

BISON Instantiating the Whitened Swap-Or-Not Construction

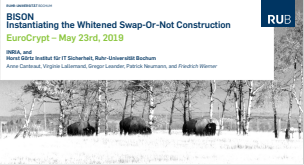
EuroCrypt – May 23rd, 2019

INRIA, and
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Anne Canteaut, Virginie Lallemand, Gregor Leander, Patrick Neumann, and *Friedrich Wiemer*



2019-04-01

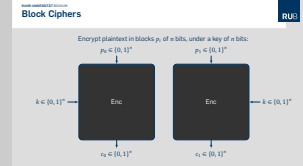
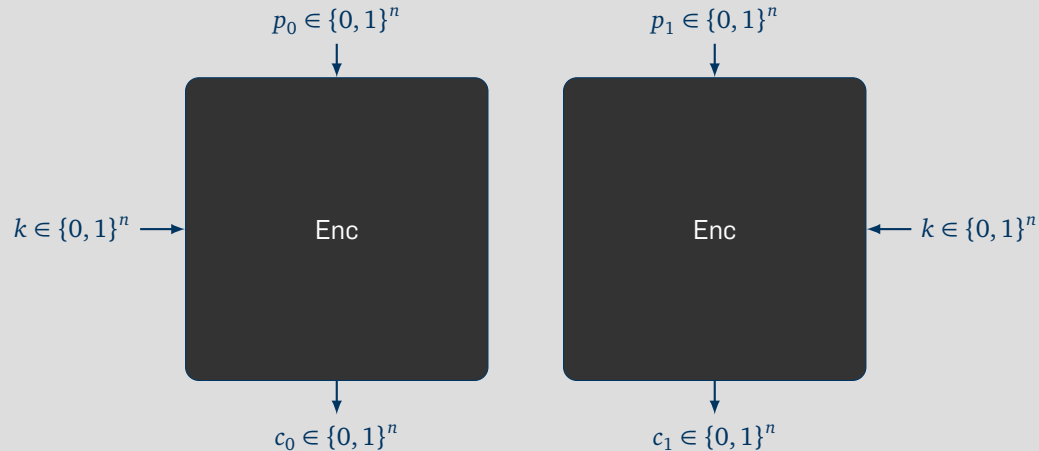
BISON Instantiating the Whitened Swap-Or-Not Construction



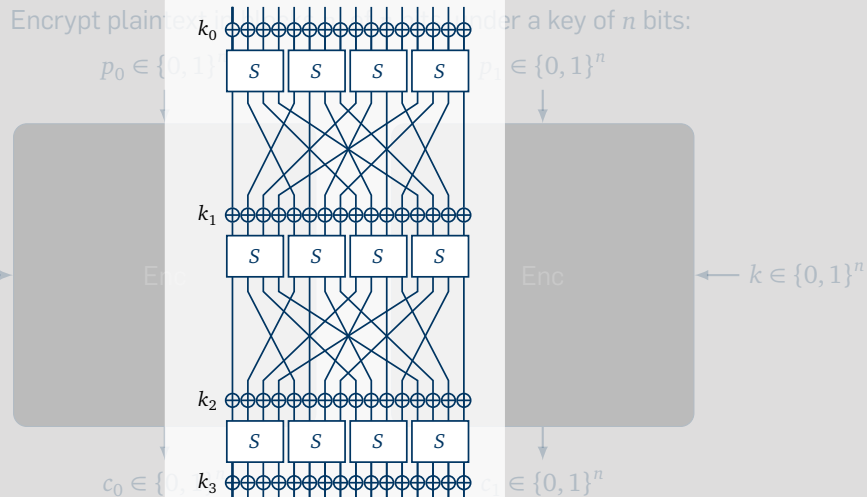
- Whitened Swap-Or-Not Construction developed by Hoang et al. and Tessaro
- Way of building block ciphers
- As this is one of the few talks here at EuroCrypt about block ciphers, lets start simple



Encrypt plaintext in blocks p_i of n bits, under a key of n bits:



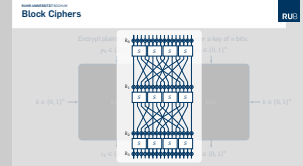
- Block ciphers encrypt *blocks* of n -bit inputs under an n -bit master key
- As a basic cryptographic primitive, we need special modes of operations, if the data to be encrypted is not of exactly n -bit length.
- This we do not consider here, instead we want to look at how to build this black box.



