

Tutorial 2

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1 Exercise 1

1.1 a)

$$\begin{aligned} \langle (x - \mu)^2 \rangle &= \langle x^2 - 2x\mu + \mu^2 \rangle \\ &= \langle x^2 \rangle - \langle 2x\mu \rangle + \langle \mu^2 \rangle \\ &= \langle x^2 \rangle - 2\langle x \rangle \mu + \mu^2 \\ &= \langle x^2 \rangle - 2\mu\mu + \mu^2 \\ &= \langle x^2 \rangle - \mu^2 \end{aligned} \tag{1}$$

1.2 b)

$$\begin{aligned} E(x) &= \int_{-\infty}^{\infty} x \frac{1}{b-a} dx \\ &= \frac{1}{2} \frac{1}{b-a} [x^2]_a^b \\ &= \frac{1}{2} \frac{b^2 - a^2}{b-a} \\ &= \frac{1}{2} (b+a) \end{aligned} \tag{2}$$

$$\begin{aligned} Var(x) &= E(x^2) - E(x)^2 \\ &= \int_{-\infty}^{\infty} x^2 \frac{1}{b-a} dx - E(x)^2 \\ &= \frac{1}{3} \frac{1}{b-a} [x^3]_a^b - E(x)^2 \\ &= \frac{1}{3} \frac{b^3 - a^3}{b-a} - \left(\frac{1}{2}(b+a)\right)^2 \\ &= \frac{1}{12} (4b^2 + 4ab + 4a^2 - 3a^2 - 6ab - 3b^2) \\ &= \frac{1}{12} (b-a)^2 \end{aligned} \tag{3}$$