RUB

EuroCrypt – May 23rd, 2019

INRIA, and

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BISON Instantiating the Whitened Swap-Or-Not $\frak{\mathbb{R}}$ Construction



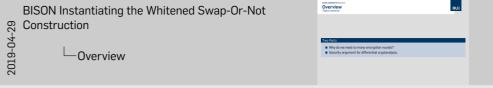
- Whitened Swap-Or-Not Construction developed by Hoang et al. and Tessaro
- Way of building block ciphers
- As this is one of the few talks here at EuroCrypt about block ciphers, we will start simple

Overview Topics covered



Two Parts

- Why do we need so many encryption rounds?
- Security argument for differential cryptanalysis.

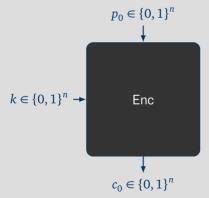


- Talk mainly about two parts of the paper:
 - Why do we need so many rounds (easy to understand argument)
 - Security against differential cryptanalysis
 (again relative simple argument that gives strong security here)

Block Ciphers



Encrypt plaintext in blocks p_i of n bits, under a key of n bits:



BISON Instantiating the Whitened Swap-Or-Not Construction
The WSN construction



- Block ciphers encrypt *blocks* of *n*-bit inputs under an *n*-bit master key
- As a basic cryptographic primitive, we need special modes of operations, if the data to be encrypted is not of exactly *n*-bit length.
- This we do not consider here, instead we want to look at how to build this black box.
- Typicall approach is an SPN structure, where key-addition, S-box layer and a linear layer are iterated over several rounds.
- Relatively well understood

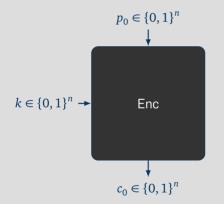
—Block Ciphers

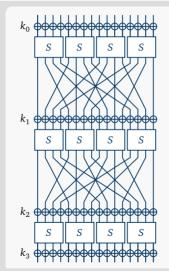
- Good security arguments against known attacks
- There are some problems: differentials and linear hull effects

Block Ciphers



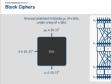
Encrypt plaintext in blocks p_i of n bits, under a key of n bits:





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The WSN construction



The West delicated

Block Ciphers

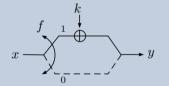
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- Good security arguments against known attacks
- There are some problems: differentials and linear hull effects

The WSN construction



Published by Tessaro at AsiaCrypt 2015 [ia.cr/2015/868].

Overview round, iterated r times



Whitened Swap-Or-Not round function

$$\{0,1\}^n \text{ and } f_k : \{0,1\}^n \to \{0,1\}$$
$$y = \begin{cases} x+k & \text{if } f_k(x) = 1\\ x & \text{if } f_k(x) = 0 \end{cases}$$

BISON Instantiating the Whitened Swap-Or-Not Construction

The WSN construction



The WSN construction

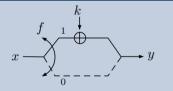
- Lets take a look at the WSN construction (simplified).
- Again, an iterated round function, where the input is fed into from the left.
- Next, a Boolean function decides if either the round key k is xored onto the input, or nothing happens.
- The result is the updated state, respective the output of the round.
- In other words, x, and k are both n-bit strings and f is an n-bit Boolean function.
- The round output y is either x + k if $f_k(x) = 1$ or just x in the other case.
- So why is this nice?

The WSN construction



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Security Proposition (informal)

The WSN construction with $r = \Theta(n)$ rounds is Full Domain secure.

BISON Instantiating the Whitened Swap-Or-Not Construction

— The WSN construction

The WSN construction Poisson of AsiaCryst 2015 [1s. cr/2015.7865].

Oberview roans, Resider triums

Should See Qu'il Yes (0.1) and $f_1(0.1)^{-1}-(0.1)$ $r = \frac{1}{s} + \frac{1}{s} f_1(s) = 1$ Seconly Projection (offered)

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The WSN construction

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- In other words, x, and k are both n-bit strings and f is an n-bit Boolean function.
- The round output y is either x + k if $f_k(x) = 1$ or just x in the other case.
- So why is this nice?
- Tessaro was able to show that this construction, when iterated over $\Theta(n)$ rounds, achieves *Full Domain* security (what ever that means).
- One further property of f which we need for decryption is that x and x + k maps to the same output.