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Construction

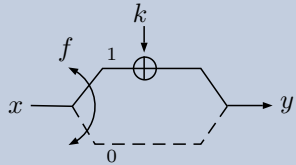
Block Ciphers



- Block ciphers encrypt *blocks* of n -bit inputs under an n -bit master key
- As a basic cryptographic primitive, we need special modes of operations, if the data to be encrypted is not of exactly n -bit length.
- This we do not consider here, instead we want to look at how to build this black box.
- Typical approach is an SPN structure, where key-addition, S-box layer and a linear layer are iterated over several rounds.
- Relatively well understood
- Good security arguments against known attacks
- There are some problems: differentials and linear hull effects

Published by Tessaro at AsiaCrypt 2015 [ia.cr/2015/868].

Overview round, iterated r times



Whitened Swap-Or-Not round function

$$x, k \in \{0, 1\}^n \quad \text{and} \quad f_k : \{0, 1\}^n \rightarrow \{0, 1\}$$

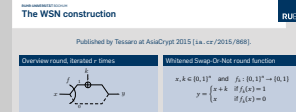
$$y = \begin{cases} x + k & \text{if } f_k(x) = 1 \\ x & \text{if } f_k(x) = 0 \end{cases}$$

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└ The WSN construction

└ The WSN construction

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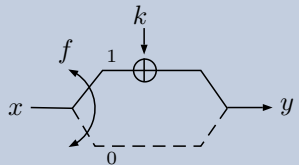


- Lets take a look at the WSN construction (simplified).
- Again, an iterated round function, where the input is fed into from the left.
- Next, a Boolean function decides if either the round key k is xored onto the input, or nothing happens.
- The result is the updated state, respective the output of the round.
- In other words, x , and k are both n -bit strings and f is an n -bit Boolean function.
- The round output y is either $x + k$ if $f_k(x) = 1$ or just x in the other case.
- So why is this nice?

The WSN construction

Published by Tessaro at AsiaCrypt 2015 [ia.cr/2015/868].

Overview round, iterated r times



Properties of f_k (needed for decryption)

$$f_k(x) = f_k(x + k)$$

Whitened Swap-Or-Not round function

$$x, k \in \{0, 1\}^n \quad \text{and} \quad f_k : \{0, 1\}^n \rightarrow \{0, 1\}$$

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Security Proposition (informal)

The WSN construction with $r = \mathcal{O}(n)$ rounds is *Full Domain* secure.

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The WSN construction	
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Overview round, iterated r times	Whitened Swap-Or-Not round function
	$x, k \in \{0, 1\}^n$ and $f_k : \{0, 1\}^n \rightarrow \{0, 1\}$ $y = \begin{cases} x + k & \text{if } f_k(x) = 1 \\ x & \text{if } f_k(x) = 0 \end{cases}$
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- So why is this nice?
- Tessaro was able to show that this construction, when iterated over $\mathcal{O}(n)$ rounds, achieves *Full Domain* security (what ever that means).
- One further property of f which we need for decryption is that x and $x + k$ maps to the same output.

The WSN construction

Encryption

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Input

x

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- └ The WSN construction

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- └ The WSN construction

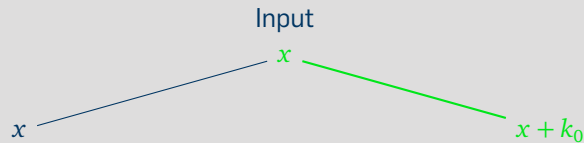


- We can observe an interesting first property, when looking at the encryption procedure round by round
- Starting with the plaintext $x \dots$

The WSN construction

Encryption

RUB

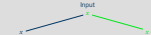


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└ The WSN construction

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The WSN construction
Encryption

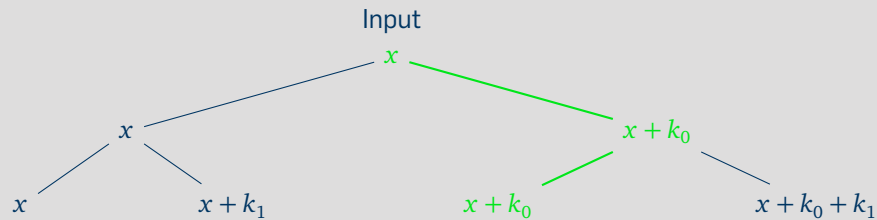


- We can observe an interesting first property, when looking at the encryption procedure round by round
- Starting with the plaintext $x \dots$
- \dots in each round, we either add the round key k_i, \dots

