pm 2.08 \times 9.62$ $z = 52.1 \pm 2.08 \times 9.62$ $z = 52.1 \pm 2.08 \times 9.62$

> We are 95% confident that distracted eaters consume between 32.1 to 72.1 grams of snacks post-meal.



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Example

> Suppose the suggested serving size of these biscuits is 30 g. Do these data provide convincing evidence that the amount of snacks consumed by distracted eaters post-lunch is different than the suggested serving size?

$$ar{x} = 52.1 \ g$$
 $H_0: \ \mu = 30$
 $s = 45.1 \ g$ $T = \frac{52.1 - 30}{9.62} = 2.3$
 $SE = 9.62$ $df = 22 - 1 = 21$



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