Encryption

The WSN construction



Input





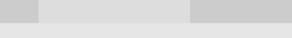
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- Starting with the plaintext x...

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The WSN construction Encryption





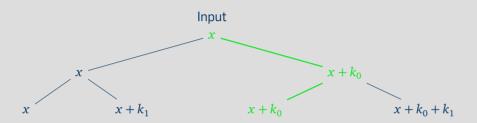


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- Starting with the plaintext *x*...
- ...in each round, we either add the round key k_i , ...

The WSN construction

Encryption





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The WSN construction



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• Starting with the plaintext x...

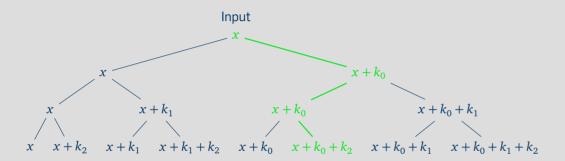
☐ The WSN construction

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The WSN construction

Encryption

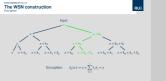




Encryption:
$$E_k(x) := x + \sum_{i=1}^r \lambda_i k_i = y$$

BISON Instantiating the Whitened Swap-Or-Not Construction

The WSN construction



The WSN construction

- We can observe an interesting first property, when looking at the encryption procedure round by round
- Starting with the plaintext x...
- ...in each round, we either add the round key k_i , ...
- ...or not.
- Thus we end up with a binary tree of possible states.
- Furthermore, the encryption can also be written as the plaintext plus the sum of some round keys, chosen by the λ_i 's here.





- Sounds all very great.
- So from a practitioners point of view the natural next point is: lets implement it.



Construction

- $f_k(x) := ?$
- Key schedule?
- \blacksquare $\Theta(n)$ rounds?

Theoretical vs. practical constructions



BISON Instantiating the Whitened Swap-Or-Not
Construction
The WSN construction
An Implementation



- Sounds all very great.
- So from a practitioners point of view the natural next point is: lets implement it.
- But uggh...
- How does this Boolean function f_{ν} actually looks like?
- What about a key schedule? How do we derive the round keys?
- And how many are $\Theta(n)$ rounds?
- So, from a theoretical point of view we have a nice construction.
- But from a practical point of view it is basically useless.
- OK. let us fix this.

Generic Analysis

On the number of rounds

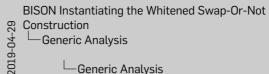
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Observation

■ The ciphertext is the plaintext plus a subset of the round keys:

$$y = x + \sum_{i=1}^{r} \lambda_i k_i$$

■ For pairs x_i, y_i : span $\{x_i + y_i\} \subseteq \text{span } \{k_i\}$.





- First observation: span $\{x_i + y_i\} \subseteq \text{span } \{k_i\}$
- Leads to a simple distinguishing attack, if number of rounds r < n.

Generic Analysis On the number of rounds

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Distinguishing Attack for r < n rounds

There is an $u \in \mathbb{F}_2^n \setminus \{0\}$, s. t. $\langle u, x \rangle = \langle u, y \rangle$ holds always:

$$\langle u, y \rangle = \langle u, x + \sum_{i} \lambda_{i} k_{i} \rangle$$
$$= \langle u, x \rangle + \langle u, \sum_{i} \lambda_{i} k_{i} \rangle = \langle u, x \rangle + 0$$

for all $u \in \text{span}\{k_1, \dots, k_r\}^{\perp} \neq \{0\}$

BISON Instantiating the Whitened Swap-Or-Not Construction
Generic Analysis

Generic Analysis



- Generic Analysis
- First observation: span $\{x_i + y_i\} \subseteq \text{span } \{k_i\}$
- Leads to a simple distinguishing attack, if number of rounds r < n.
- It is easy to find a u, s. t. $\langle u, y \rangle = \langle u, x \rangle = 0$ for all x, y = x, E(x).
- Simply use the bilinearity of the scalar product.
- Then any u from the dual space spanned by the round keys fullfills the above equation.
- ullet As long as there are less then n round keys, this dual space has dimension greater or equal then one.

Generic Analysis On the number of rounds

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Rationale 1

Any instance must iterate at least n rounds; any set of n consecutive keys should be linearly indp.

BISON Instantiating the Whitened Swap-Or-Not © Construction -Generic Analysis

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- Then any u from the dual space spanned by the round keys fullfills the above equation.
- As long as there are less then n round keys, this dual space has dimension greater or equal then one.
- A first design rational is thus...