The WSN construction

Encryption

RUB



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└─ The WSN construction

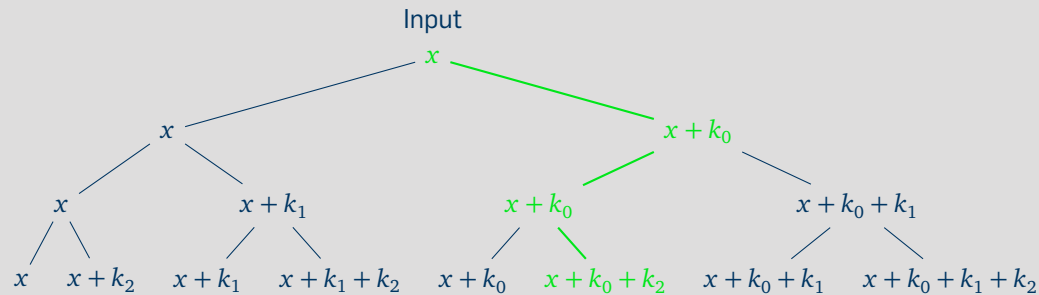
└─ The WSN construction



- We can observe an interesting first property, when looking at the encryption procedure round by round
- Starting with the plaintext x ...
- ...in each round, we either add the round key k_i , ...
- ...or not.

The WSN construction

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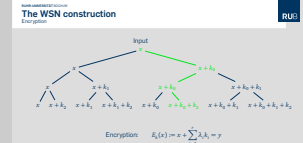


BISON Instantiating the Whitened Swap-Or-Not Construction

Construction

└ The WSN construction

└ The WSN construction



- We can observe an interesting first property, when looking at the encryption procedure round by round
- Starting with the plaintext $x \dots$
- ...in each round, we either add the round key k_i , ...
- ...or not.
- Thus we end up with a binary tree of possible states.
- Furthermore, the encryption can also be written as the plaintext plus the sum of some round keys, chosen by the λ_i 's here.

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Construction

└─ The WSN construction

└─ An Implementation

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An Implementation

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- Sounds all very great.
- So from a practitioners point of view the natural next point is: lets implement it.



Construction

- $f_k(x) := ?$
- Key schedule?
- $\mathcal{O}(n)$ rounds?

Theoretical vs. practical constructions

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Construction

└ The WSN construction

└└ An Implementation

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Construction
<ul style="list-style-type: none"> ■ $f_k(x) := ?$ ■ Key schedule? ■ $\mathcal{O}(n)$ rounds?

Theoretical vs. practical constructions

- Sounds all very great.
- So from a practitioners point of view the natural next point is: lets implement it.
- But ugh...
- How does this Boolean function f_k actually looks like?
- What about a key schedule? How do we derive the round keys?
- And how many are $\mathcal{O}(n)$ rounds?
- So, from a theoretical point of view we have a nice construction.
- But from a practical point of view it is basically useless.
- OK, let us fix this.

Generic Analysis

On the number of rounds

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Observation

- The ciphertext is the plaintext plus a subset of the round keys:

$$y = x + \sum_{i=1}^r \lambda_i k_i$$

- For pairs x_i, y_i : $\text{span} \{x_i + y_i\} \subseteq \text{span} \{k_j\}$.

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Construction

└ Generic Analysis

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Generic Analysis
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Distinguishing Attack for $r < n$ rounds

There is an $u \in \mathbb{F}_2^n \setminus \{0\}$, s. t. $\langle u, x \rangle = \langle u, y \rangle$ holds always:

$$\begin{aligned} \langle u, y \rangle &= \left\langle u, x + \sum \lambda_i k_i \right\rangle \\ &= \langle u, x \rangle + \left\langle u, \sum \lambda_i k_i \right\rangle = \langle u, x \rangle + 0 \end{aligned}$$

for all $u \in \text{span}\{k_1, \dots, k_r\}^\perp \neq \{0\}$

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Rationale 1

Any instance must iterate at least n rounds; any set of n consecutive keys should be linearly indep.

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Any instance must iterate at least n rounds; any set of n consecutive keys should be linearly indep.

A bit out of the blue sky, but:

Rationale 2

For any instance, f_k has to depend on all bits, and for any $\delta \in \mathbb{F}_2^n$: $\Pr[f_k(x) = f_k(x + \delta)] \approx \frac{1}{2}$.

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Construction

└ Generic Analysis

└ Generic Analysis

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A genus of the WSN family: BISON

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Generic properties of Bent whitened Swap Or Not

- At least n iterations of the round function
- The round function depends on all bits
- Consecutive round keys linearly independent
- $\forall \delta : \Pr[f_k(x) = f_k(x + \delta)] = \frac{1}{2}$ (*bent*)

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BISON Instantiating the Whitened Swap-Or-Not Construction

Generic Analysis

A genus of the WSN family: BISON

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Rational 1 & 2: WSN is *slow* in practice!

But what about
Differential Cryptanalysis?

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BISON Instantiating the Whitened Swap-Or-Not Construction
└ Generic Analysis

└ A genus of the WSN family: BISON

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A genus of the WSN family: BISON

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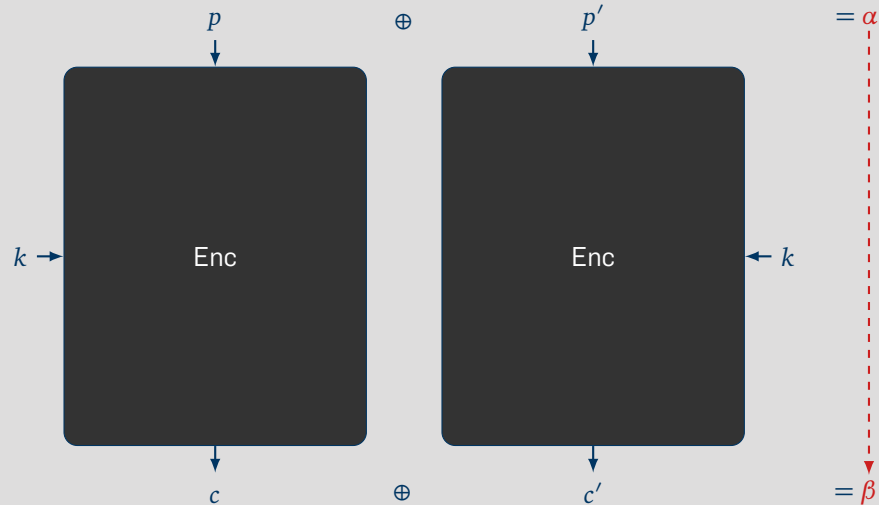
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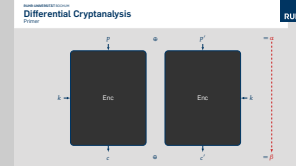
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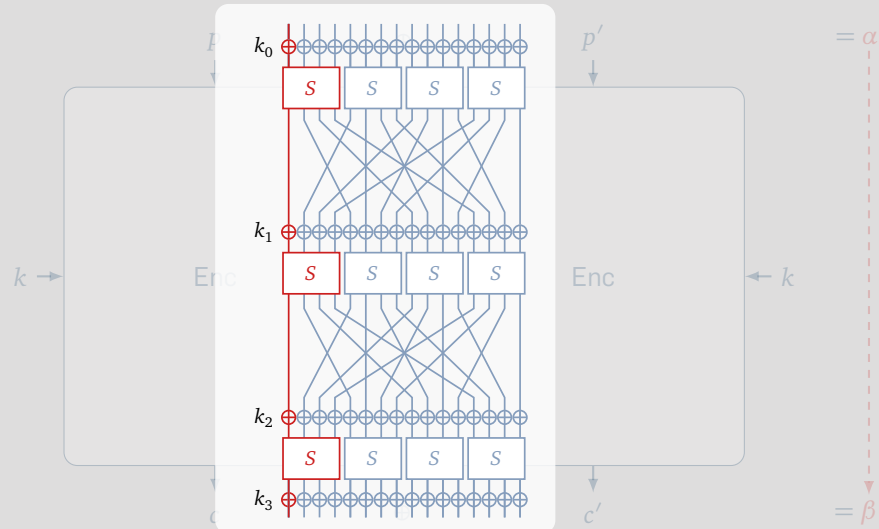
- Differential Analysis
- Differential Cryptanalysis