Generic AnalysisOn the Boolean functions *f*



A bit out of the blue sky, but:

Rationale 2

For any instance, f_k has to depend on all bits, and for any $\delta \in \mathbb{F}_2^n$: $\Pr[f_k(x) = f_k(x+\delta)] \approx \frac{1}{2}$.

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Construction
Generic Analysis



• We also need this second rationale.

Generic Analysis

- Its not so easy explainable without going into more depth.
- So you have to believe me on this one.
- It basically says that for any input difference $\delta \neq k$:

$$\Pr[f_k(x) = f_k(x+\delta)] \approx \frac{1}{2}$$

A genus of the WSN family: BISON



Rationale 1

Any instance must iterate at least n rounds; any set of n consecutive keys should be linearly indp.

Rationale 2

For any instance, f_k has to depend on all bits, and for any $\delta \in \mathbb{F}_2^n$: $\Pr[f_k(x) = f_k(x + \delta)] \approx \frac{1}{2}$.

Generic properties of **B**ent wh**I**tened **S**wap **O**r **N**ot (BISON)

 \blacksquare At least n iterations of the round function

- The round function depends on all bits
- Consecutive round keys linearly independent
- $\forall \delta : \Pr[f_k(x) = f_k(x+\delta)] = \frac{1}{2} (bent)$

BISON Instantiating the Whitened Swap-Or-Not Construction
Generic Analysis

└─A genus of the WSN family: BISON



- A quick recap and implications for any WSN instance.
- Rationale 2 basically tells us, we have to use bent functions.
- Thats nice, as those functions are quite well understood and already well scrutinised.
- Also, this is the reason for the name: Bent Whitened Swap-Or-Not
- But, and thats not so nice...

A genus of the WSN family: BISON



Rationale 1

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Rational 1 & 2: WSN is *slow* in practice!

But what about Differential Cryptanalysis?

BISON Instantiating the Whitened Swap-Or-Not Construction

Generic Analysis

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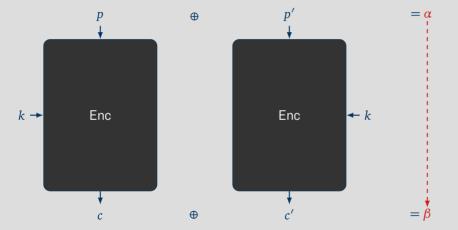
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- But, and thats not so nice...
- *n* iterations of a round function that depends on *all* bits will be slow
- Let me repeat this (Reviewer 2 argued that we should optimise more): No matter how good we will optimise this: *it will be slow*
- For example, assume you can do one round in one clock cycle, this is still an order of magnitude slower than AES.
- So, why should we care about any instance?
- All hope is not lost, let's have a look at differential cryptanalysis!

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Differential Cryptanalysis



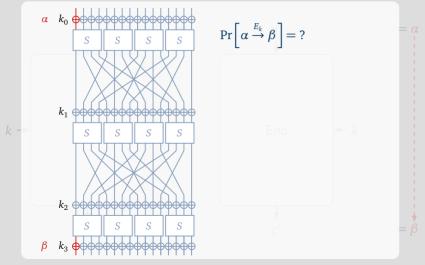
BISON Instantiating the Whitened Swap-Or-Not Construction -Differential Analysis



- For differential cryptanalysis, interested in propagation of input difference α to output difference β .
- Doing this in general at this abstraction level is a very hard problem.

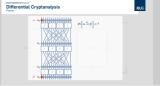
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Prime



BISON Instantiating the Whitened Swap-Or-Not Construction

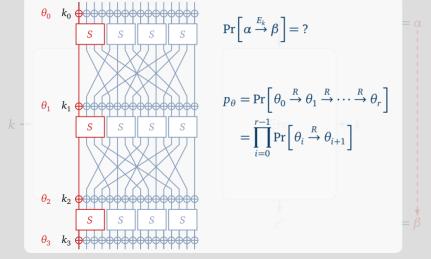
Differential Analysis



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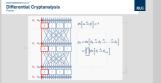
Primer





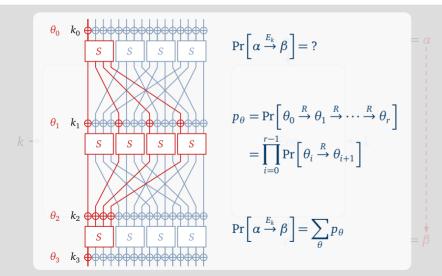
BISON Instantiating the Whitened Swap-Or-Not Construction

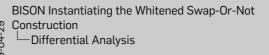
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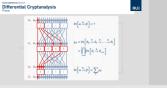


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- Now, computing the probability of one such trail is actually doable.
- But, trails can go several alternative ways through non-linear parts, thus we have to cope with a branching effect...