Differential Cryptanalysis

Primer

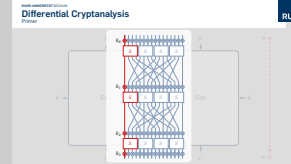
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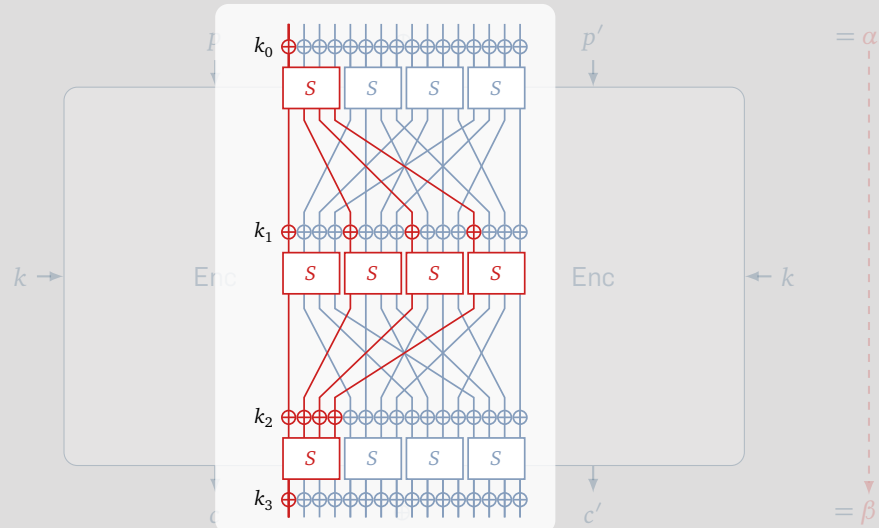
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Differential Cryptanalysis

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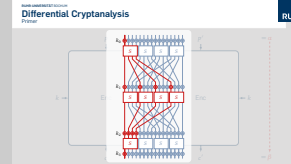
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BISON Instantiating the Whitened Swap-Or-Not Construction

- Differential Analysis
- Differential Cryptanalysis



Differential Cryptanalysis

One round

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Proposition

For one round of BISON the probabilities are:

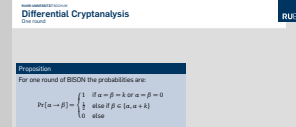
$$\Pr[\alpha \rightarrow \beta] = \begin{cases} 1 & \text{if } \alpha = \beta = k \text{ or } \alpha = \beta = 0 \\ \frac{1}{2} & \text{else if } \beta \in \{\alpha, \alpha + k\} \\ 0 & \text{else} \end{cases}$$

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BISON Instantiating the Whitened Swap-Or-Not
Construction

└ Differential Analysis

└ Differential Cryptanalysis



Differential Cryptanalysis

One round

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BISON Instantiating the Whitened Swap-Or-Not Construction
└ Differential Analysis

└ Differential Cryptanalysis

Differential Cryptanalysis	
One round	
Proposition	Possible differences
For one round of BISON the probabilities are:	$ \begin{array}{rcl} x & + & f_k(x) \\ \oplus x + \alpha & & + f_k(x + \alpha) \\ = & & \alpha + (f_k(x) + f_k(x + \alpha)) \cdot k \end{array} $
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Differential Cryptanalysis

One round

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BISON Instantiating the Whitened Swap-Or-Not Construction
└ Differential Analysis

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Differential Cryptanalysis	
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<p>Remember</p> $\Pr[f_k(x) = f_k(x + \alpha)] = \frac{1}{2}$	