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- To say anything, we usually look for single so called *trails* through the inner building blocks.
- Now, computing the probability of one such trail is actually doable.
- But, trails can go several alternative ways through non-linear parts, thus we have to cope with a branching effect...
- And eventually, several of these trails cluster in a so called differential.
- While in this example it is still feasible, computing the *exact* probability in a real cipher is not.
- We thus have to restrain on bounding or approximating this probability.
- In the end, tight bounds for differentials over several rounds remain an open (but important!) problem.
- For BISON our aim is to give exactly this: a tight bound for any differential over several rounds.

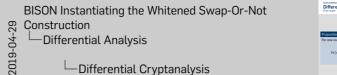
Differential Cryptanalysis One round



Proposition

For one round of BISON the probabilities are:

$$\Pr[\alpha \to \beta] = \begin{cases} 1 & \text{if } \alpha = \beta = k \text{ or } \alpha = \beta = 0 \\ \frac{1}{2} & \text{else if } \beta \in \{\alpha, \alpha + k\} \\ 0 & \text{else} \end{cases}$$





- We start by understanding the differential one round behaviour.
- For the three possible cases, let us look at what differences are actually possible.

Differential CryptanalysisOne round

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Possible differences

$$x + f_k(x) \cdot k$$

$$\oplus x + \alpha + f_k(x + \alpha) \cdot k$$

$$= \alpha + (f_k(x) + f_k(x + \alpha)) \cdot k$$

Properties of f_k

$$f_{\nu}(x) = f_{\nu}(x+k) \tag{1}$$

BISON Instantiating the Whitened Swap-Or-Not Construction

Differential Analysis



- We start by understanding the differential one round behaviour.
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- Remember that one round computes the output as $x + f_k(x) \cdot k$.
- With the input difference α we get as possible output differences $\beta \in \{0, \alpha, k, \alpha + k\}$.
- For decryption we need that x and x + k are mapped to the same value by f_{ν}
- Thus, $\beta = \alpha$ with probability one, if and only if $\alpha = k$ or $\alpha = 0$
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Differential CryptanalysisOne round

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$$f_k(x) = f_k(x+k) \tag{1}$$

$$\Pr[f_k(x) = f_k(x + \alpha)] = \frac{1}{2}$$
 (2)

BISON Instantiating the Whitened Swap-Or-Not Construction Differential Analysis

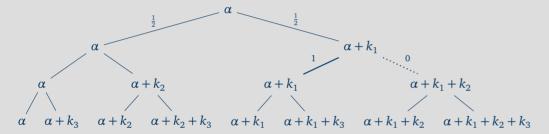


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- For decryption we need that x and x + k are mapped to the same value by f_{ν}
- Thus, $\beta = \alpha$ with probability one, if and only if $\alpha = k$ or $\alpha = 0$
- If β is not one of the above four values, such an input/output pair cannot occur, thus the probability is zero.
- For the last case, remember that for any input difference, we required that f_k collides with probability one half.

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More rounds

Example differences over r = 3 rounds ($\alpha = k_1 + k_2$):



BISON Instantiating the Whitened Swap-Or-Not Construction

Differential Analysis

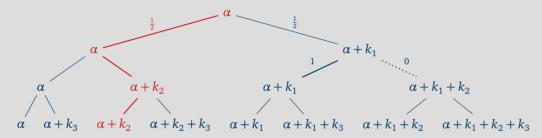


- When we look at more rounds, we can depict these cases again in this tree structure.
- Starting with the input difference α_1 assume it is different from the first round key k_0 and nonzero.
- After one round the two differences α and $\alpha + k_0$ occur with equal probability one half.
- As long as the intermediate difference is different from the next round key and nonzero, this argument iterates.
- At the point where the difference equals the next round key, these two choices collide into a deterministic propagation with probability one, where the round key is not added to the difference.

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More rounds

Example differences over r = 3 rounds ($\alpha = k_1 + k_2$):



Theorem (Differentials in BISON)

Let α , $\beta \in \mathbb{F}_2^n$. Then the probability for the differential $\alpha \to \beta$ is $\Pr[\alpha \to \beta] = \sum_{\alpha} p_{\theta} = p_{(\alpha,\theta_1,\dots,\theta_{r-1},\beta)}$.

BISON Instantiating the Whitened Swap-Or-Not Construction

— Differential Analysis



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- As long as the intermediate difference is different from the next round key and nonzero, this argument iterates.
- At the point where the difference equals the next round key, these two choices collide into a deterministic propagation with probability one, where the round key is not added to the difference.
- Regarding differentials, the important observation is:
- For any input/output pair (α, β) , there is only one path.
- In other words; no branching occurs and the differential consists of a single trail only.

BISON



A concrete species



BISON Instantiating the Whitened Swap-Or-Not © Construction The concrete Instance



—BISON

- Up to now we do not have specified much more then the initial WSN construction had.
- For a concrete implementation, we still need to define
 - Number of rounds
 - Key Schedule
 - Boolean function f_k
- So let us look at a concrete BISON species
- In particular, we discuss how to tackle Rationales 1 and 2.

Addressing Rationale 1

The Key Schedule



Rationale 1

Any instance must iterate at least n rounds; any set of n consecutive keys should be linearly indp.

Design Decisions

- Choose number of rounds as $3 \cdot n$
- Round keys derived from the state of LFSRs
- \blacksquare Add round constants c_i to w_i round keys

Implications

- Clocking an LFSR is cheap
- For an LFSR with irreducible feedback polynomial of degree *n*, every *n* consecutive states are linearly independent
- Round constants avoid structural weaknesses

BISON Instantiating the Whitened Swap-Or-Not Construction

The concrete Instance



Addressing Rationale 1

- Due to analysis of the alg. deg., we chose 3n rounds, see last slide.
- Deriving round keys from the states of LFSRs is efficiently implementable and fullfils our requirements for linear independent round keys.
- For those of you how attended Gregors talk at FSE:
 - While generating test vectors for the implementation we again noted some unwanted symmetries for encryptions with low hamming weight.
 - Thus we added round constants, to avoid these structural weaknesses.
 - (Sorry for fixing another cipher)

Addressing Rationale 2

RUB

The Round Function

Rationale 2

For any instance, the f_k should depend on all bits, and for any $\delta \in \mathbb{F}_2^n$: $\Pr[f_k(x) = f_k(x + \delta)] \approx \frac{1}{2}$.

Design Decisions

■ Choose $f_k : \mathbb{F}_2^n \to \mathbb{F}_2$ s.t.

$$\delta \in \mathbb{F}_2^n$$
: $\Pr[f_k(x) = f_k(x+\delta)] = \frac{1}{2}$,

that is, f_{ν} is a bent function.

■ Choose the simplest bent function known:

$$f_k(x,y) := \langle x,y \rangle$$

Implications

- Bent functions well studied
- \blacksquare Bent functions only exists for even n
- Instance not possible for every block length n

BISON Instantiating the Whitened Swap-Or-Not Construction
The concrete Instance

Addressing Rationale 2



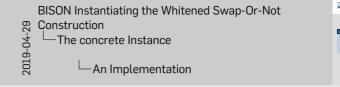
- Just chose the simplest bent function, the scalar product.
- This is also efficiently implementable.
- But, another drawback:
- Bent functions exists only for even n.
- Thus BISON cannot be instantiated for every block length n.
- In particular, due to reasons not covered here, we can actually only instantiate it for *odd* block lengths.



Construction

- $f_k(x) := ?$
- Key schedule?
- \blacksquare $\Theta(n)$ rounds?





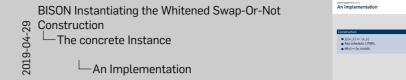


- Coming back to our initial question.
- And basically only for the sake of completeness, as we already saw this is going to be slow.



Construction

- Key schedule: LFSRs.
- \blacksquare $\Theta(n) = 3n$ rounds.



- Coming back to our initial question.
- And basically only for the sake of completeness, as we already saw this is going to be slow.
- We have specified everything, so let's benchmark against AES (what else).



Construction

- $f_k(x,y) := \langle x,y \rangle$
- Key schedule: LFSRs.
- $\Theta(n) = 3n$ rounds.