Proposition

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Remember

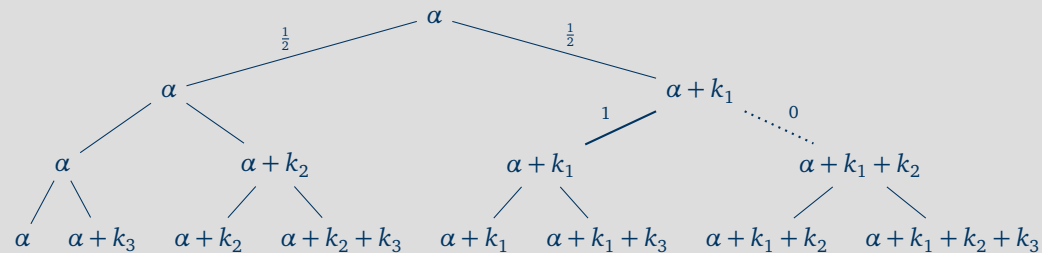
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Differential Cryptanalysis

More rounds

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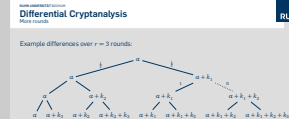
Example differences over $r = 3$ rounds:



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 └─ Differential Analysis

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└─ Differential Cryptanalysis



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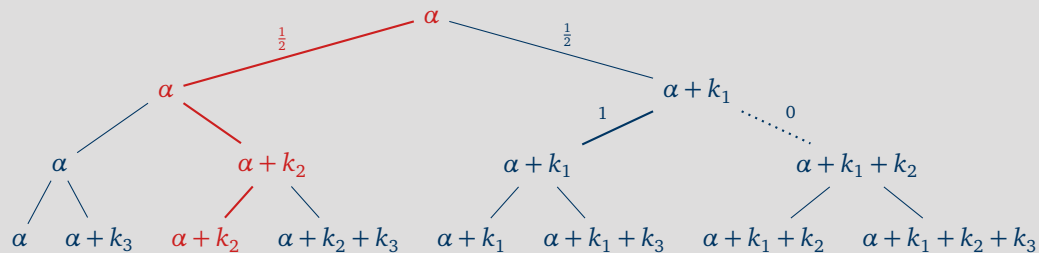


Differential Cryptanalysis

More rounds

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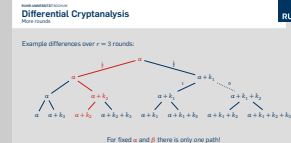


For fixed α and β there is only *one* path!

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Construction
└ Differential Analysis

└ Differential Cryptanalysis



A concrete species



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BISON Instantiating the Whitened Swap-Or-Not Construction
 └ The concrete Instance
 └ BISON



Addressing Rationale 1

The Key Schedule

Rationale 1

Any instance must iterate at least n rounds; any set of n consecutive keys should be linearly indep.

Design Decisions

- Choose number of rounds as $3 \cdot n$
- Round keys derived from the state of LFSRs
- Add round constants c_i to w_i round keys

Implications

- Clocking an LFSR is cheap
- For an LFSR with irreducible feedback polynomial of degree n , every n consecutive states are linearly independent
- Round constants avoid structural weaknesses

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BISON Instantiating the Whitened Swap-Or-Not Construction

- └ The concrete Instance

└ Addressing Rationale 1

Addressing Rationale 1	
Any instance must iterate at least n rounds; any set of n consecutive keys should be linearly indep.	
Design Decisions	Implications
<ul style="list-style-type: none"> ■ Choose number of rounds as $3 \cdot n$ ■ Round keys derived from the state of LFSRs ■ Add round constants c_i to w_i round keys 	<ul style="list-style-type: none"> ■ Clocking an LFSR is cheap ■ For an LFSR with irreducible feedback polynomial of degree n, every n consecutive states are linearly independent ■ Round constants avoid structural weaknesses

Addressing Rationale 2

The Round Function

Rationale 2

For any instance, the f_k should depend on all bits, and for any $\delta \in \mathbb{F}_2^n$: $\Pr[f_k(x) = f_k(x + \delta)] \approx \frac{1}{2}$.

Design Decisions

- Choose $f_k : \mathbb{F}_2^n \rightarrow \mathbb{F}_2$ s. t.

$$\delta \in \mathbb{F}_2^n : \Pr[f_k(x) = f_k(x + \delta)] = \frac{1}{2},$$

that is, f_k is a bent function.

- Choose the simplest bent function known:

$$f_k(x, y) := \langle x, y \rangle$$

Implications

- Bent functions well studied
- Bent functions only exists for even n
- Instance not possible for every block length n

BISON Instantiating the Whitened Swap-Or-Not Construction

The concrete Instance

Addressing Rationale 2

BISON Instantiating the Whitened Swap-Or-Not Construction

Addressing Rationale 2
The Round Function

Rationale 2

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Linear Cryptanalysis

For $r \geq n$ rounds, the correlation of any non-trivial linear trail for BISON is upper bounded by $2^{-\frac{n+1}{2}}$.

Zero Correlation

For $r > 2n - 2$ rounds, BISON does not exhibit any zero correlation linear hulls.

Invariant Attacks

For $r \geq n$ rounds, neither invariant subspaces nor nonlinear invariant attacks do exist for BISON.

Impossible Differentials

For $r > n$ rounds, there are no impossible differentials for BISON.

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BISON Instantiating the Whitened Swap-Or-Not Construction

└ Further Analysis

└ Further Cryptanalysis

Further Cryptanalysis	
Linear Cryptanalysis For $r \geq n$ rounds, the correlation of any non-trivial linear trail for BISON is upper bounded by $2^{-\frac{n+1}{2}}$.	Invariant Attacks For $r \geq n$ rounds, neither invariant subspaces nor nonlinear invariant attacks do exist for BISON.
Zero Correlation For $r > 2n - 2$ rounds, BISON does not exhibit any zero correlation linear hulls.	Impossible Differentials For $r > n$ rounds, there are no impossible differentials for BISON.

TODO

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- BISON Instantiating the Whitened Swap-Or-Not Construction
 - └ Further Analysis
 - └ Implementation

TODO

Conclusion/Questions

Thank you for your attention!

RUB

BISON

- A first instance of the WSN construction
- Good results for differential cryptanalysis

Open Problems

- Construction for linear cryptanalysis
- Further analysis: division properties

Thank you!

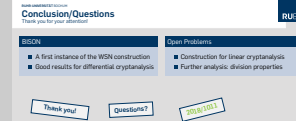
Questions?

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BISON Instantiating the Whitened Swap-Or-Not Construction

- └ Further Analysis
- └ Conclusion/Questions



Details

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BISON Instantiating the Whitened Swap-Or-Not
Construction
└─ Further Analysis

Details

BISON's round function

For round keys $k_i \in \mathbb{F}_2^n$ and $w_i \in \mathbb{F}_2^{n-1}$ the round function computes

$$R_{k_i, w_i}(x) := x + f_{b(i)}(w_i + \Phi_{k_i}(x)) \cdot k_i.$$

where

- Φ_{k_i} and $f_{b(i)}$ are defined as

$$\Phi_k(x) : \mathbb{F}_2^n \rightarrow \mathbb{F}_2^{n-1}$$

$$\Phi_k(x) := (x + x[i(k)] \cdot k)[j]_{\substack{1 \leq j \leq n \\ j \neq i(k)}}$$

$$f_{b(i)} : \mathbb{F}_2^{\frac{n-1}{2}} \times \mathbb{F}_2^{\frac{n-1}{2}} \rightarrow \mathbb{F}_2$$

$$f_{b(i)}(x, y) := \langle x, y \rangle + b(i),$$

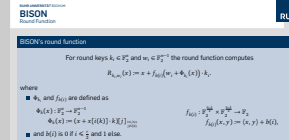
- and $b(i)$ is 0 if $i \leq \frac{r}{2}$ and 1 else.

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Specification

BISON



BISON's key schedule

Given

- primitive $p_k, p_w \in \mathbb{F}_2[x]$ with degrees $n, n - 1$ and companion matrices C_k, C_w .
- master key $K = (k, w) \in (\mathbb{F}_2^n \times \mathbb{F}_2^{n-1}) \setminus \{0, 0\}$

The i th round keys are computed by

$$\begin{aligned} \text{KS}_i : \mathbb{F}_2^n \times \mathbb{F}_2^{n-1} &\rightarrow \mathbb{F}_2^n \times \mathbb{F}_2^{n-1} \\ \text{KS}_i(k, w) &:= (k_i, c_i + w_i) \end{aligned}$$

where

$$k_i = (C_k)^i k, \quad c_i = (C_w)^{-i} e_1, \quad w_i = (C_w)^i w.$$

BISON Instantiating the Whitened Swap-Or-Not Construction

└ Specification

└ BISON