Cipher	Block size (bit)	Cycles/Byte mean
AES*	128	0.65
BISON [†]	129	3 064.08

BISON Instantiating the Whitened Swap-Or-Not Construction
The concrete Instance



• Coming back to our initial question.

An Implementation

- And basically only for the sake of completeness, as we already saw this is going to be slow.
- We have specified everything, so let's benchmark against AES (what else).
- OK, told you so, BISON is like 4700 times slower than AES.
- Or: more than three orders of magnitude.
- Optimising this will not help enough.

^{*} AES-128 on Skylake Intel® Core i7-7800X @ 3.5GHz, see Daemen et al. [The design of Xoodoo and Xoofff, Table 5].

[†] BISON on CoffeeLake Intel® Core i7-8700 @ 3.7 GHz.

Further Cryptanalysis



Linear Cryptanalysis

For $r \ge n$ rounds, the correlation of any non-trivial linear trail for BISON is upper bounded by $2^{-\frac{n+1}{2}}$.

Invariant Attacks

For $r \ge n$ rounds, neither invariant subspaces nor nonlinear invariant attacks do exist for BISON.

Zero Correlation

For r > 2n - 2 rounds, BISON does not exhibit any zero correlation linear hulls.

Impossible Differentials

For r > n rounds, there are no impossible differentials for BISON.

Algebraic Degree and Division Property

Algebraic degree grows *linearly*. Conservative estimate: for $r \ge 3n$ rounds, no attack possible.

BISON Instantiating the Whitened Swap-Or-Not Construction
—Further Analysis

Further Cryptanalysis

Further Cryptanalysis

Exec Cryptanalysis

For 2 in a month, the contains of any formation of any formation

- We did more cryptanalysis, but our results are more of the "classical" kind.
- For linear cryptanalysis, we bound the correlation of any non-trivial trail.
- Current known security arguments for resistance against invariant attacks apply.
- Zero correlation and impossible differentials do not exist for 2n rounds or more.
- Best attacks seem to exploit the algebraic degree.
- We show that it grows only linearly which is especially bad in comparison to SPN ciphers.
- The result on the algebraic degree also applies to NLFSRs or maximally unbalanced Feistel networks.
- Conservative estimation: might work for more than 2n rounds, but not for 3n or more.

Conclusion/Questions

Thank you for your attention!



BISON

- A first instance of the WSN construction
- Good results for differential cryptanalysis

Open Problems

- Construction for linear cryptanalysis?
- Similar args. for Unbalanced Feistel?

Thank you!

Questions?



BISON Instantiating the Whitened Swap-Or-Not
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Conclusion/Questions



Details

Construction
Further Analysis

BISON Instantiating the Whitened Swap-Or-Not

Details



BISON's round function

For round keys $k_i \in \mathbb{F}_2^n$ and $w_i \in \mathbb{F}_2^{n-1}$ the round function computes

$$R_{k_i,w_i}(x) := x + f_{b(i)}(w_i + \Phi_{k_i}(x)) \cdot k_i.$$

where

lacksquare Φ_{k_i} and $f_{b(i)}$ are defined as

$$\begin{split} \Phi_k(x) : \mathbb{F}_2^n &\to \mathbb{F}_2^{n-1} \\ \Phi_k(x) \coloneqq (x+x[i(k)] \cdot k)[j]_{j \neq i(k)}^{1 \leqslant j \leqslant n} & f_{b(i)} : \mathbb{F}_2^{\frac{n-1}{2}} \times \mathbb{F}_2^{\frac{n-1}{2}} \to \mathbb{F}_2 \\ f_{b(i)}(x,y) \coloneqq \langle x,y \rangle + b(i), \end{split}$$

■ and b(i) is 0 if $i \le \frac{r}{2}$ and 1 else.

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BISON Key Schedule



BISON's key schedule

Given

- primitive p_k , $p_w \in \mathbb{F}_2[x]$ with degrees n, n-1 and companion matrices C_k , C_w .
- master key $K = (k, w) \in (\mathbb{F}_2^n \times \mathbb{F}_2^{n-1}) \setminus \{0, 0\}$

The *i*th round keys are computed by

$$KS_i : \mathbb{F}_2^n \times \mathbb{F}_2^{n-1} \to \mathbb{F}_2^n \times \mathbb{F}_2^{n-1}$$

$$KS_i(k, w) := (k_i, c_i + w_i)$$

where

$$k_i = (C_k)^i k$$
, $c_i = (C_w)^{-i} e_1$, $w_i = (C_w)^i w$.

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